

Fig: Light baryon orbital spectrum for Λ_{QCD} = 0.25 GeV in the HW model. The **56** trajectory corresponds to L even P = + states, and the **70** to L odd P = - states.

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Non-Conformal Extension of Algebraic Structure (Soft Wall Model)

• We write the Dirac equation

$$(\alpha \Pi(\zeta) - \mathcal{M}) \,\psi(\zeta) = 0,$$

in terms of the matrix-valued operator Π

$$\Pi_{\nu}(\zeta) = -i\left(\frac{d}{d\zeta} - \frac{\nu + \frac{1}{2}}{\zeta}\gamma_5 - \kappa^2\zeta\gamma_5\right),\,$$

and its adjoint $\Pi^{\dagger},$ with commutation relations

$$\left[\Pi_{\nu}(\zeta), \Pi_{\nu}^{\dagger}(\zeta)\right] = \left(\frac{2\nu+1}{\zeta^2} - 2\kappa^2\right)\gamma_5.$$

• Solutions to the Dirac equation

$$\psi_{+}(\zeta) \sim z^{\frac{1}{2}+\nu} e^{-\kappa^{2}\zeta^{2}/2} L_{n}^{\nu}(\kappa^{2}\zeta^{2}),$$

$$\psi_{-}(\zeta) \sim z^{\frac{3}{2}+\nu} e^{-\kappa^{2}\zeta^{2}/2} L_{n}^{\nu+1}(\kappa^{2}\zeta^{2}).$$

• Eigenvalues

$$\mathcal{M}^2 = 4\kappa^2(n+\nu+1).$$

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• Baryon: twist-dimension 3 + L ($\nu = L + 1$)

$$\mathcal{O}_{3+L} = \psi D_{\{\ell_1} \dots D_{\ell_q} \psi D_{\ell_{q+1}} \dots D_{\ell_m}\} \psi, \quad L = \sum_{i=1}^m \ell_i.$$

• Define the zero point energy (identical as in the meson case) $\mathcal{M}^2 \to \mathcal{M}^2 - 4\kappa^2$:

$$\mathcal{M}^2 = 4\kappa^2(n+L+1).$$



 ${\rm Proton \ Regge \ Trajectory} \quad \kappa = 0.49 {\rm GeV}$

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SU(6)	S	L	Baryon State											
56	$\frac{1}{2}$	0	$N\frac{1}{2}^{+}(939)$											
	$\frac{2}{3}$	0	$\Delta \frac{3}{2}^{+}(1232)$											
70	$\frac{1}{2}$	1	$N\frac{1}{2}^{-}(1535) N\frac{3}{2}^{-}(1520)$											
	$\frac{3}{2}$	1	$N\frac{1}{2}^{-}(1650) N\frac{3}{2}^{-}(1700) N\frac{5}{2}^{-}(1675)$											
	$\frac{1}{2}$	1	$\Delta \frac{1}{2}^{-}(1620) \ \Delta \frac{3}{2}^{-}(1700)$											
56	$\frac{1}{2}$	2	$N\frac{3}{2}^{+}(1720) N\frac{5}{2}^{+}(1680)$											
	$\frac{3}{2}$	2	$\Delta_{\frac{1}{2}}^{\pm}(1910) \ \Delta_{\frac{3}{2}}^{\pm}(1920) \ \Delta_{\frac{5}{2}}^{\pm}(1905) \ \Delta_{\frac{7}{2}}^{\pm}(1950)$											
70	$\frac{1}{2}$	3	$N\frac{5}{2}^{-}$ $N\frac{7}{2}^{-}$											
	$\frac{3}{2}$	3	$N\frac{3}{2}^{-}$ $N\frac{5}{2}^{-}$ $N\frac{7}{2}^{-}(2190)$ $N\frac{9}{2}^{-}(2250)$											
	$\frac{1}{2}$	3	$\Delta \frac{5}{2}^{-}(1930) \ \Delta \frac{7}{2}^{-}$											
56	$\frac{1}{2}$	4	$N\frac{7}{2}^+$ $N\frac{9}{2}^+(2220)$											
	$\frac{3}{2}$	4	$\Delta \frac{5}{2}^+ \qquad \Delta \frac{7}{2}^+ \qquad \Delta \frac{9}{2}^+ \qquad \Delta \frac{11}{2}^+ (2420)$											
70	$\frac{1}{2}$	5	$N\frac{9}{2}^{-}$ $N\frac{11}{2}^{-}(2600)$											
	$\frac{3}{2}$	5	$N\frac{7}{2}^{-}$ $N\frac{9}{2}^{-}$ $N\frac{11}{2}^{-}$ $N\frac{13}{2}^{-}$											

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Space-Like Dirac Proton Form Factor

• Consider the spin non-flip form factors

$$F_{+}(Q^{2}) = g_{+} \int d\zeta J(Q,\zeta) |\psi_{+}(\zeta)|^{2},$$

$$F_{-}(Q^{2}) = g_{-} \int d\zeta J(Q,\zeta) |\psi_{-}(\zeta)|^{2},$$

where the effective charges g_+ and g_- are determined from the spin-flavor structure of the theory.

- Choose the struck quark to have $S^z = +1/2$. The two AdS solutions $\psi_+(\zeta)$ and $\psi_-(\zeta)$ correspond to nucleons with $J^z = +1/2$ and -1/2.
- For SU(6) spin-flavor symmetry

$$F_1^p(Q^2) = \int d\zeta J(Q,\zeta) |\psi_+(\zeta)|^2,$$

$$F_1^n(Q^2) = -\frac{1}{3} \int d\zeta J(Q,\zeta) \left[|\psi_+(\zeta)|^2 - |\psi_-(\zeta)|^2 \right],$$

where $F_1^p(0) = 1$, $F_1^n(0) = 0$.

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• Scaling behavior for large Q^2 : $Q^4 F_1^p(Q^2) \rightarrow \text{constant}$ Proton $\tau = 3$



SW model predictions for $\kappa = 0.424$ GeV. Data analysis from: M. Diehl *et al.* Eur. Phys. J. C **39**, 1 (2005).

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Neutron
$$\tau = 3$$



SW model predictions for $\kappa = 0.424$ GeV. Data analysis from M. Diehl *et al.* Eur. Phys. J. C **39**, 1 (2005).

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Features of Soft-Wall AdS/QCD

- Single-variable frame-independent radial Schrodinger equation
- Massless pion $(m_q = 0)$
- Regge Trajectories: universal slope in n and L
- Valid for all integer J & S.
- Dimensional Counting Rules for Hard Exclusive Processes
- Phenomenology: Space-like and Time-like Form Factors
- LF Holography: LFWFs; broad distribution amplitude
- No large Nc limit required
- Add quark masses to LF kinetic energy
- Systematically improvable -- diagonalize H_{LF} on AdS basis

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Líght-Front QCD Heisenberg Equation

 $H_{LC}^{QCD} |\Psi_h\rangle = \mathcal{M}_h^2 |\Psi_h\rangle$

	n	Sector	1 qq	2 99	3 qq g	4 qq qq	5 gg g	6 qq gg	7 qq qq g	8 qq qq qq	9 99 99	10 qq gg g	11 qq qq gg	12 qq qq qq g	13 ବସ୍ପିବସ୍ପିବସ୍ପିବସ୍ପି
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Use AdS/QCD basis functions!

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Use AdS/CFT orthonormal LFWFs as a basis for diagonalizing the QCD LF Hamiltonian

- Good initial approximant
- Better than plane wave basis Pauli, Hornbostel, Hiller, McCartor, sjb
- DLCQ discretization -- highly successful 1+1
- Use independent HO LFWFs, remove CM motion
 Vary, Harinandrath, Maris, sjb
- Similar to Shell Model calculations

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New Perspectives for QCD from AdS/CFT

- LFWFs: Fundamental frame-independent description of hadrons at amplitude level
- Holographic Model from AdS/CFT : Confinement at large distances and conformal behavior at short distances
- Model for LFWFs, meson and baryon spectra: many applications!
- New basis for diagonalizing Light-Front Hamiltonian
- Physics similar to MIT bag model, but covariant. No problem with support 0 < x < 1.
- Quark Interchange dominant force at short distances

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CIM: Blankenbecler, Gunion, sjb



Quark Interchange (Spín exchange ín atomatom scattering) Gluon Exchange (Van der Waal --Landshoff)

$$\frac{d\sigma}{dt} = \frac{|M(s,t)|^2}{s^2}$$

 $M(t,u)_{
m interchange} \propto rac{1}{ut^2}$

M(s,t)gluonexchange $\propto sF(t)$

MIT Bag Model (de Tar), large N_C, ('t Hooft), AdS/CFT all predict dominance of quark interchange:

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Comparison of Exclusive Reactions at Large t

B. R. Baller, ^(a) G. C. Blazey, ^(b) H. Courant, K. J. Heller, S. Heppelmann, ^(c) M. L. Marshak, E. A. Peterson, M. A. Shupe, and D. S. Wahl^(d) University of Minnesota, Minneapolis, Minnesota 55455

> D. S. Barton, G. Bunce, A. S. Carroll, and Y. I. Makdisi Brookhaven National Laboratory, Upton, New York 11973

> > and

S. Gushue^(e) and J. J. Russell

Southeastern Massachusetts University, North Dartmouth, Massachusetts 02747 (Received 28 October 1987; revised manuscript received 3 February 1988)

Cross sections or upper limits are reported for twelve meson-baryon and two baryon-baryon reactions for an incident momentum of 9.9 GeV/c, near 90° c.m.: $\pi^{\pm}p \rightarrow p\pi^{\pm}, p\rho^{\pm}, \pi^{+}\Delta^{\pm}, K^{+}\Sigma^{\pm}, (\Lambda^{0}/\Sigma^{0})K^{0};$ $K^{\pm}p \rightarrow pK^{\pm}; p^{\pm}p \rightarrow pp^{\pm}$. By studying the flavor dependence of the different reactions, we have been able to isolate the quark-interchange mechanism as dominant over gluon exchange and quark-antiquark annihilation.





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Anomalous Threshold Dependence

 $[qq\bar{q}\bar{q}\bar{q}]$ or $[ggg] J^{PC} = 1^{--}$ resonance?

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S. S. Adler *et al.* PHENIX Collaboration *Phys. Rev. Lett.* **91**, 172301 (2003). *Particle ratio changes with centrality!*



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Crucial Test of Leading -Twist QCD: Scaling at fixed x_T



$$E\frac{d\sigma}{d^3p}(pN \to \pi X) = \frac{F(x_T, \theta_{CM})}{p_T^{neff}}$$

Parton model: $n_{eff} = 4$

As fundamental as Bjorken scaling in DIS

Conformal scaling: $n_{eff} = 2 n_{active} - 4$

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 $\sqrt{s}^n E \frac{d\sigma}{d^3 p} (pp \to \gamma X)$ at fixed x_T

Tannenbaum



Scaling of direct photon production consistent with PQCD

> Stan Brodsky SLAC

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QCD prediction: Modification of power fall-off due to DGLAP evolution and the Running Coupling



Key test of PQCD: power-law fall-off at fixed x_T

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Protons produced in AuAu collisions at RHIC do not exhibit clear scaling properties in the available p_T range. Shown are data for central (0-5%) and for peripheral (60-90%) collisions.



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S. S. Adler et al. PHENIX Collaboration Phys. Rev. Lett. 91, 172301 (2003).

Baryon Anomaly: Particle ratio changes with centrality!



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 $\sqrt{s_{NN}} = 130$ and 200 GeV



Proton power changes with centrality !

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Baryon can be made directly within hard subprocess





S. S. Adler *et al.* PHENIX Collaboration *Phys. Rev. Lett.* **91**, 172301 (2003). *Particle ratio changes with centrality!*



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Anne Sickles



Paul Sorensen



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Power-law exponent $n(x_T)$ for π^0 and h spectra in central and peripheral Au+Au collisions at $\sqrt{s_{NN}} = 130$ and 200 GeV

S. S. Adler, et al., PHENIX Collaboration, Phys. Rev. C 69, 034910 (2004) [nucl-ex/0308006].



Proton production dominated by color-transparent direct high n_{eff} subprocesses

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Lambda can be made directly within hard subprocess



Baryon Anomaly: Evídence for Dírect, Hígher-Twíst Subprocesses

- Explains anomalous power behavior at fixed x_T
- Protons more likely to come from direct higher-twist subprocess than pions
- Protons less absorbed than pions in central nuclear collisions because of color transparency
- Predicts increasing proton to pion ratio in central collisions
- Proton power n_{eff} increases with centrality since leading twist contribution absorbed
- Fewer same-side hadrons for proton trigger at high centrality
- Exclusive-inclusive connection at $x_T = I$

Erlich, Katz, Son, Stephanov

In presence of quark masses the Holographic LF wave equation is $(\zeta = z)$

$$\left[-\frac{d^2}{d\zeta^2} + V(\zeta) + \frac{X^2(\zeta)}{\zeta^2}\right]\phi(\zeta) = \mathcal{M}^2\phi(\zeta),$$

and thus

$$\delta M^2 = \left\langle \frac{X^2}{\zeta^2} \right\rangle.$$

Identify:

$$X(z) = \frac{m}{\sqrt{x}} z - \sqrt{x} \langle \bar{\psi}\psi \rangle z^3$$

Condensate evaluated ínsíde hadron boundary

Thus

$$\delta M^2 = \sum_i \left\langle \frac{m_i^2}{x_i} \right\rangle - 2 \sum_i m_i \langle \bar{\psi}\psi \rangle \langle z^2 \rangle + \langle \bar{\psi}\psi \rangle^2 \langle z^4 \rangle.$$

Línear quark mass term generated by transition from valence to meson-nucleon LF Fock state

$$\Delta M_p^2 = < p_F |H_I^{LF}| p_I > H_I^{LF} = g A \bar{\psi} \gamma^\mu \psi \sim -g m_q a_g b_q^\dagger d_q^\dagger$$

de Teramond, Shrock, sjb

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The arrows and superscripts indicate helicity/chirality

Línear quark mass term generated by transition from valence to meson-nucleon LF Fock state **Dynamical chiral symmetry breaking**

Relate Observables to Each Other

- Eliminate intermediate scheme
- No scale ambiguity
- Transitive!
- Commensurate Scale Relations
- Example: Generalized Crewther Relation

$$R_{e^{+}e^{-}}(Q^{2}) \equiv 3 \sum_{\text{flavors}} e_{q^{2}} \left[1 + \frac{\alpha_{R}(Q)}{\pi} \right].$$
$$\int_{0}^{1} dx \left[g_{1}^{ep}(x,Q^{2}) - g_{1}^{en}(x,Q^{2}) \right] \equiv \frac{1}{3} \left| \frac{g_{A}}{g_{V}} \right| \left[1 - \frac{\alpha_{g_{1}}(Q)}{\pi} \right].$$

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$$\begin{split} \frac{\alpha_R(Q)}{\pi} &= \frac{\alpha_{\overline{\mathrm{MS}}}(Q)}{\pi} + \left(\frac{\alpha_{\overline{\mathrm{MS}}}(Q)}{\pi}\right)^2 \left[\left(\frac{41}{8} - \frac{11}{3}\zeta_3\right) C_A - \frac{1}{8}C_F + \left(-\frac{11}{12} + \frac{2}{3}\zeta_3\right) f \right] \\ &\quad + \left(\frac{\alpha_{\overline{\mathrm{MS}}}(Q)}{\pi}\right)^3 \left\{ \left(\frac{90445}{2592} - \frac{2737}{108}\zeta_3 - \frac{55}{18}\zeta_5 - \frac{121}{432}\pi^2\right) C_A^2 + \left(-\frac{127}{48} - \frac{143}{12}\zeta_3 + \frac{55}{3}\zeta_5\right) C_A C_F - \frac{23}{32}C_F^2 \right. \\ &\quad + \left[\left(-\frac{970}{81} + \frac{224}{27}\zeta_3 + \frac{5}{9}\zeta_5 + \frac{11}{108}\pi^2\right) C_A + \left(-\frac{29}{96} + \frac{19}{6}\zeta_3 - \frac{10}{3}\zeta_5\right) C_F \right] f \\ &\quad + \left(\frac{151}{162} - \frac{19}{27}\zeta_3 - \frac{1}{108}\pi^2\right) f^2 + \left(\frac{11}{144} - \frac{1}{6}\zeta_3\right) \frac{d^{abc}d^{abc}}{C_F d(R)} \frac{\left(\sum_f Q_f\right)^2}{\sum_f Q_f^2} \right\}. \end{split}$$

$$\begin{aligned} \frac{\alpha_{g_1}(Q)}{\pi} &= \frac{\alpha_{\overline{\mathrm{MS}}}(Q)}{\pi} + \left(\frac{\alpha_{\overline{\mathrm{MS}}}(Q)}{\pi}\right)^2 \left[\frac{23}{12}C_A - \frac{7}{8}C_F - \frac{1}{3}f\right] \\ &+ \left(\frac{\alpha_{\overline{\mathrm{MS}}}(Q)}{\pi}\right)^3 \left\{ \left(\frac{5437}{648} - \frac{55}{18}\zeta_5\right)C_A^2 + \left(-\frac{1241}{432} + \frac{11}{9}\zeta_3\right)C_AC_F + \frac{1}{32}C_F^2 \right. \\ &+ \left[\left(-\frac{3535}{1296} - \frac{1}{2}\zeta_3 + \frac{5}{9}\zeta_5\right)C_A + \left(\frac{133}{864} + \frac{5}{18}\zeta_3\right)C_F \right]f + \frac{115}{648}f^2 \right\}. \end{aligned}$$

Eliminate MSbar, Find Amazing Simplification

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Lu, Kataev, Gabadadze, Sjb

Generalized Crewther Relation

$$[1 + \frac{\alpha_R(s^*)}{\pi}][1 - \frac{\alpha_{g_1}(q^2)}{\pi}] = 1$$
$$\sqrt{s^*} \simeq 0.52Q$$

Conformal relation true to all orders in perturbation theory No radiative corrections to axial anomaly Nonconformal terms set relative scales (BLM) Analytic matching at quark thresholds No renormalization scale ambiguity!

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Novel QCD Phenomena and Perspectives

- Hadroproduction at large transverse momentum does not derive exclusively from 2 to 2 scattering subprocesses: Baryon Anomaly at RHIC Sickles, sjb
- Color Transparency Mueller, sjb; Diffractive Di-Jets and Tri-jets Strikman et al
- Heavy quark distributions do not derive exclusively from DGLAP or gluon splitting -- component intrinsic to hadron wavefunction. Hoyer, et al
- Higgs production at large x_F from intrinsic heavy quarks Kopeliovitch, Goldhaber, Schmidt, Soffer, sjb
- Initial and final-state interactions are not always power suppressed in a hard QCD reaction: Sivers Effect, Diffractive DIS, Breakdown of Lam Tung PQCD Relation Schmidt, Hwang, Hoyer, Boer, sjb; Collins
- LFWFS are universal, but measured nuclear parton distributions are not universal -- antishadowing is flavor dependent Schmidt, Yang, sjb
- Renormalization scale is not arbitrary; multiple scales, unambiguous at given order. Disentangle running coupling and conformal effects, Skeleton expansion: Gardi, Grunberg, Rathsman, sjb

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Quark and Gluon condensates reside within hadrons: Shrock, sjb
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