

**$DY \cos 2\phi$  correlation at leading twist from double ISI**

# Double Initial-State Interactions

generate anomalous  $\cos 2\phi$

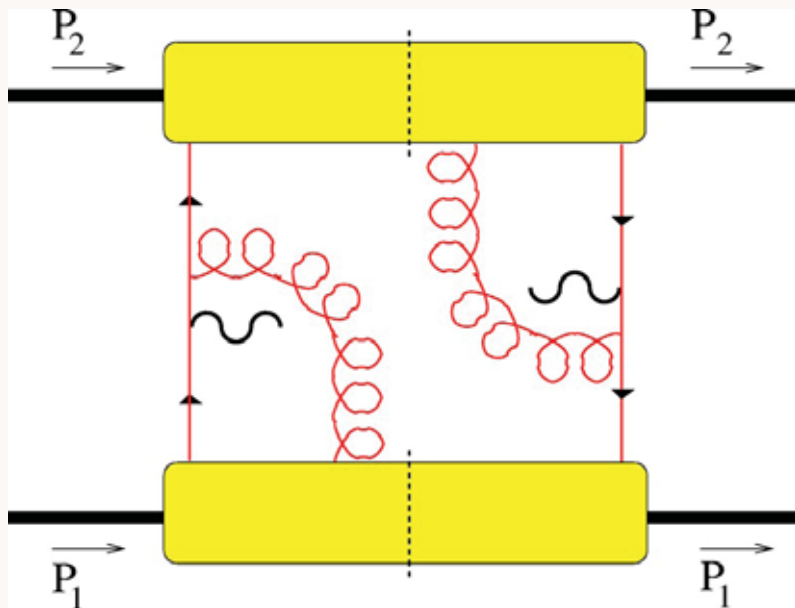
Boer, Hwang, sjb

## Drell-Yan planar correlations

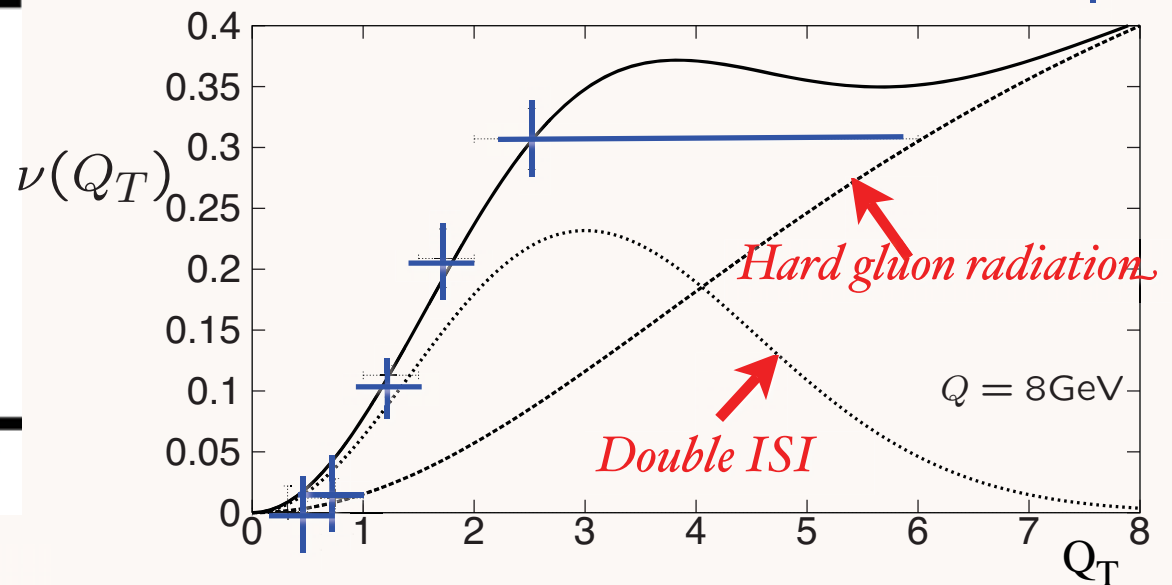
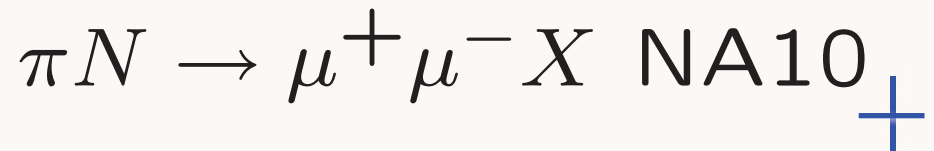
$$\frac{1}{\sigma} \frac{d\sigma}{d\Omega} \propto \left( 1 + \lambda \cos^2 \theta + \mu \sin 2\theta \cos \phi + \frac{\nu}{2} \sin^2 \theta \cos 2\phi \right)$$

PQCD Factorization (Lam Tung):  $1 - \lambda - 2\nu = 0$

$$\frac{\nu}{2} \propto h_1^\perp(\pi) h_1^\perp(N)$$



**Violates Lam-Tung relation!**



Model: Boer,

Stan Brodsky

SLAC & IPPP

Manchester  
August 5, 2008

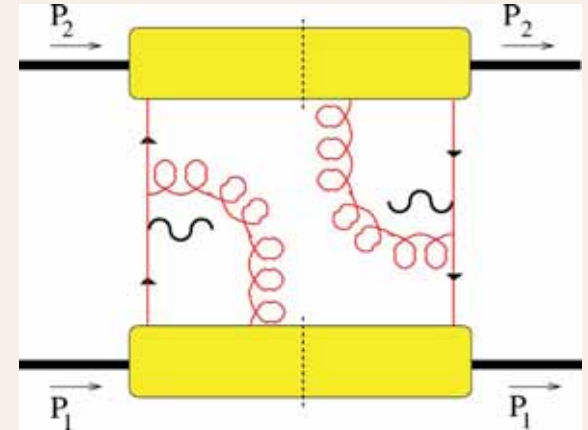
**Light-Front Holography**

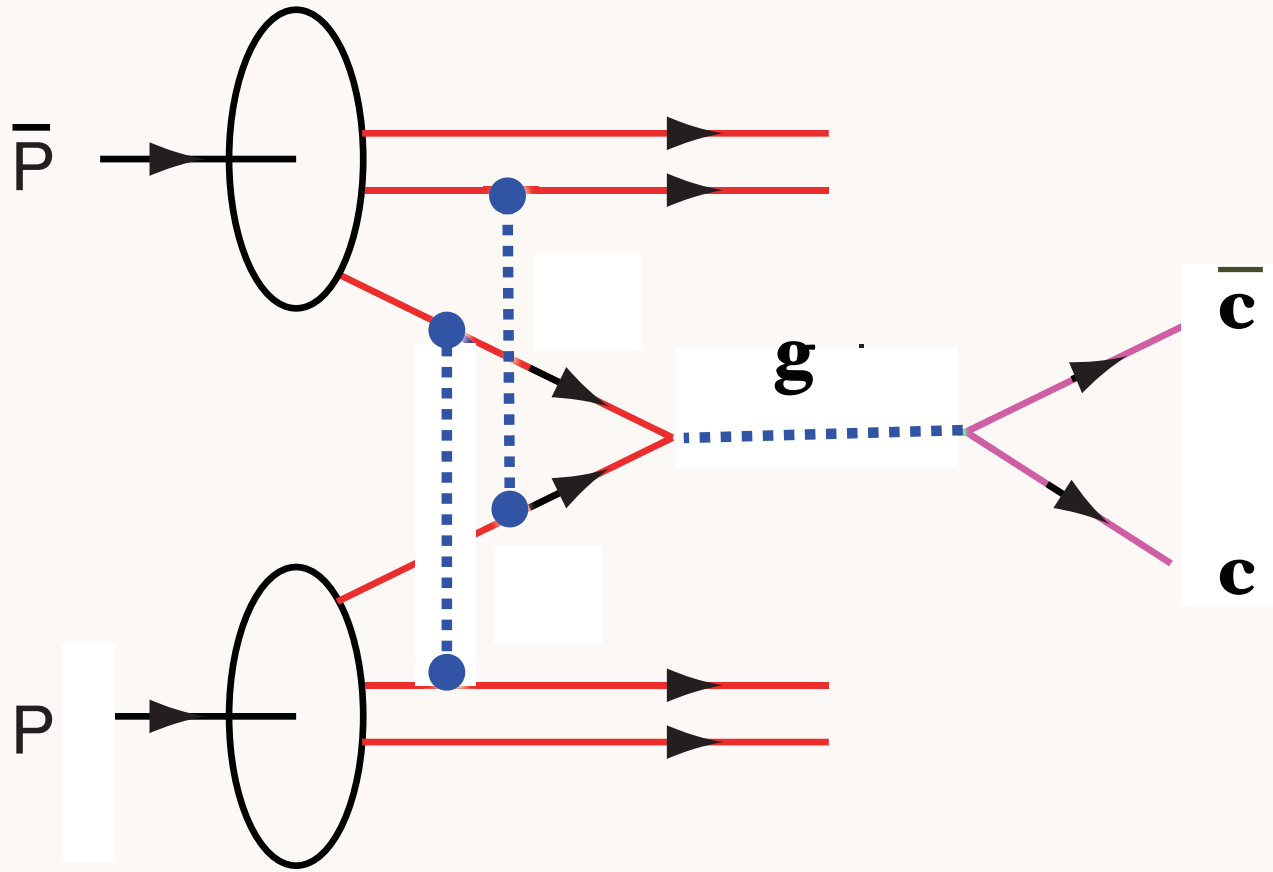
# Anomalous effect from Double ISI in Massive Lepton Production

Boer, Hwang, sjb

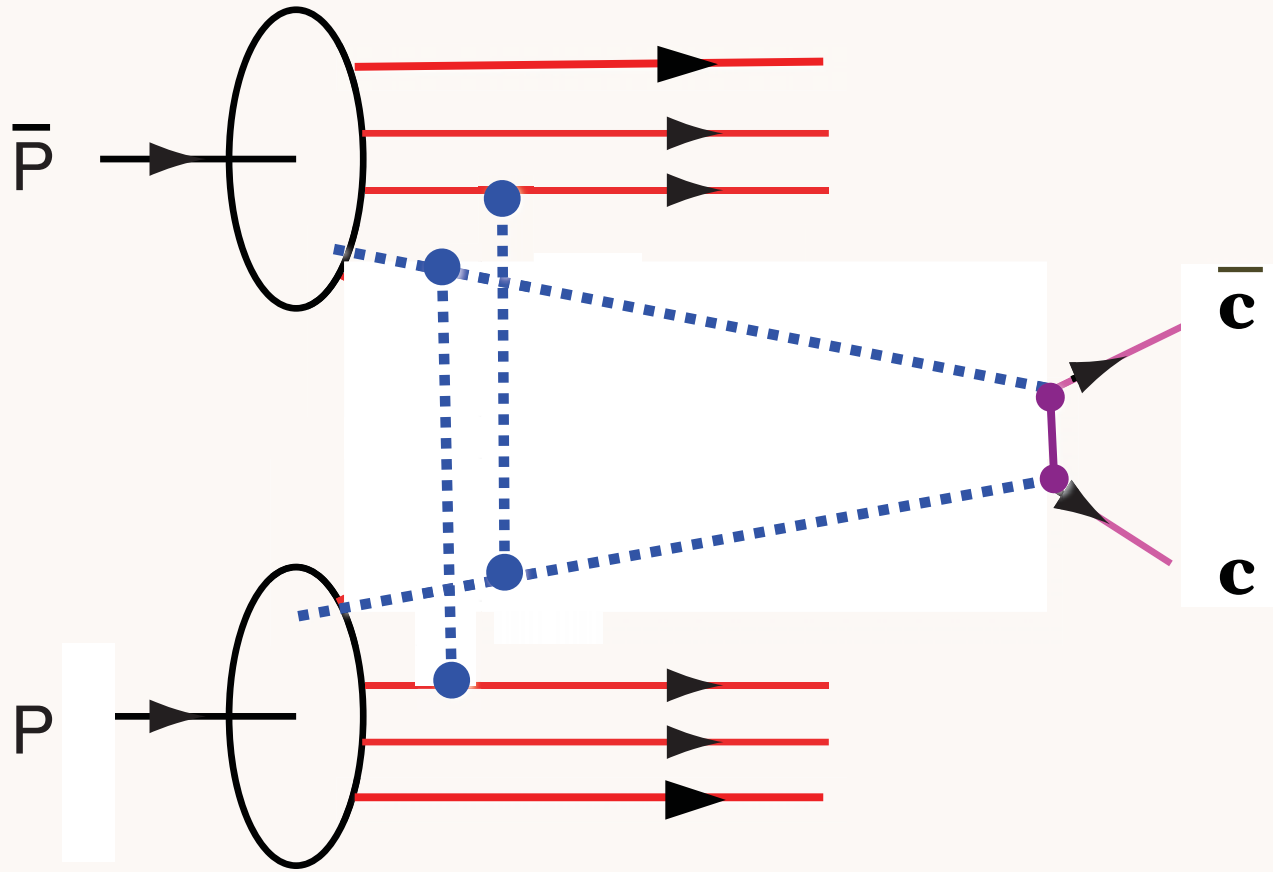
$\cos 2\phi$  correlation

- Leading Twist, valence quark dominated
- Violates Lam-Tung Relation!
- Not obtained from standard PQCD subprocess analysis
- Normalized to the square of the single spin asymmetry in semi-inclusive DIS
- No polarization required
- Challenge to standard picture of PQCD Factorization



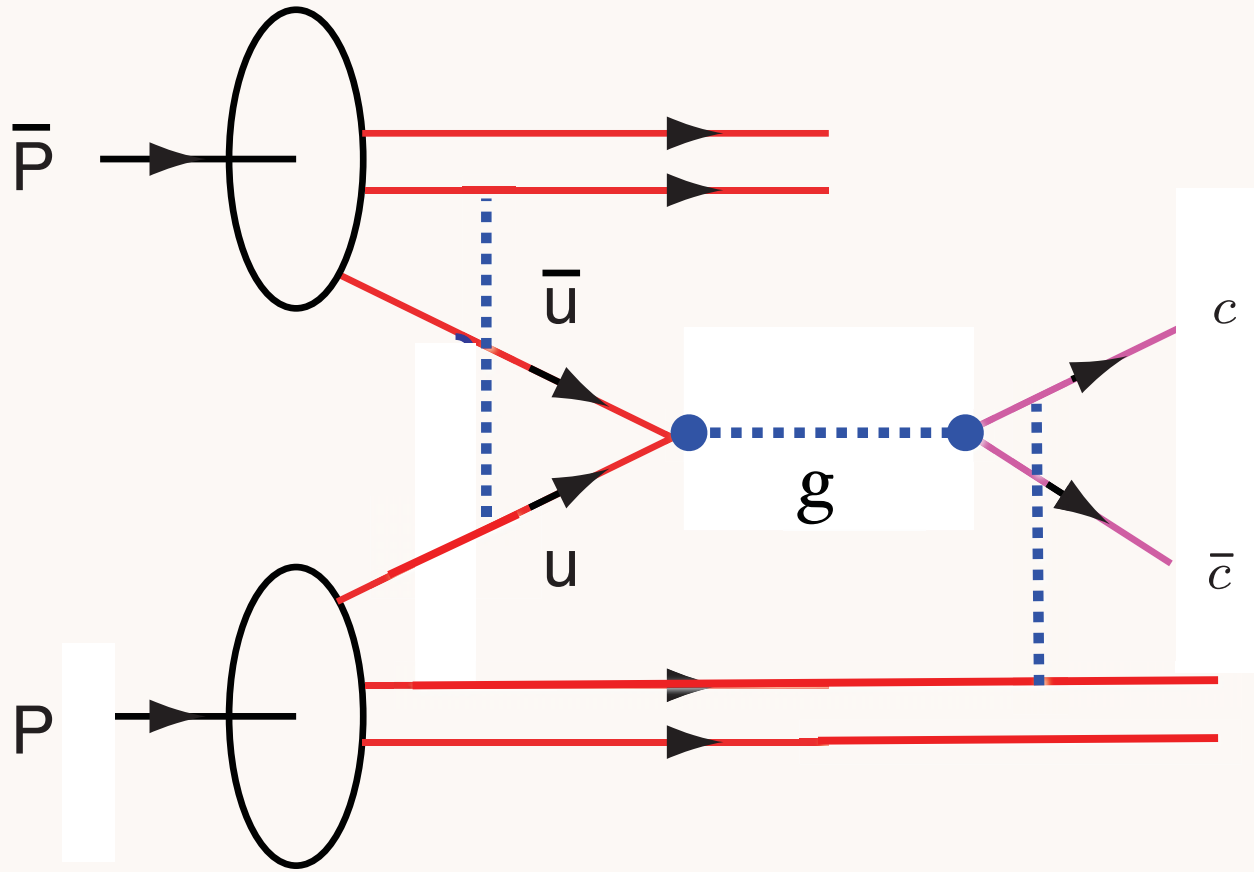


$\cos 2\phi$  correlation for quarkonium production at leading twist from double ISI



$\cos 2\phi$  correlation for quarkonium production at leading twist from double ISI

**Enhanced by gluon color charge**

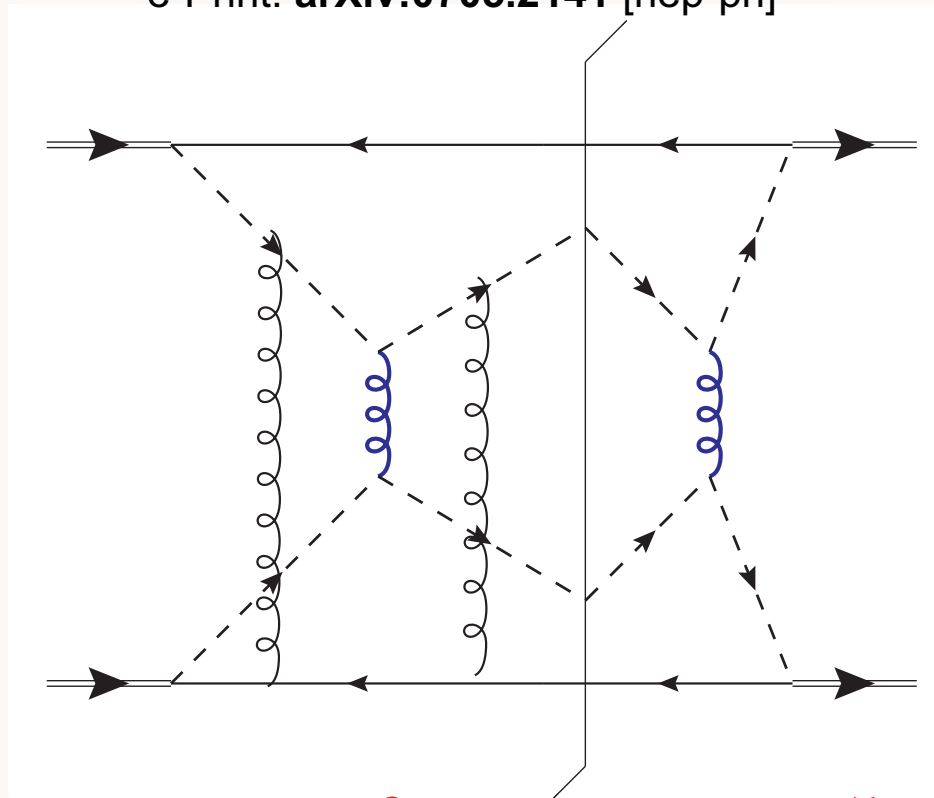


*Problem for factorization when both ISI and FSI occur*

# Factorization is violated in production of high-transverse-momentum particles in hadron-hadron collisions

John Collins, [Jian-Wei Qiu](#) . ANL-HEP-PR-07-25, May 2007.

e-Print: [arXiv:0705.2141](#) [hep-ph]



## *Implications for QCD at the LHC*

The exchange of two extra gluons, as in this graph, will tend to give non-factorization in unpolarized cross sections.

**Manchester**  
**August 5, 2008**

**Light-Front Holography**

47

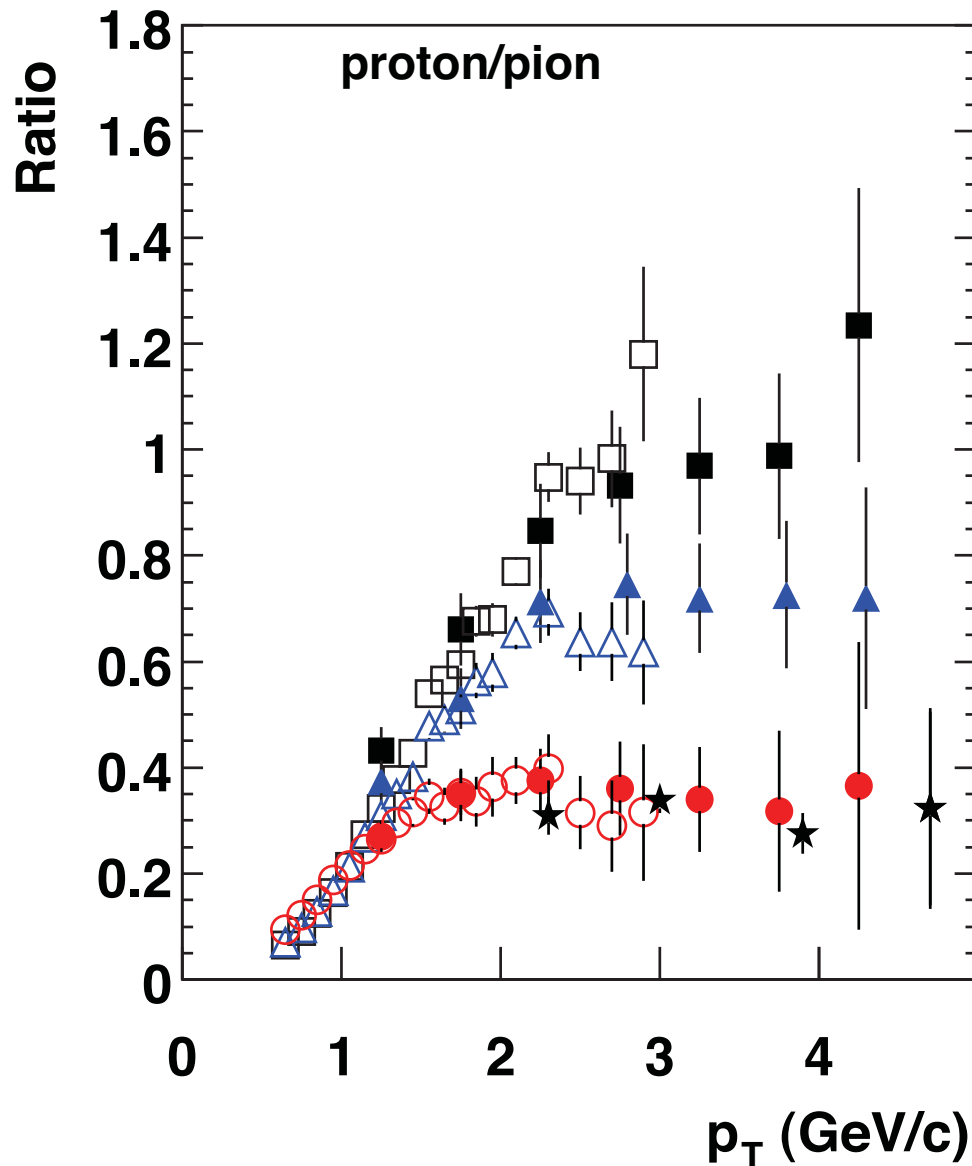
**Stan Brodsky**  
**SLAC & IPPP**

- Although we know the QCD Lagrangian, we have only begun to understand its remarkable properties and features.
- Novel QCD Phenomena: hidden color, color transparency, strangeness asymmetry, intrinsic charm, anomalous heavy quark phenomena, anomalous spin effects, single-spin asymmetries, odderon, diffractive deep inelastic scattering, dangling gluons, shadowing, antishadowing, QGP, CGC, ...

*Truth is stranger than fiction, but it is because Fiction is obliged to stick to possibilities.*      *—Mark Twain*



*Baryon Anomaly: Particle ratio changes with centrality!*



*Protons less absorbed in nuclear collisions than pions*

← **Central**

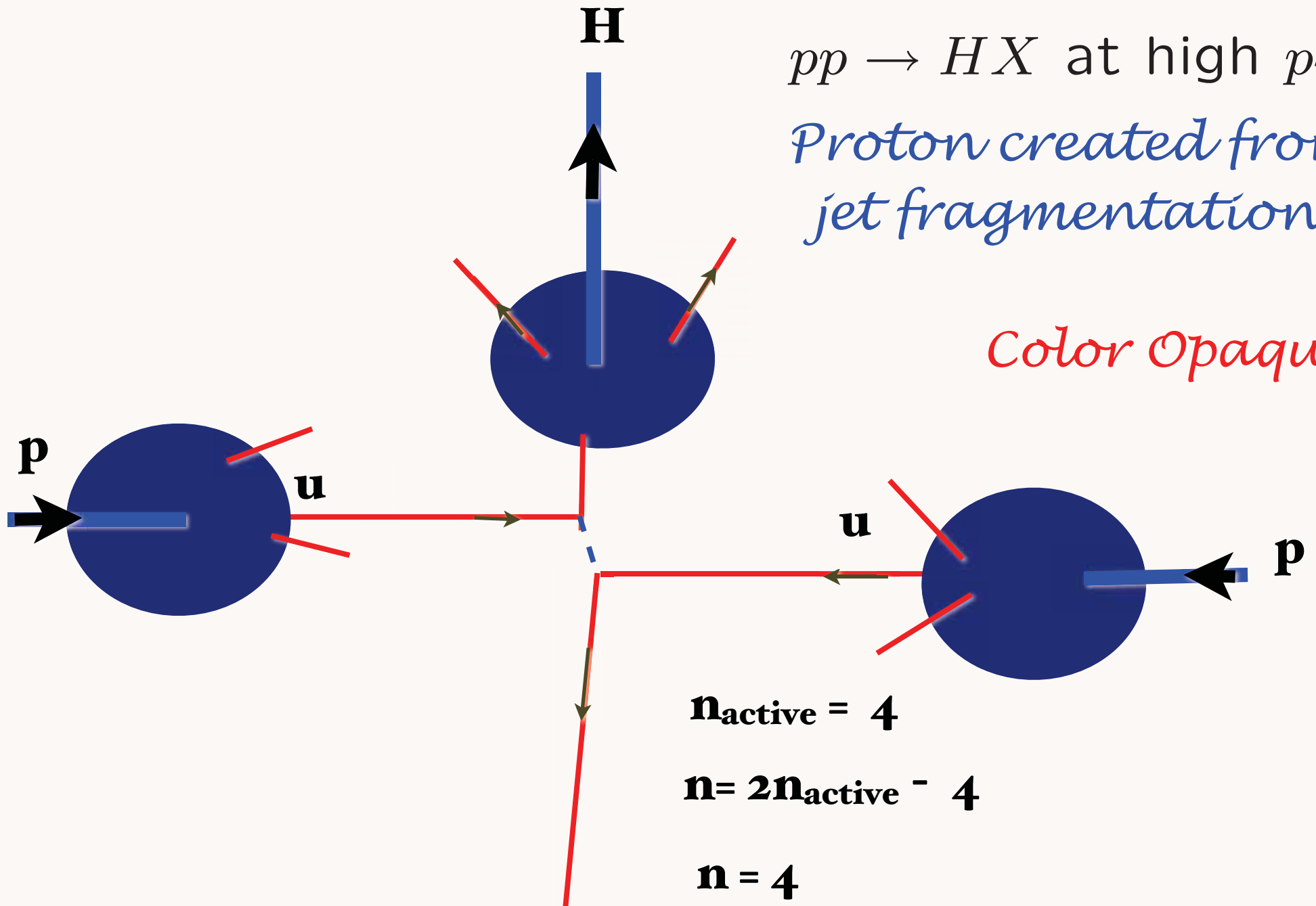
- ■ Au+Au 0-10%
- △ ▲ Au+Au 20-30%
- ● Au+Au 60-92%
- ★ p+p,  $\sqrt{s} = 53$  GeV, ISR
- e<sup>+</sup>e<sup>-</sup>, gluon jets, DELPHI
- ..... e<sup>+</sup>e<sup>-</sup>, quark jets, DELPHI

← **Peripheral**

Sickles, sjb

$pp \rightarrow HX$  at high  $p_T$   
*Proton created from  
jet fragmentation*

*Color Opaque*



$$n_{\text{active}} = 4$$

$$n = 2n_{\text{active}} - 4$$

$$n = 4$$

**u**  
**Light-Front Holography**

Manchester  
August 5, 2008

Stan Brodsky  
SLAC & IPPP

*Crucial Test of Leading -Twist QCD:  
Scaling at fixed  $x_T$*

$$x_T = \frac{2p_T}{\sqrt{s}}$$

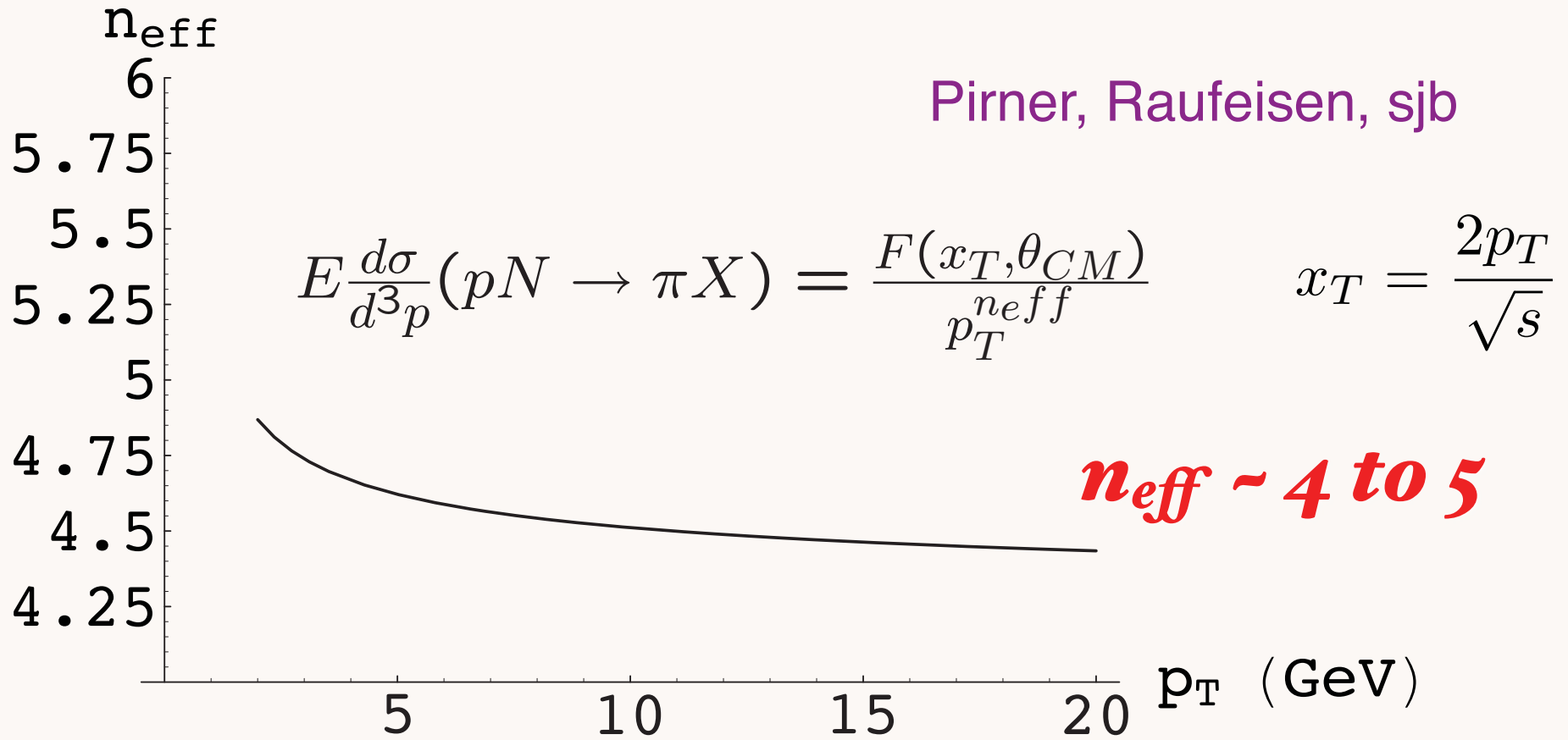
$$E \frac{d\sigma}{d^3p} (pN \rightarrow \pi X) = \frac{F(x_T, \theta_{CM})}{p_T^{n_{eff}}}$$

***Parton model:  $n_{eff} = 4$***

***As fundamental as Bjorken scaling in DIS***

**Conformal scaling:  $n_{eff} = 2 n_{active} - 4$**

*QCD prediction: Modification of power fall-off due to DGLAP evolution and the Running Coupling*

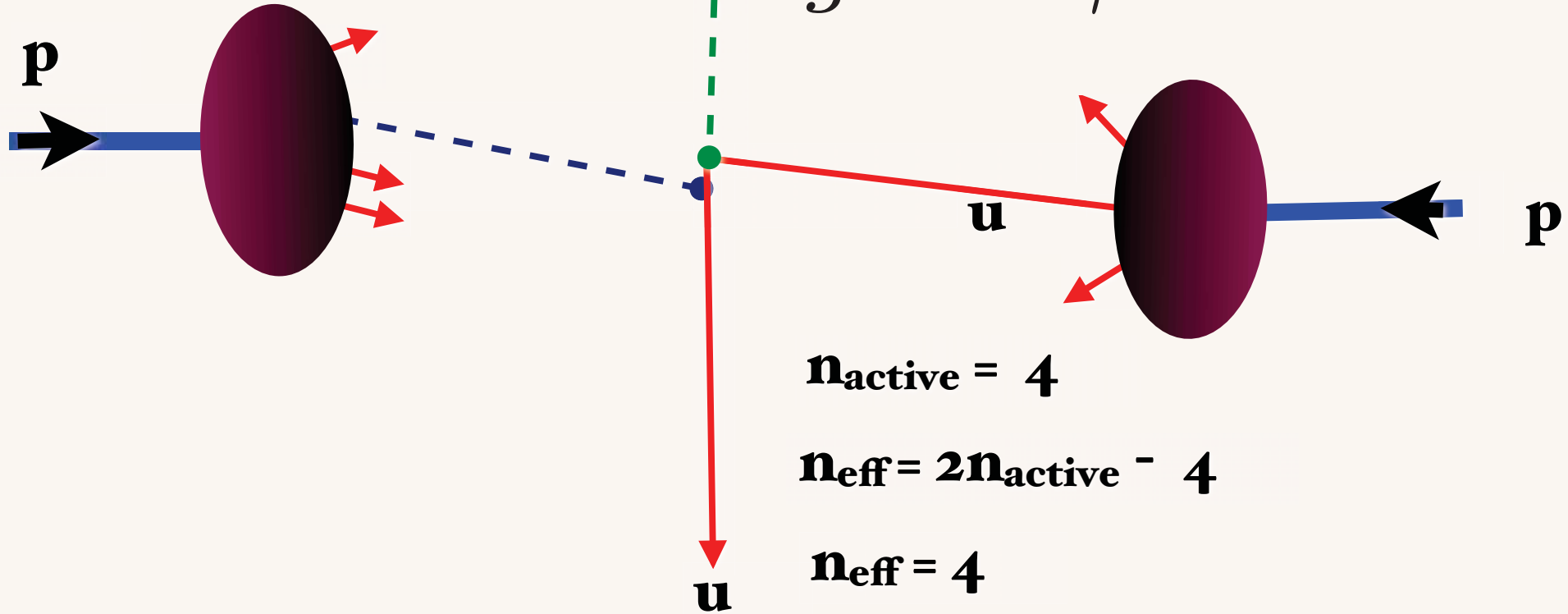


*Key test of PQCD: power-law fall-off at fixed  $x_T$*

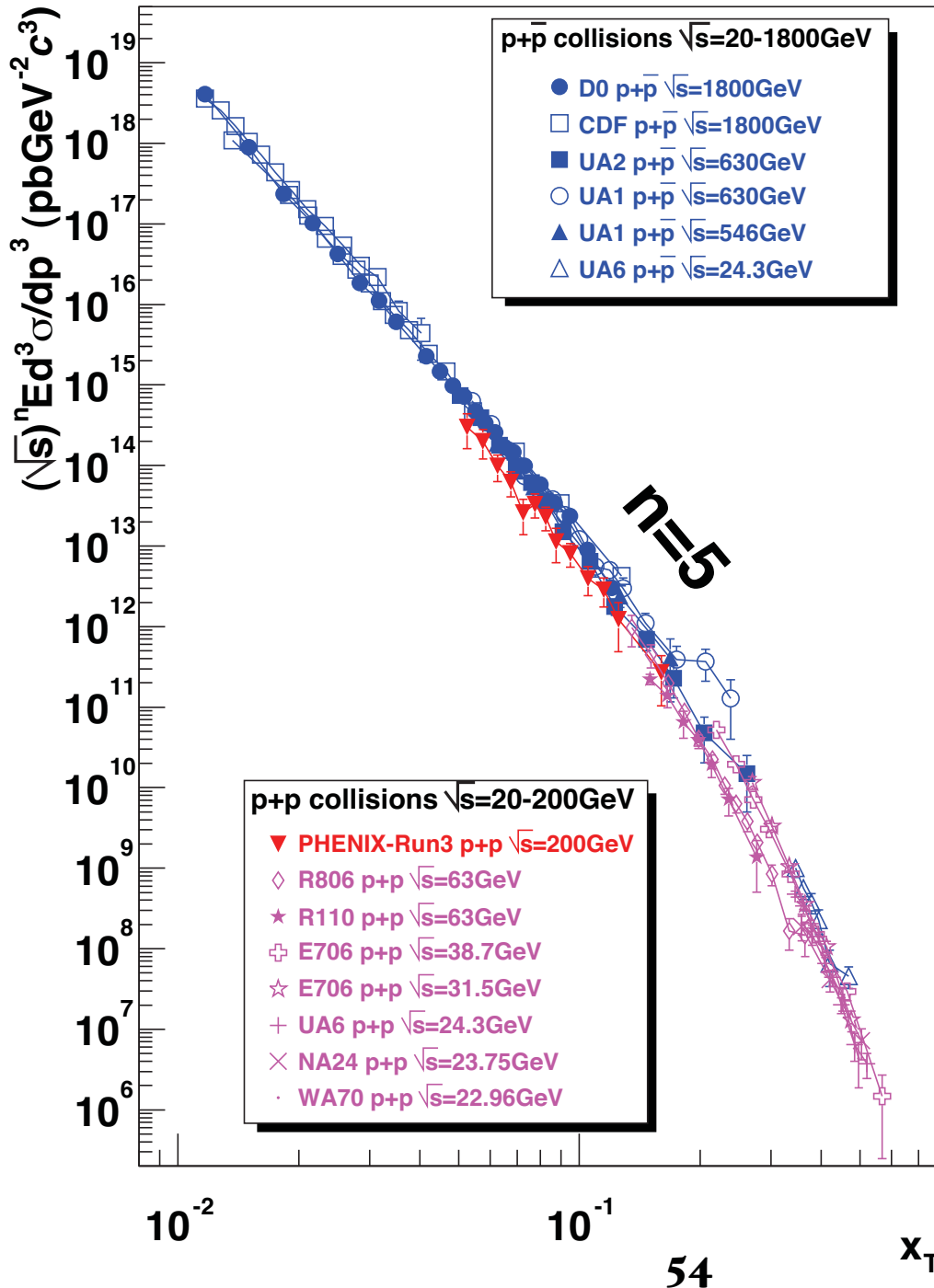
$pp \rightarrow \gamma X$

$$E \frac{d\sigma}{d^3p}(pp \rightarrow \gamma X) = \frac{F(\theta_{cm}, x_T)}{p_T^4}$$

$gu \rightarrow \gamma u$

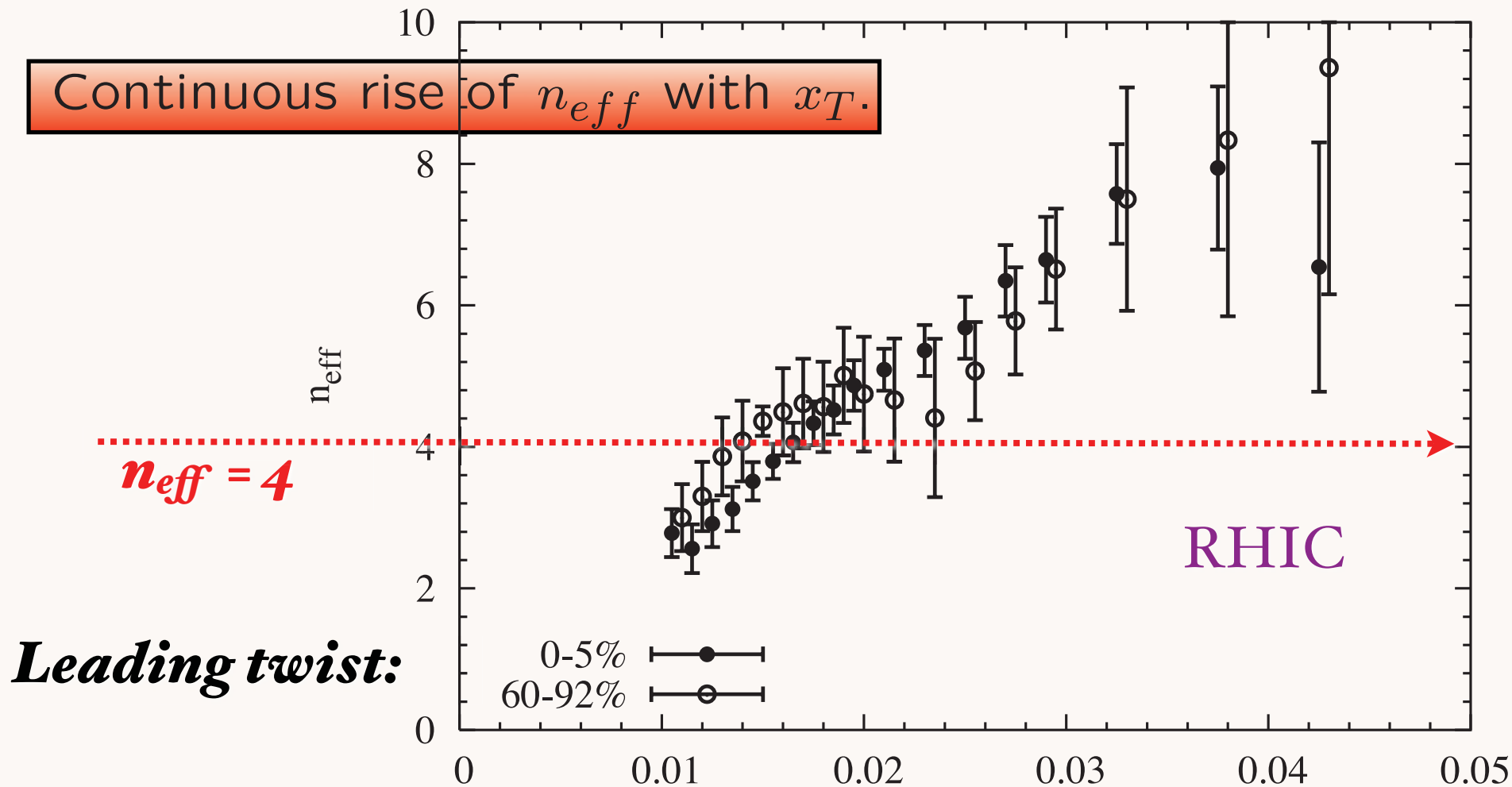


$$\sqrt{s}^n E \frac{d\sigma}{d^3p} (pp \rightarrow \gamma X) \text{ at fixed } x_T$$



**Scaling of direct  
photon  
production  
consistent with  
PQCD**

Protons produced in AuAu collisions at RHIC do not exhibit clear scaling properties in the available  $p_T$  range. Shown are data for central (0 – 5%) and for peripheral (60 – 90%) collisions.



$$E \frac{d\sigma}{d^3p} (pN \rightarrow pX) = \frac{F(x_T, \theta_{CM})}{p_T^{n_{eff}}} x_T$$

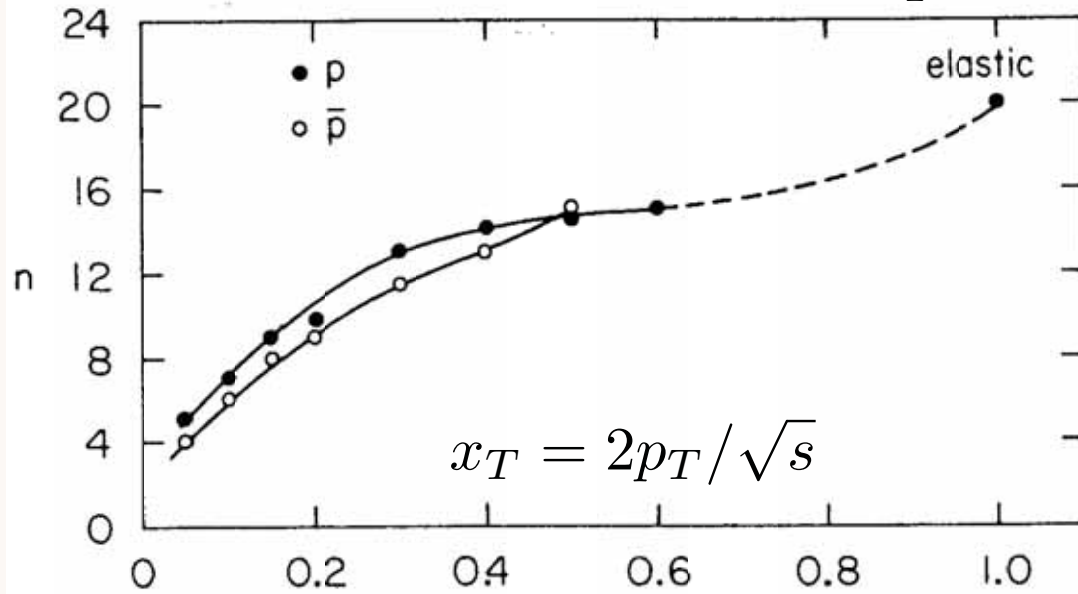
Manchester  
August 5, 2008

Light-Front Holography

55

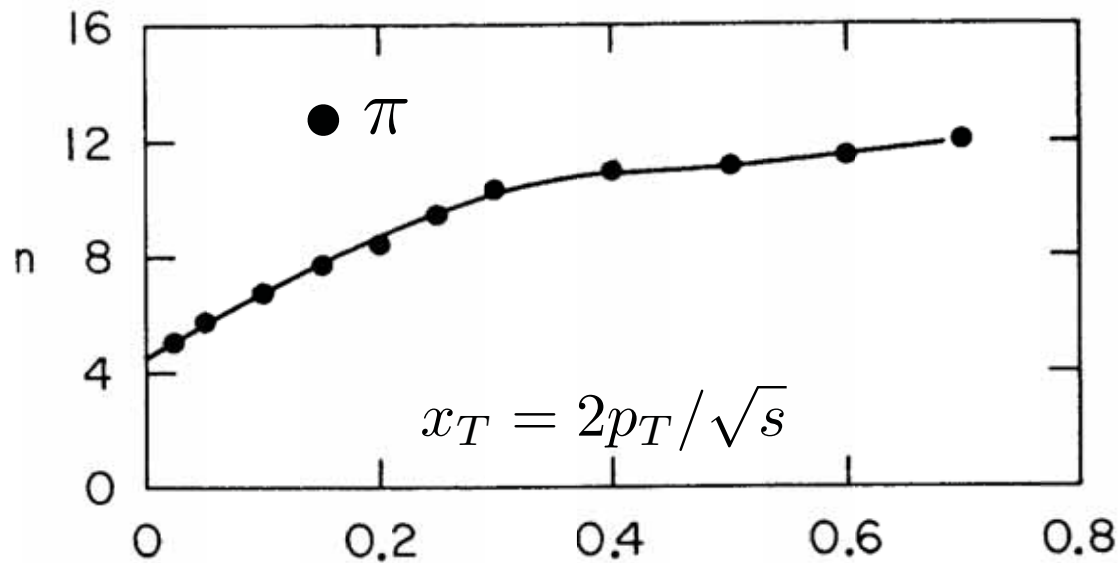
Stan Brodsky  
SLAC & IPPP

$$E \frac{d\sigma}{d^3p} (pp \rightarrow HX) = \frac{F(x_T, \theta_{cm} = \pi/2)}{p_T^n}$$



*Clear evidence  
for higher-twist  
contributions*

**Fermilab, ISR data**



**Manchester  
August 5, 2008**

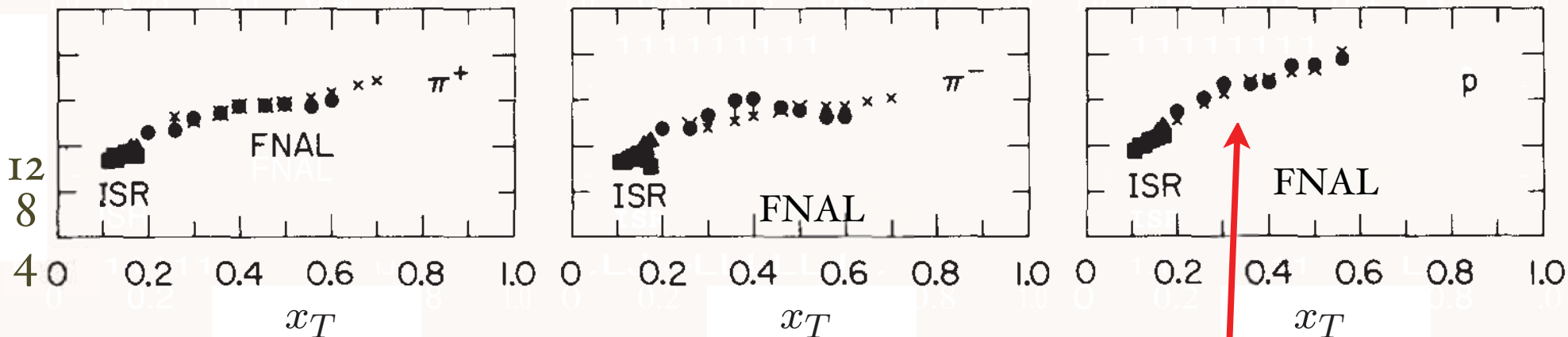
**Light-Front Holography**

56

**Stan Brodsky  
SLAC & IPPP**



$$E \frac{d\sigma}{d^3p} (pp \rightarrow HX) = \frac{F(x_T, \theta_{CM})}{n_{eff} p_T}$$



$$E \frac{d\sigma}{d^3p} (pp \rightarrow pX) = \frac{F(x_T, \theta_{CM})}{p_T^{12}}$$

$$E \frac{d\sigma}{d^3p} (pp \rightarrow pX) = \frac{F(x_T, \theta_{CM})}{p_T^8}$$

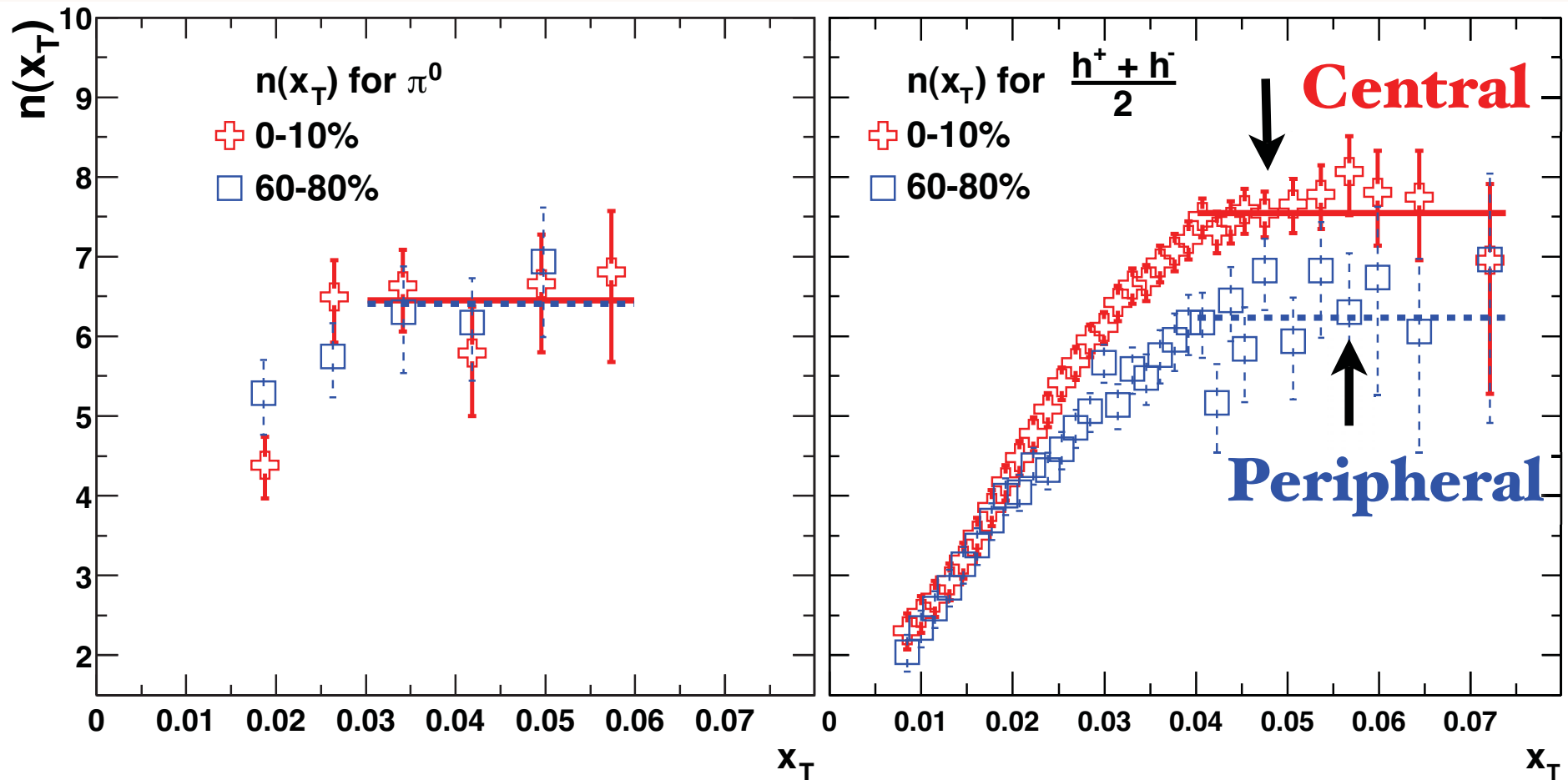
*Trend consistent with RHIC at small  $x_T$*

Manchester  
August 5, 2008

$x_T$  Light-Front Holography

Stan Brodsky  
SLAC & IPPP

$$\sqrt{s_{NN}} = 130 \text{ and } 200 \text{ GeV}$$



*Proton power changes with centrality !*

Manchester  
August 5, 2008

**Light-Front Holography**

58

Stan Brodsky  
SLAC & IPPP

# Baryon can be made directly within hard subprocess

## Coalescence within hard subprocess

$$b_{\perp} \simeq 1/p_T$$

Bjorken

Blankenbecler, Gunion, sjb

Berger, sjb

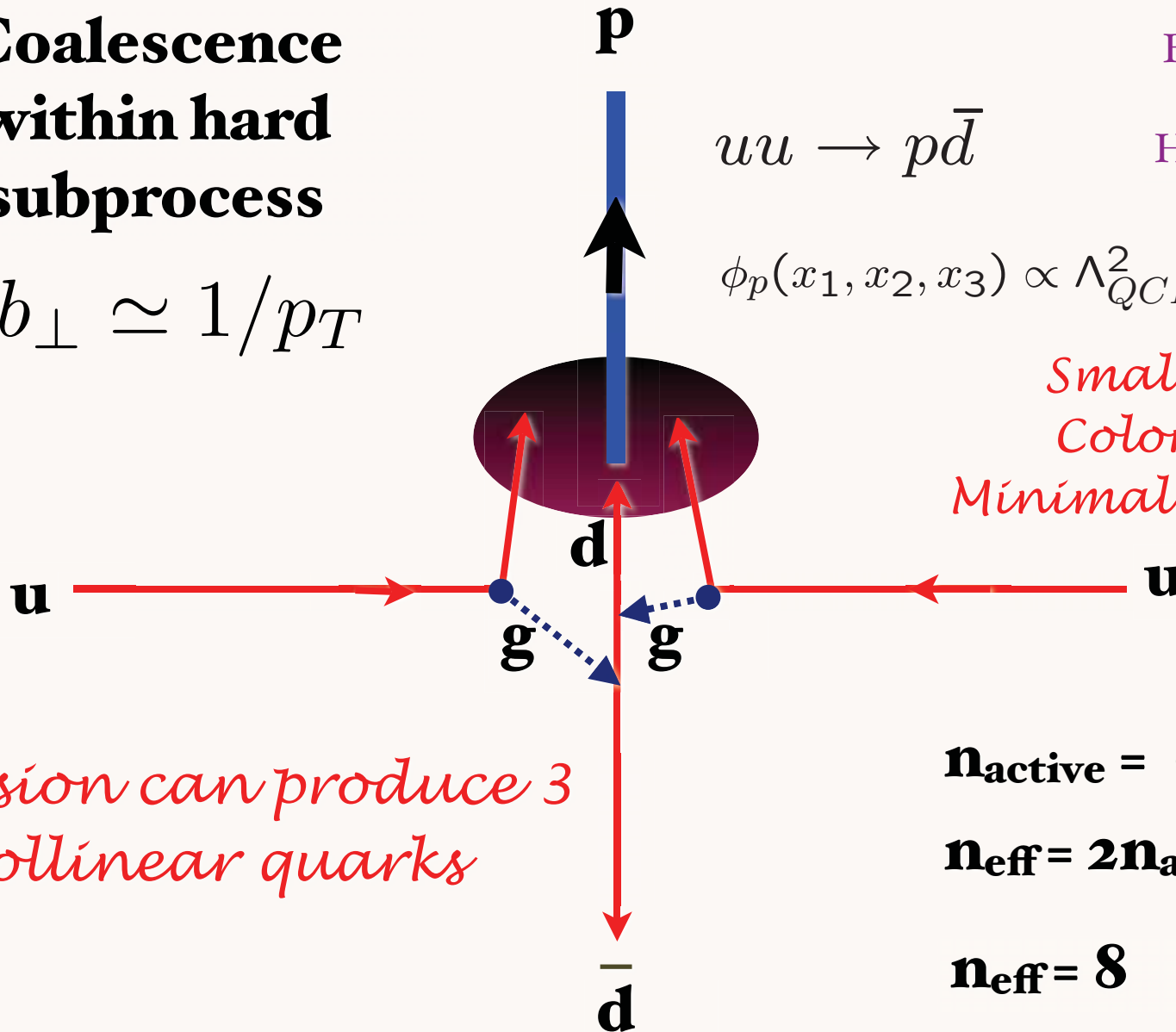
Hoyer, et al: Semi-Exclusive

Sickles, sjb

$$uu \rightarrow p\bar{d}$$

$$\phi_p(x_1, x_2, x_3) \propto \Lambda_{QCD}^2$$

*Small color-singlet  
Color Transparent  
Minimal same-side energy*



*Collision can produce 3 collinear quarks*

$$n_{\text{active}} = 6$$

$$n_{\text{eff}} = 2n_{\text{active}} - 4$$

$$n_{\text{eff}} = 8$$

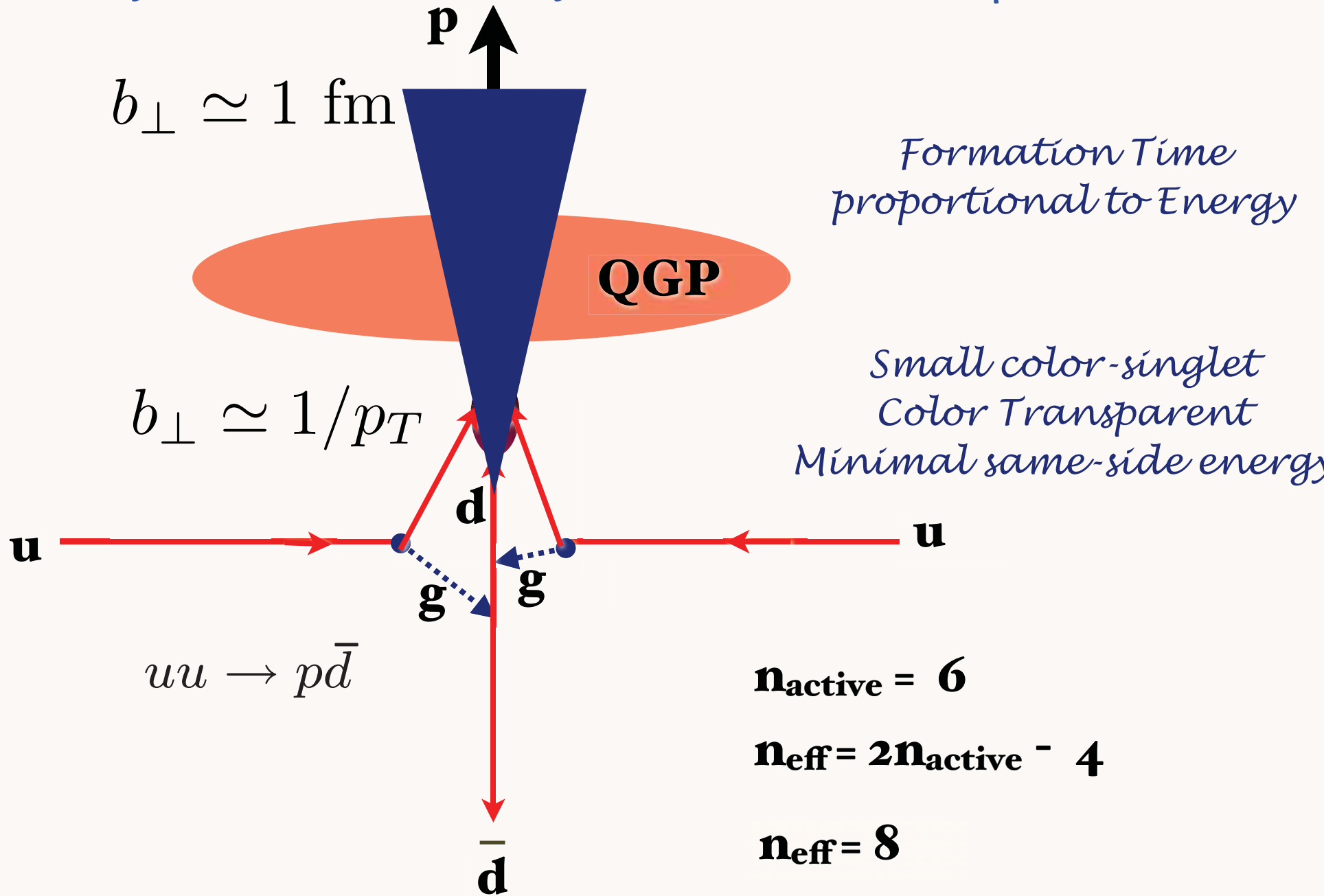
Manchester  
August 5, 2008

Light-Front Holography

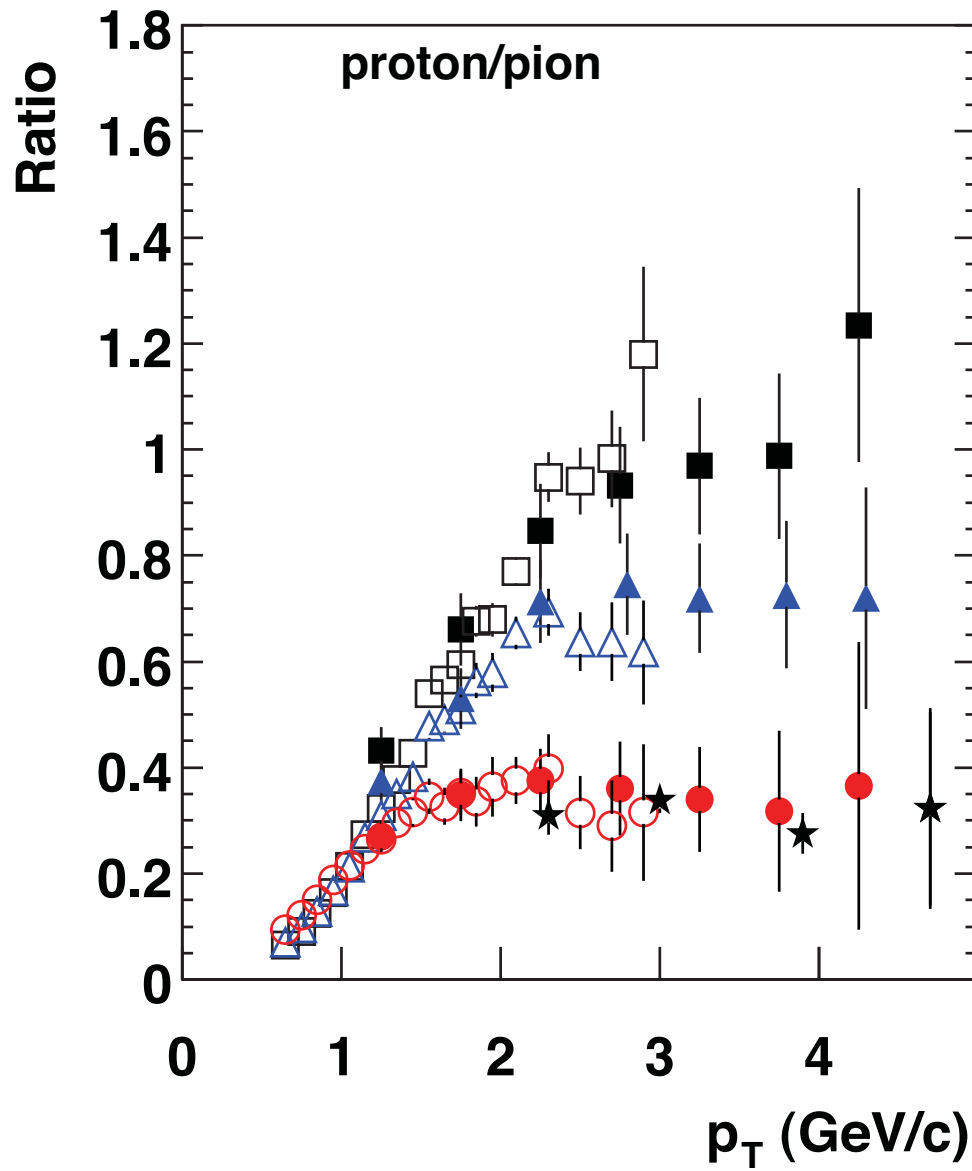
59

Stan Brodsky  
SLAC & IPPP

*Baryon made directly within hard subprocess*



*Particle ratio changes with centrality!*

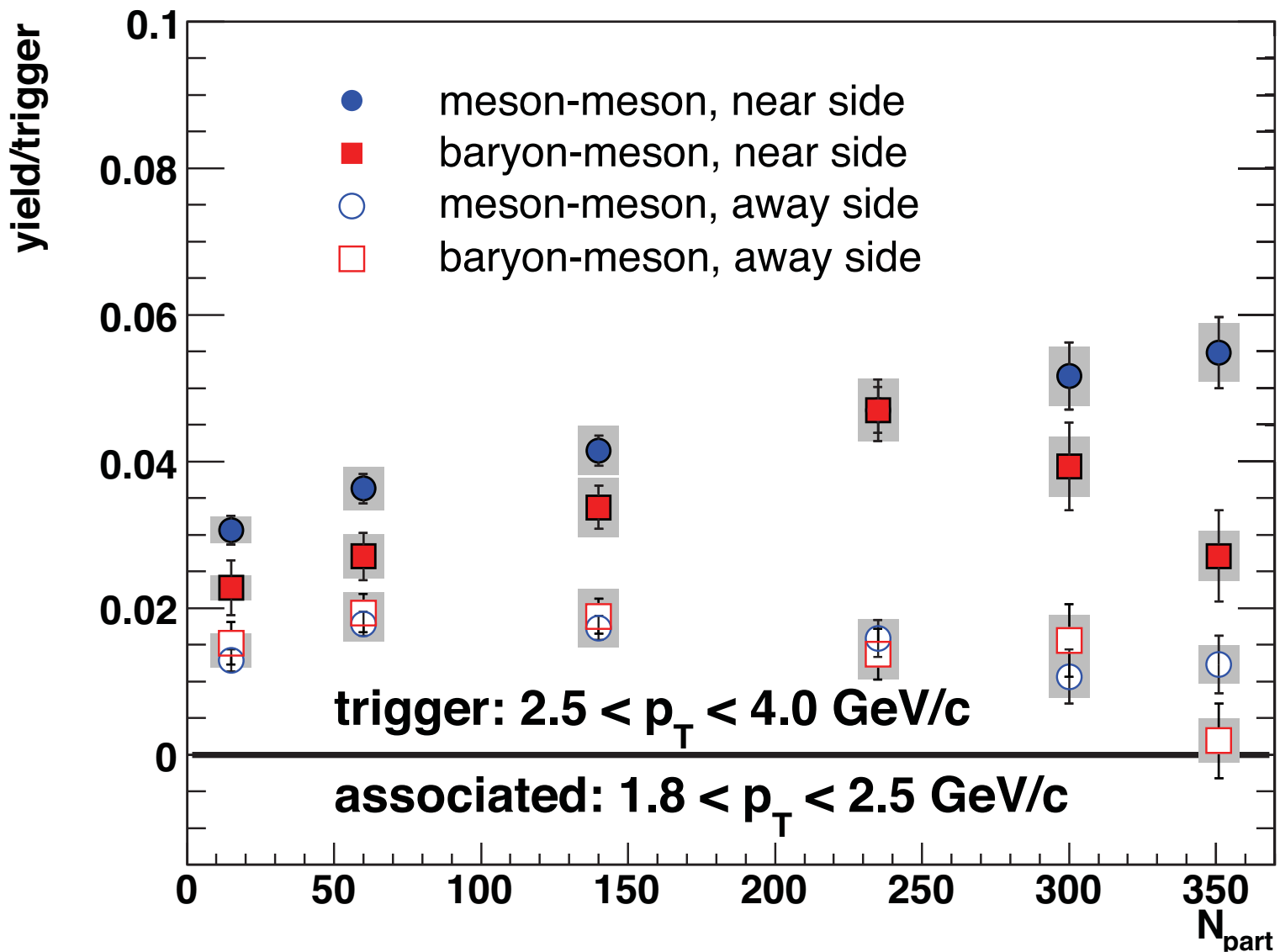


*Protons less absorbed  
in nuclear collisions than pions  
because of dominant  
color transparent higher twist process*

← **Central**

- ■ Au+Au 0-10%
- △ ▲ Au+Au 20-30%
- ● Au+Au 60-92%
- ★ p+p,  $\sqrt{s} = 53$  GeV, ISR
- e<sup>+</sup>e<sup>-</sup>, gluon jets, DELPHI
- ..... e<sup>+</sup>e<sup>-</sup>, quark jets, DELPHI

← **Peripheral**

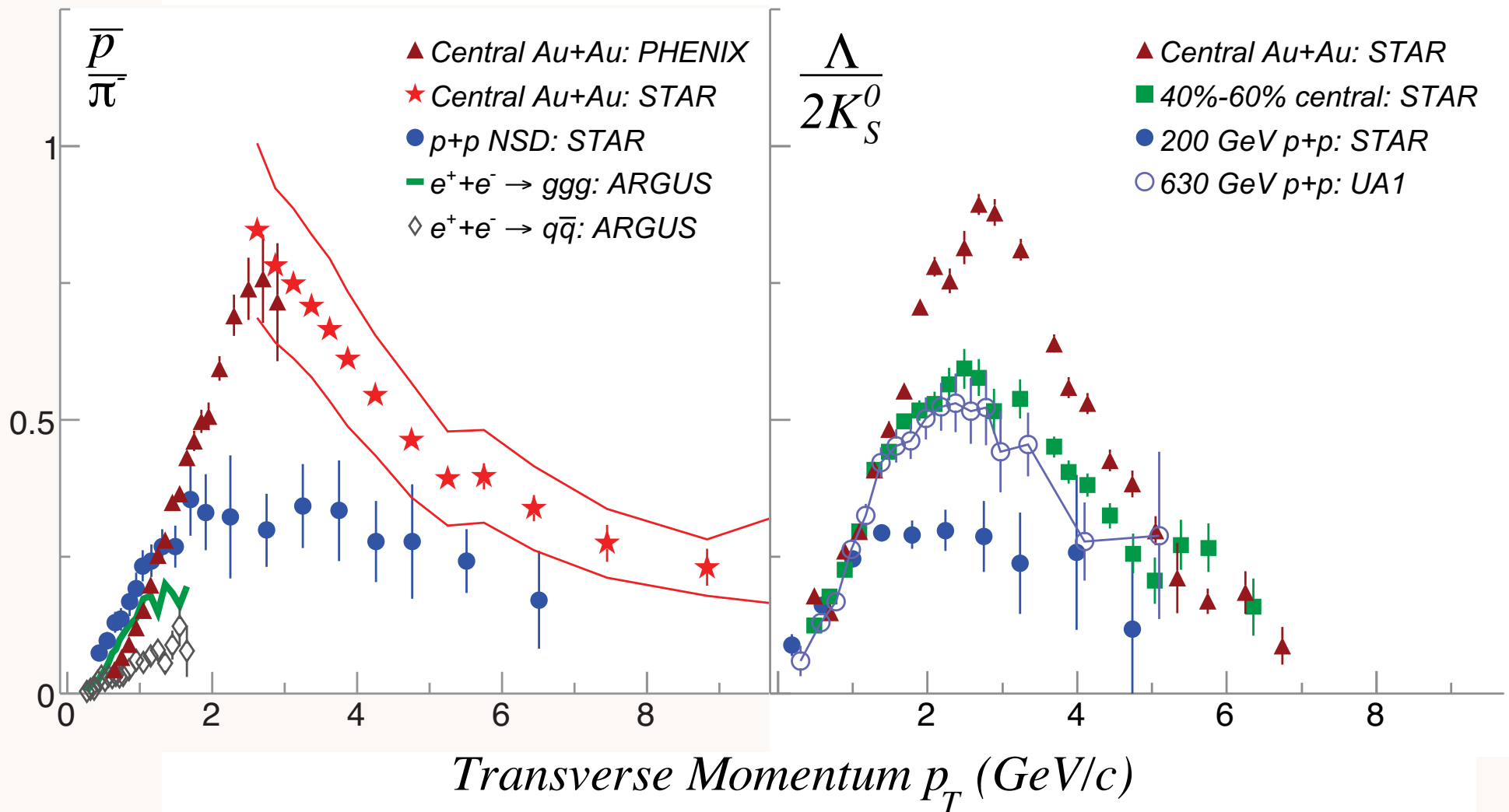


*proton trigger:  
# same-side particles  
decreases with centrality*



**Proton production more dominated by color-transparent direct high- $n_{eff}$  subprocesses**

Baryon to Meson Ratios



Manchester  
August 5, 2008

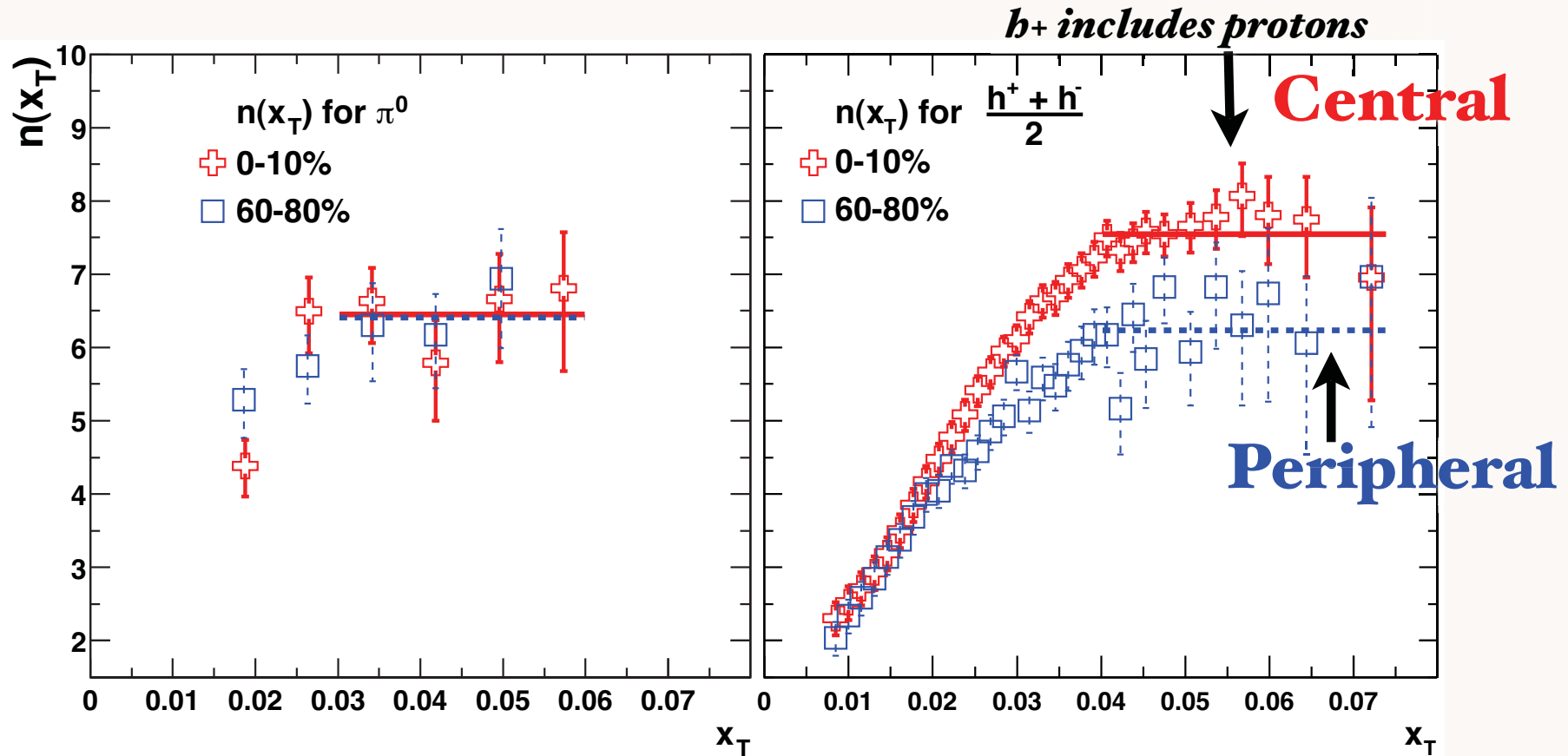
Light-Front Holography

63

Stan Brodsky  
SLAC & IPPP

Power-law exponent  $n(x_T)$  for  $\pi^0$  and  $h$  spectra in central and peripheral Au+Au collisions at  $\sqrt{s_{NN}} = 130$  and 200 GeV

S. S. Adler, *et al.*, PHENIX Collaboration, *Phys. Rev. C* **69**, 034910 (2004) [nucl-ex/0308006].



*Proton production dominated by color-transparent direct high  $n_{eff}$  subprocesses*

Manchester  
August 5, 2008

Light-Front Holography  
64

Stan Brodsky  
SLAC & IPPP

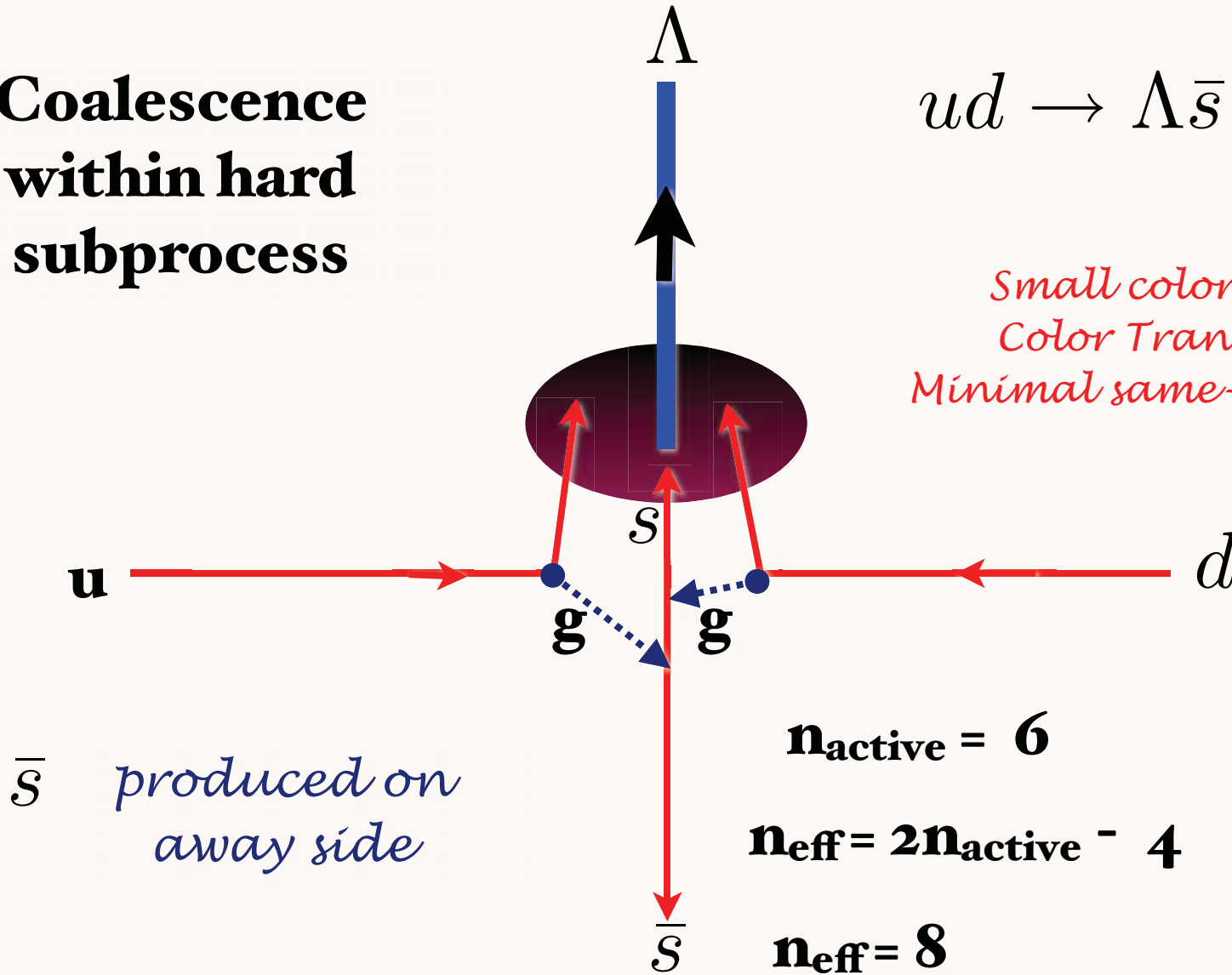


*Lambda can be made directly within hard subprocess*

**Coalescence  
within hard  
subprocess**

$$ud \rightarrow \Lambda \bar{s}$$

*Small color-singlet  
Color Transparent  
Minimal same-side energy*



$\bar{s}$  *produced on  
away side*

Sickles, sjb

$$n_{\text{active}} = 6$$

$$n_{\text{eff}} = 2n_{\text{active}} - 4$$

$$n_{\text{eff}} = 8$$

# *Baryon Anomaly:*

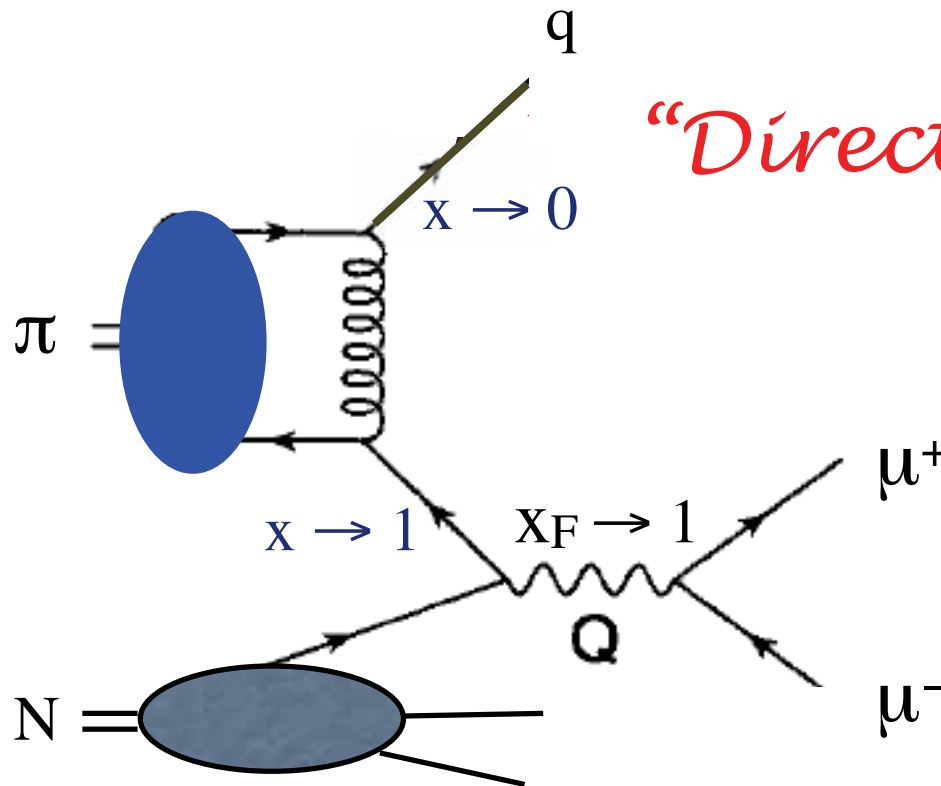
## *Evidence for Direct, Higher-Twist Subprocesses*

- Explains anomalous power behavior at fixed  $x_T$
- Protons more likely to come from direct higher-twist subprocess than pions
- Protons less absorbed than pions in central nuclear collisions because of color transparency
- Predicts increasing proton to pion ratio in central collisions
- Proton power  $n_{\text{eff}}$  increases with centrality since leading twist contribution absorbed
- Fewer same-side hadrons for proton trigger at high centrality
- Exclusive-inclusive connection at  $x_T = 1$

$$\pi N \rightarrow \mu^+ \mu^- X \text{ at high } x_F$$

In the limit where  $(1-x_F)Q^2$  is fixed as  $Q^2 \rightarrow \infty$

Entire pion wf  
contributes to  
hard process



*“Direct” Subprocess*

Virtual photon is  
longitudinally  
polarized

Berger, sjb  
Khoze, Brandenburg, Muller, sjb  
Hoyer Vanttinen

Manchester  
August 5, 2008

**Light-Front Holography**

67

**Stan Brodsky  
SLAC & IPPP**

$$\pi^- N \rightarrow \mu^+ \mu^- X \text{ at } 80 \text{ GeV}/c$$

$$\frac{d\sigma}{d\Omega} \propto 1 + \lambda \cos^2\theta + \rho \sin 2\theta \cos\phi + \omega \sin^2\theta \cos 2\phi.$$

$$\frac{d^2\sigma}{dx_\pi d\cos\theta} \propto x_\pi \left[ (1 - x_\pi)^2 (1 + \cos^2\theta) + \frac{4}{9} \frac{\langle k_T^2 \rangle}{M^2} \sin^2\theta \right]$$

$$\langle k_T^2 \rangle = 0.62 \pm 0.16 \text{ GeV}^2/c^2$$

*Dramatic change in  
angular distribution at  
large  $x_F$*

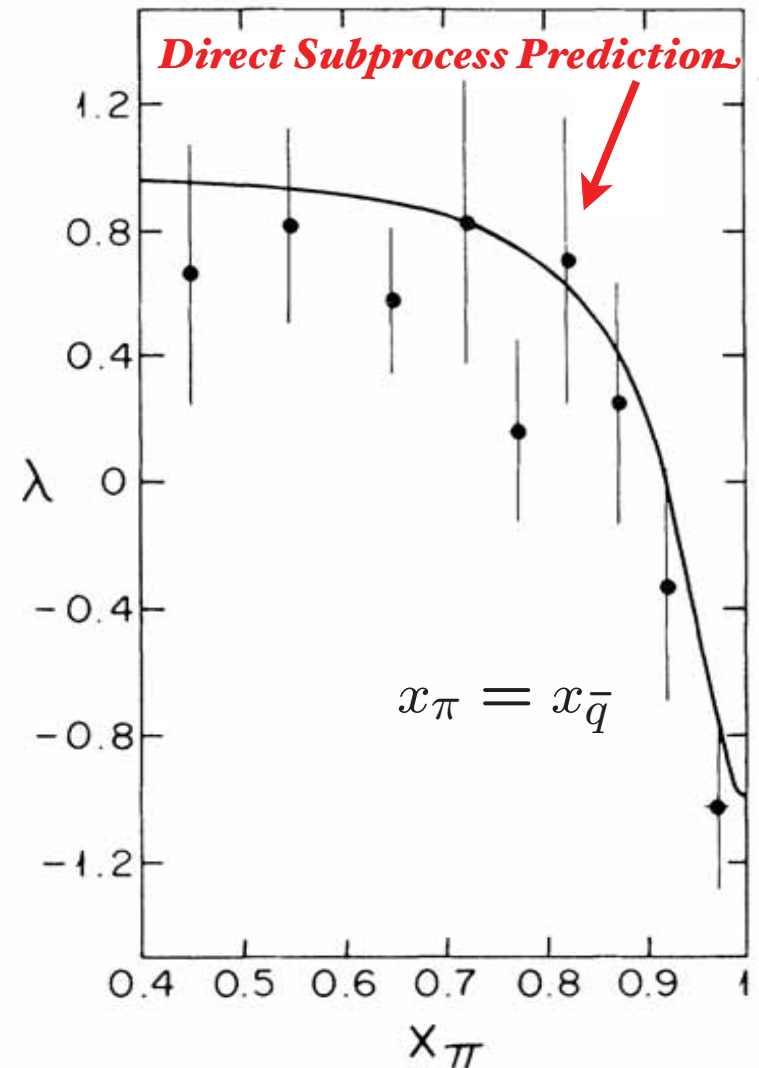
**Example of a higher-twist  
direct subprocess**

Manchester  
August 5, 2008

**Light-Front Holography**

68

**Stan Brodsky  
SLAC & IPPP**



Chicago-Princeton  
Collaboration

Phys.Rev.Lett.55:2649,1985

## *Role of higher twist in hard inclusive reactions*

- **Hadron can be produced directly in hard subprocess as in exclusive reactions**
- **Sum over reactions**
- **Trigger bias: No wasted same-side energy**
- **Exclusive - inclusive connection important at high  $x_T$**
- **Explanation of  $n_{\text{eff}} = 8, 12$  observed at ISR, Fermilab: Chicago-Princeton experiments**
- **Direct Hadron Production -- color transparency and reduced same side absorption**
- **Critical to plot data at fixed  $x_T$**
- **Interpretation of RHIC data is modified if higher twist subprocesses play an important role**

# QCD Lagrangian

The diagram shows the QCD Lagrangian  $L_{\text{QCD}}$  enclosed in a red box. Labels with arrows point to various parts of the equation:

- gluon dynamics** points to the first term:  $-\frac{1}{4g^2} \text{Tr}(G^{\mu\nu} G_{\mu\nu})$ .
- quark kinetic energy + quark-gluon dynamics** points to the second term:  $\sum_{f=1}^{nf} i \bar{\Psi}_f D_\mu \gamma^\mu \Psi_f$ .
- mass term** points to the third term:  $\sum_{f=1}^{nf} m_f \bar{\Psi}_f \Psi_f$ .
- QCD color charge** points to the  $g^2$  in the denominator of the first term.
- field strength tensor** points to  $G^{\mu\nu}$  in the first term.
- covariant derivative** points to  $D_\mu$  in the second term.
- quark field** points to  $\Psi_f$  in the second term.

*Yang-Mills Gauge Principle:  
Invariance under Color  
Rotation and Phase Change at  
Every Point of Space and Time*

Dimensionless Coupling  
Renormalizable  
**Asymptotic Freedom**  
**Color Confinement**

$$L_{\text{QCD}} \rightarrow H_{\text{QCD}}^{LF} \rightarrow \psi_{n/H}^{LF}(x_i, \vec{k}_{\perp i}, \lambda_i)$$

# Light-Front QCD

## Heisenberg Matrix Formulation

Physical gauge:  $A^+ = 0$

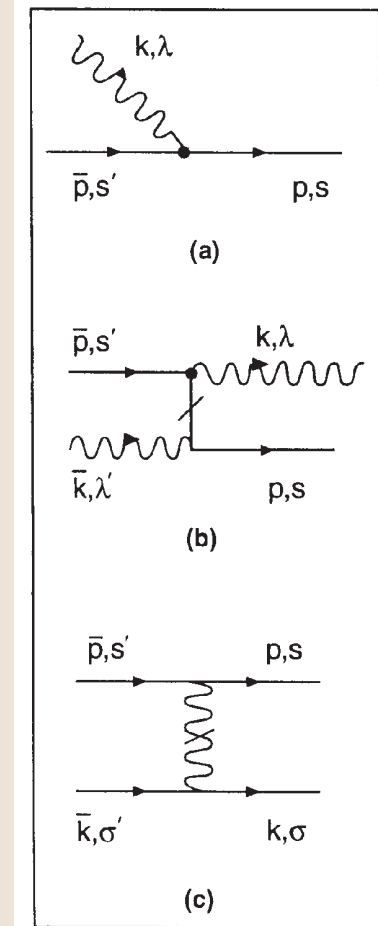
$$L^{QCD} \rightarrow H_{LF}^{QCD}$$

$$H_{LF}^{QCD} = \sum_i \left[ \frac{m^2 + k_{\perp}^2}{x} \right]_i + H_{LF}^{int}$$

$H_{LF}^{int}$ : Matrix in Fock Space

$$H_{LF}^{QCD} |\Psi_h\rangle = \mathcal{M}_h^2 |\Psi_h\rangle$$

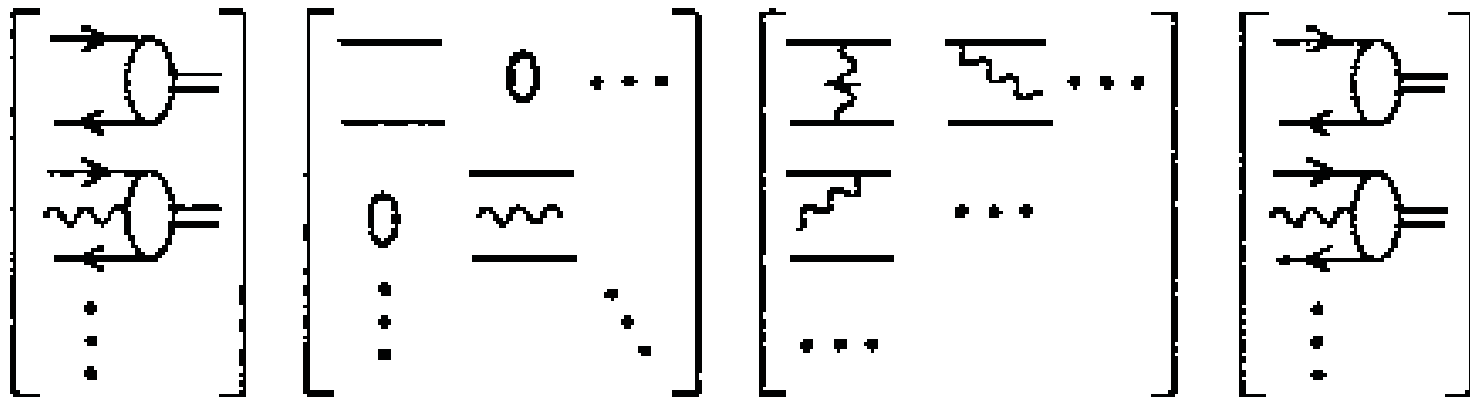
Eigenvalues and Eigensolutions give Hadron Spectrum and Light-Front wavefunctions



DLCQ: Periodic BC in  $x^-$ . Discrete  $k^+$ ; frame-independent truncation

# LIGHT-FRONT SCHRÖDINGER EQUATION

$$\left( M_\pi^2 - \sum_i \frac{\vec{k}_{\perp i}^2 + m_i^2}{x_i} \right) \begin{bmatrix} \psi_{q\bar{q}/\pi} \\ \psi_{q\bar{q}g/\pi} \\ \vdots \end{bmatrix} = \begin{bmatrix} \langle q\bar{q} | V | q\bar{q} \rangle & \langle q\bar{q} | V | q\bar{q}g \rangle & \cdots \\ \langle q\bar{q}g | V | q\bar{q} \rangle & \langle q\bar{q}g | V | q\bar{q}g \rangle & \cdots \\ \vdots & \vdots & \ddots \end{bmatrix} \begin{bmatrix} \psi_{q\bar{q}/\pi} \\ \psi_{q\bar{q}g/\pi} \\ \vdots \end{bmatrix}$$



$$A^+ = 0$$

G.P. Lepage, sjb

Manchester  
August 5, 2008

Light-Front Holography

72

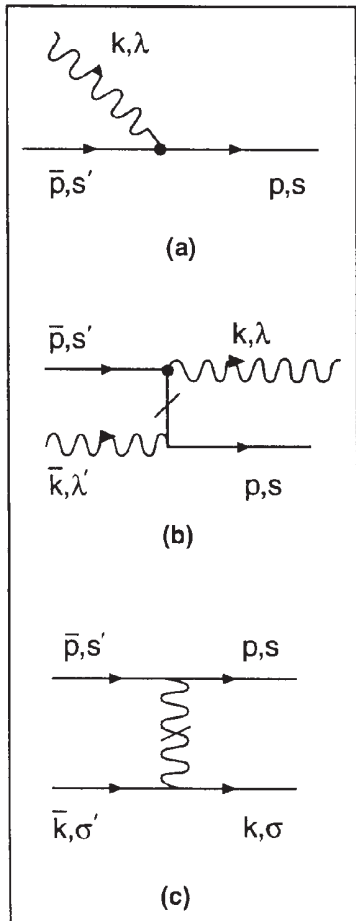
Stan Brodsky  
SLAC & IPPP



## Heisenberg Matrix Formulation

$$H_{LF}^{QCD} |\Psi_h\rangle = \mathcal{M}_h^2 |\Psi_h\rangle$$

## Discretized Light-Cone Quantization



n	Sector	1 q $\bar{q}$	2 gg	3 q $\bar{q}$ g	4 q $\bar{q}$ q $\bar{q}$	5 ggg	6 q $\bar{q}$ gg	7 q $\bar{q}$ q $\bar{q}$ g	8 q $\bar{q}$ q $\bar{q}$ q $\bar{q}$	9 gggg	10 q $\bar{q}$ ggg	11 q $\bar{q}$ q $\bar{q}$ gg	12 q $\bar{q}$ q $\bar{q}$ q $\bar{q}$ g	13 q $\bar{q}$ q $\bar{q}$ q $\bar{q}$ q $\bar{q}$
1	q $\bar{q}$					.		.	.	.	.	.	.	.
2	gg				.			.	.		.	.	.	.
3	q $\bar{q}$ g								.	.		.	.	.
4	q $\bar{q}$ q $\bar{q}$		.			.				.	.		.	.
5	ggg	.			.			.	.			.	.	.
6	q $\bar{q}$ gg								.				.	.
7	q $\bar{q}$ q $\bar{q}$ g	.	.			.				.				.
8	q $\bar{q}$ q $\bar{q}$ q $\bar{q}$	.	.	.		.	.			.	.			
9	gggg	.		.	.			.	.			.	.	.
10	q $\bar{q}$ ggg	.	.		.				.				.	.
11	q $\bar{q}$ q $\bar{q}$ gg	.	.	.		.				.				.
12	q $\bar{q}$ q $\bar{q}$ q $\bar{q}$ g	.	.	.	.	.	.			.	.			
13	q $\bar{q}$ q $\bar{q}$ q $\bar{q}$ q $\bar{q}$	.	.	.	.	.	.	.		.	.	.		

Eigenvalues and Eigensolutions give Hadron Spectrum and Light-Front wavefunctions

*DLCQ: Frame-independent, No fermion doubling; Minkowski Space*

DLCQ: Periodic BC in  $x^-$ . Discrete  $k^+$ ; frame-independent truncation

# Goal:

- **Use AdS/CFT to provide an approximate, covariant, and analytic model of hadron structure with confinement at large distances, conformal behavior at short distances**
- **Analogous to the Schrodinger Theory for Atomic Physics**
- *AdS/QCD Light-Front Holography*
- *Hadronic Spectra and Light-Front Wavefunctions*

*Conformal Theories are invariant under the Poincare and conformal transformations with*

$$M^{\mu\nu}, P^\mu, D, K^\mu,$$


*the generators of  $SO(4,2)$*

**$SO(4,2)$  has a mathematical representation on  $AdS_5$**

## Scale Transformations

- Isomorphism of  $SO(4, 2)$  of conformal QCD with the group of isometries of AdS space

$$ds^2 = \frac{R^2}{z^2} (\eta_{\mu\nu} dx^\mu dx^\nu - dz^2),$$

*invariant measure* 

$x^\mu \rightarrow \lambda x^\mu, z \rightarrow \lambda z$ , maps scale transformations into the holographic coordinate  $z$ .

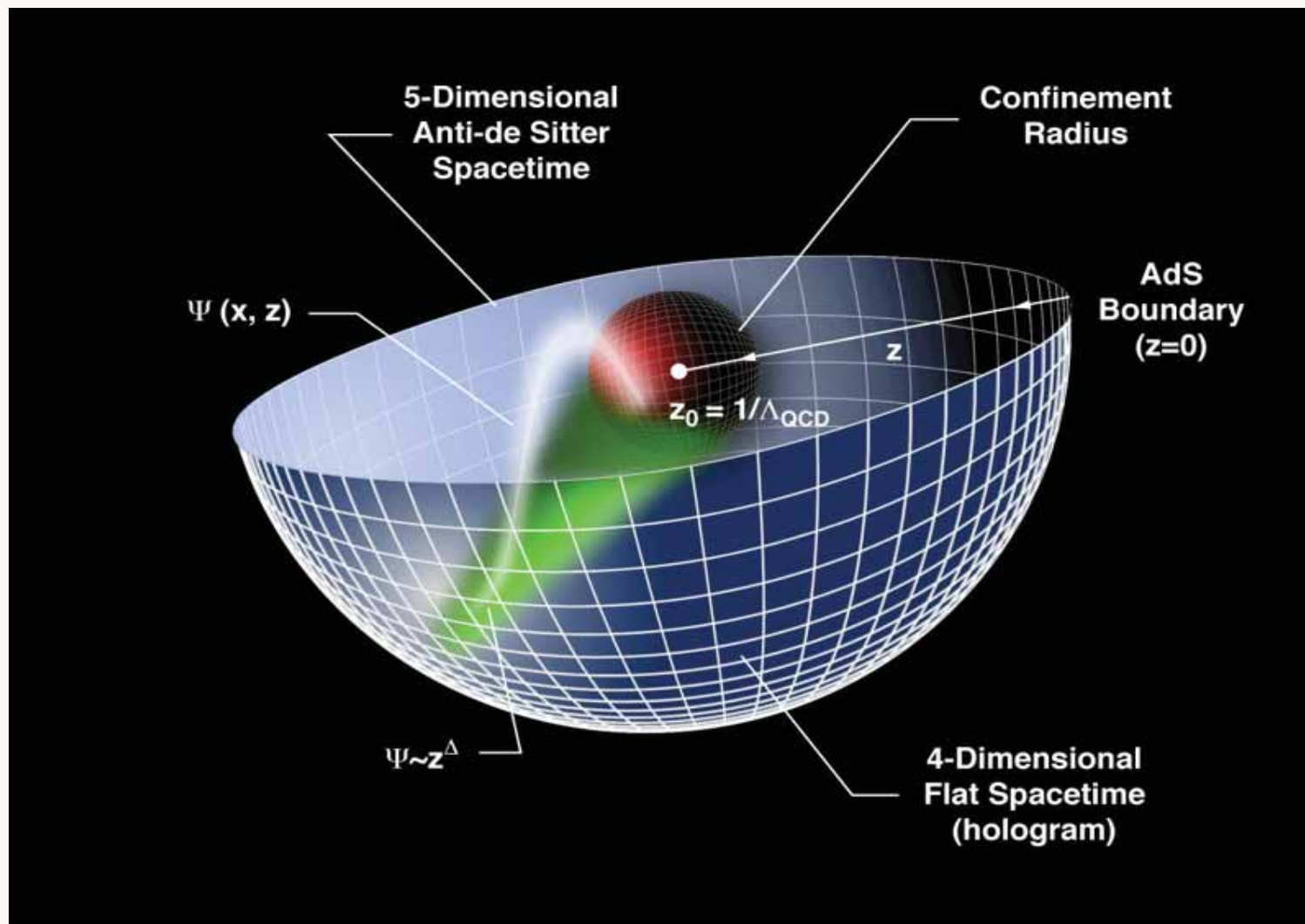
- AdS mode in  $z$  is the extension of the hadron wf into the fifth dimension.
- Different values of  $z$  correspond to different scales at which the hadron is examined.

$$x^2 \rightarrow \lambda^2 x^2, \quad z \rightarrow \lambda z.$$

$x^2 = x_\mu x^\mu$ : invariant separation between quarks

- The AdS boundary at  $z \rightarrow 0$  correspond to the  $Q \rightarrow \infty$ , UV zero separation limit.

# Applications of AdS/CFT to QCD



*Changes in physical length scale mapped to evolution in the 5th dimension  $z$*

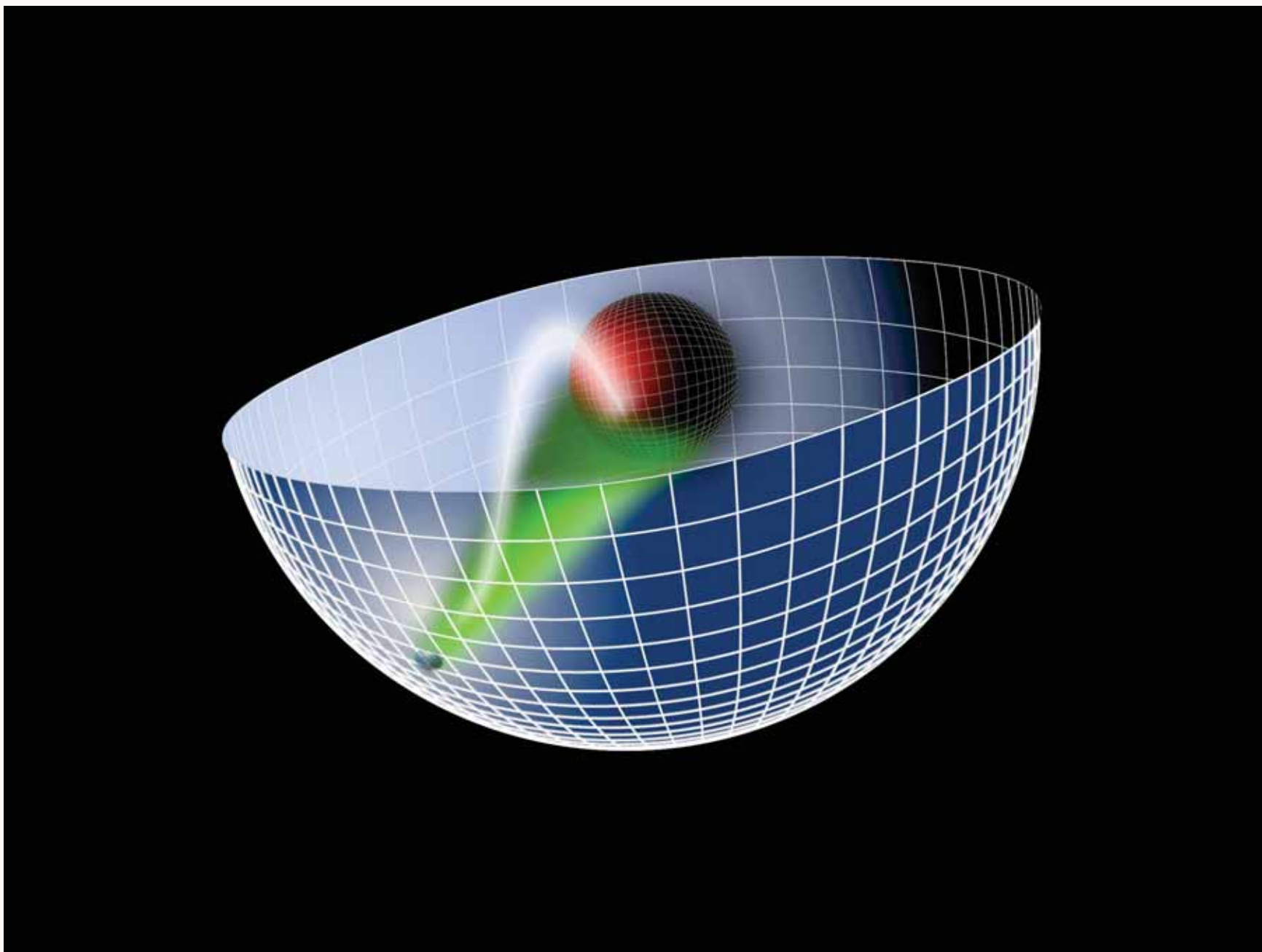
**in collaboration with Guy de Teramond**

**Manchester**  
**August 5, 2008**

**Light-Front Holography**

77

**Stan Brodsky**  
**SLAC & IPPP**



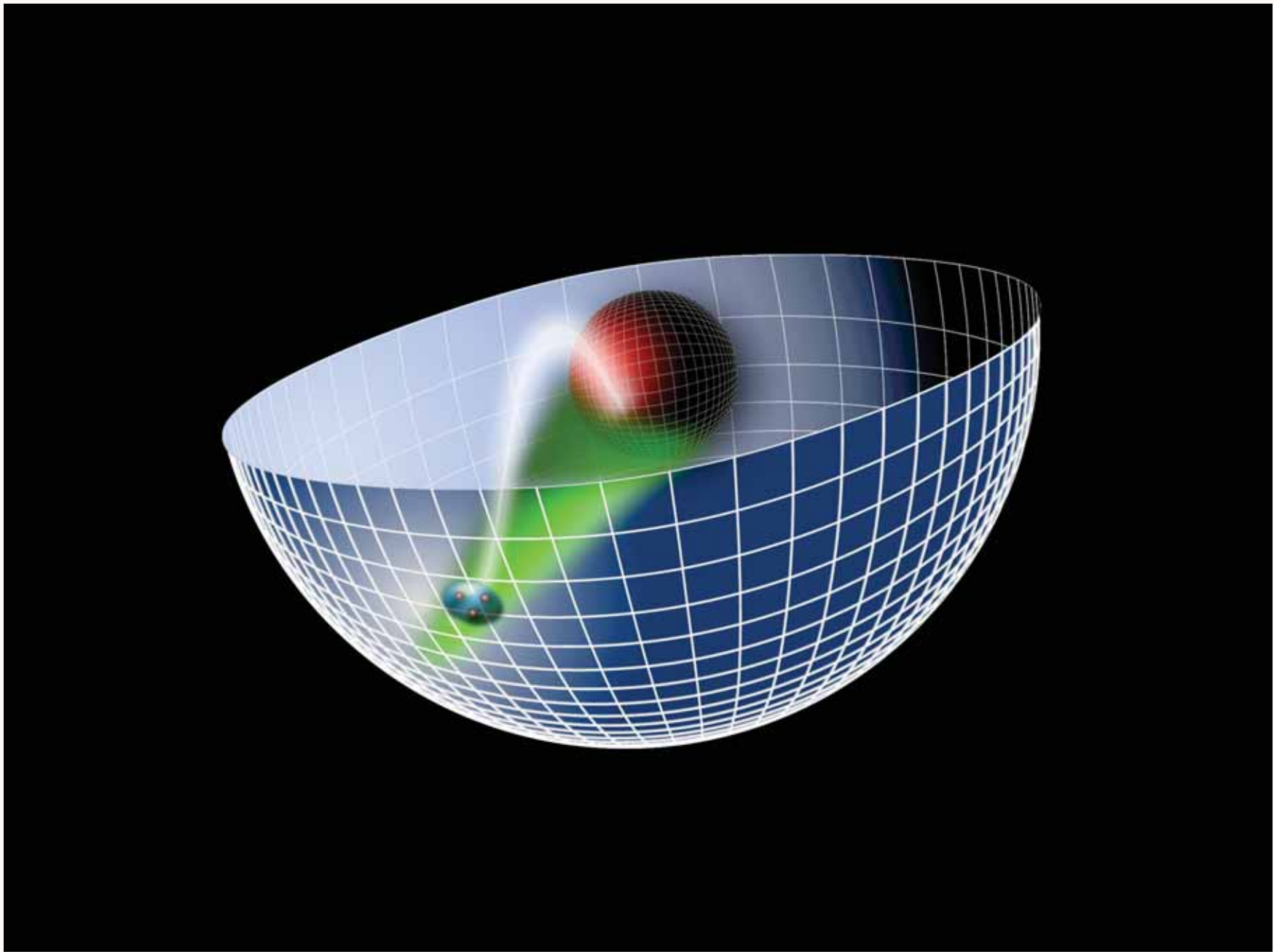
**Manchester**  
**August 5, 2008**

## **Light-Front Holography**

**78**

**Stan Brodsky**  
**SLAC & IPPP**



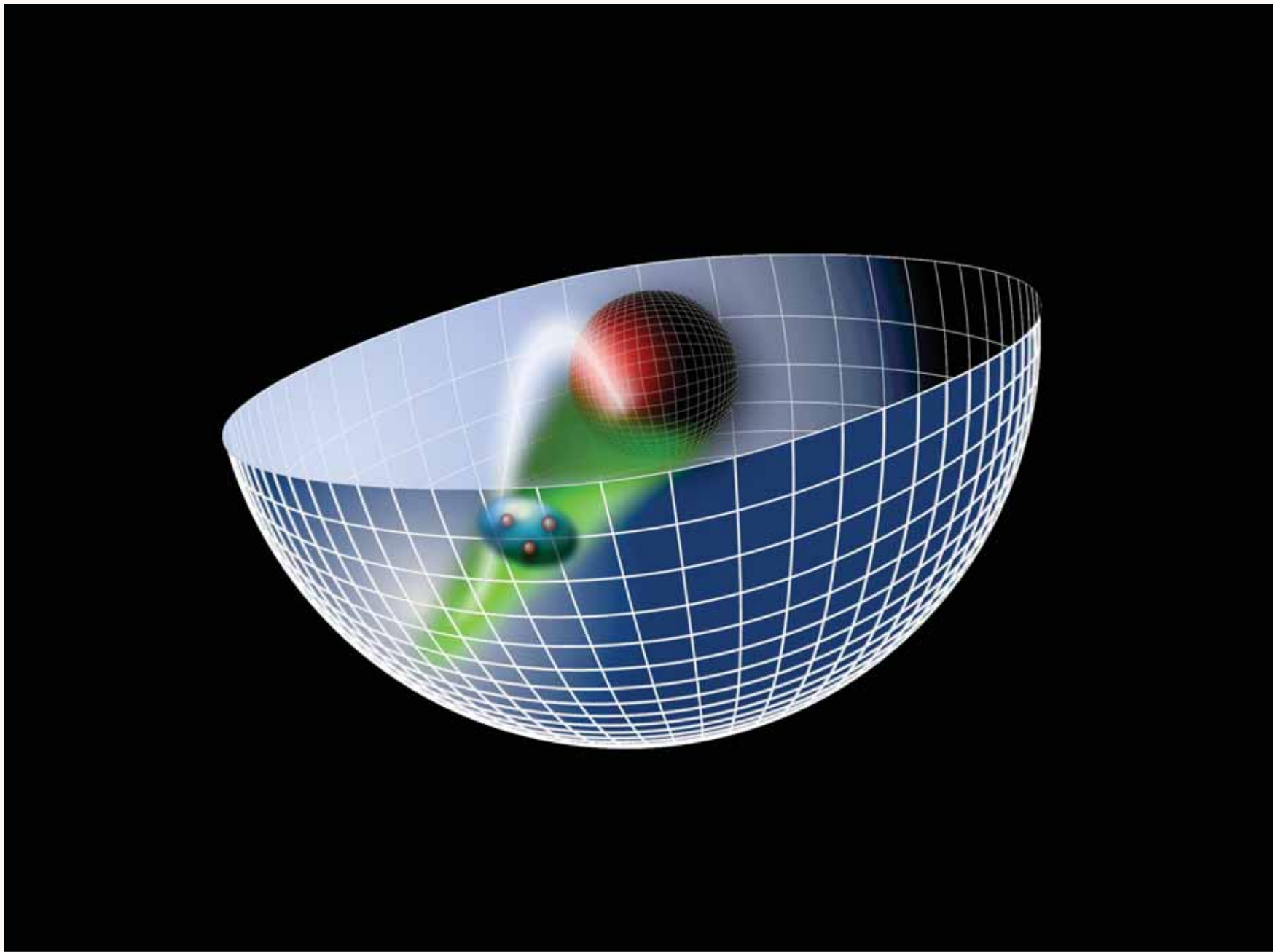


**Manchester**  
**August 5, 2008**

## **Light-Front Holography**

**79**

**Stan Brodsky**  
**SLAC & IPPP**



**Manchester**  
**August 5, 2008**

**Light-Front Holography**  
**80**

**Stan Brodsky**  
**SLAC & IPPP**