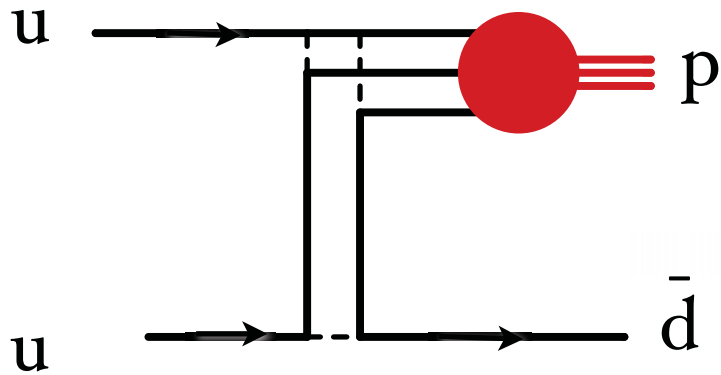


# Direct Proton Production



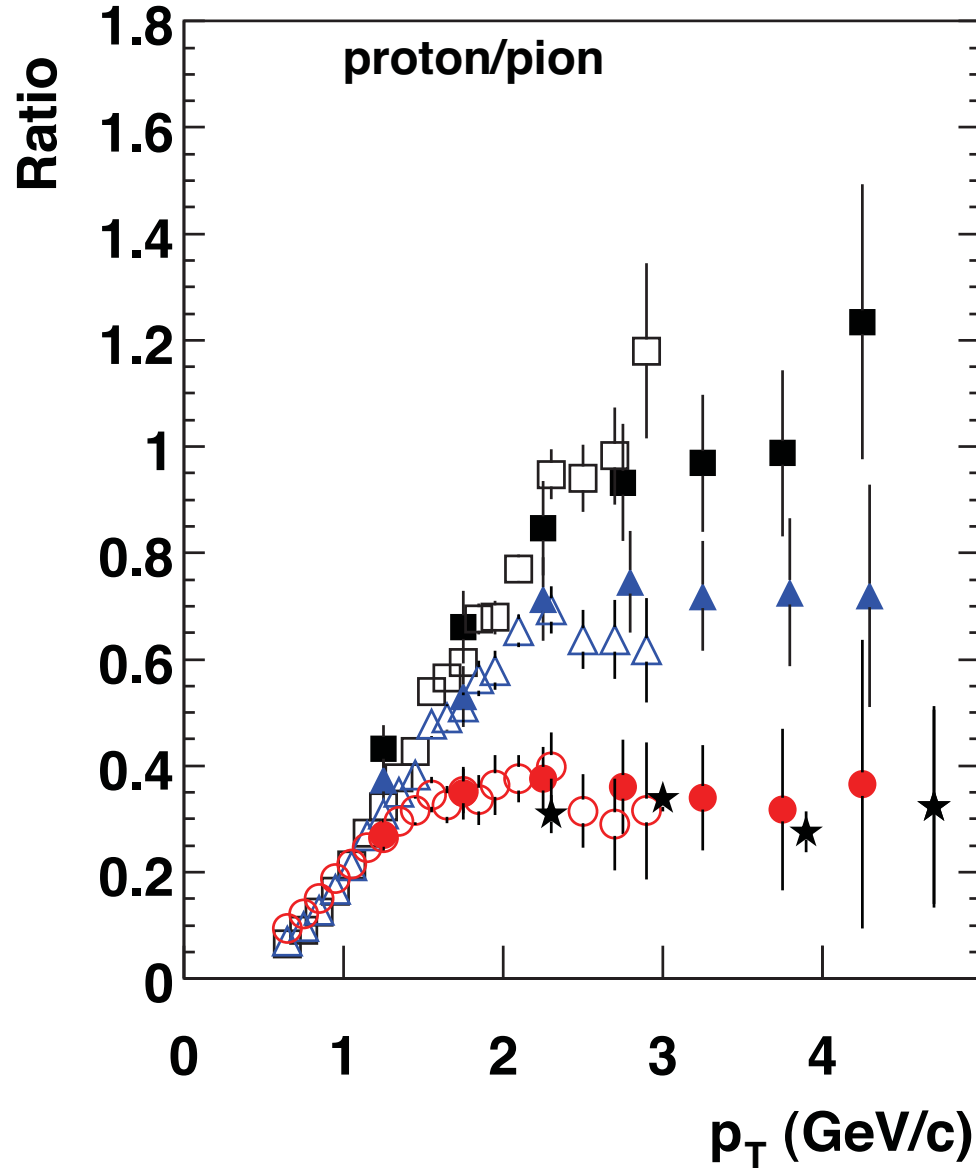
$$n_{\text{active}} = 6$$

$$E \frac{d\sigma}{d^3p} (p p \rightarrow p X) \sim \frac{F(x_{\perp}, \vartheta^{\text{cm}})}{p_{\perp}^8}$$

**Explains “Baryon anomaly” at RHIC!**

Sickles, sjb

*Particle ratio changes with centrality!*



*Protons less absorbed  
in nuclear collisions than pions  
because of dominant  
color transparent higher twist process*

← **Central**

- ■ Au+Au 0-10%
- △ ▲ Au+Au 20-30%
- ● Au+Au 60-92%
- ★ p+p,  $\sqrt{s} = 53$  GeV, ISR
- e<sup>+</sup>e<sup>-</sup>, gluon jets, DELPHI
- ..... e<sup>+</sup>e<sup>-</sup>, quark jets, DELPHI

← **Peripheral**

*Tannenbaum:  
Baryon Anomaly:*

*Baryon can be made directly within hard subprocess!*

**Coalescence  
within hard  
subprocess**

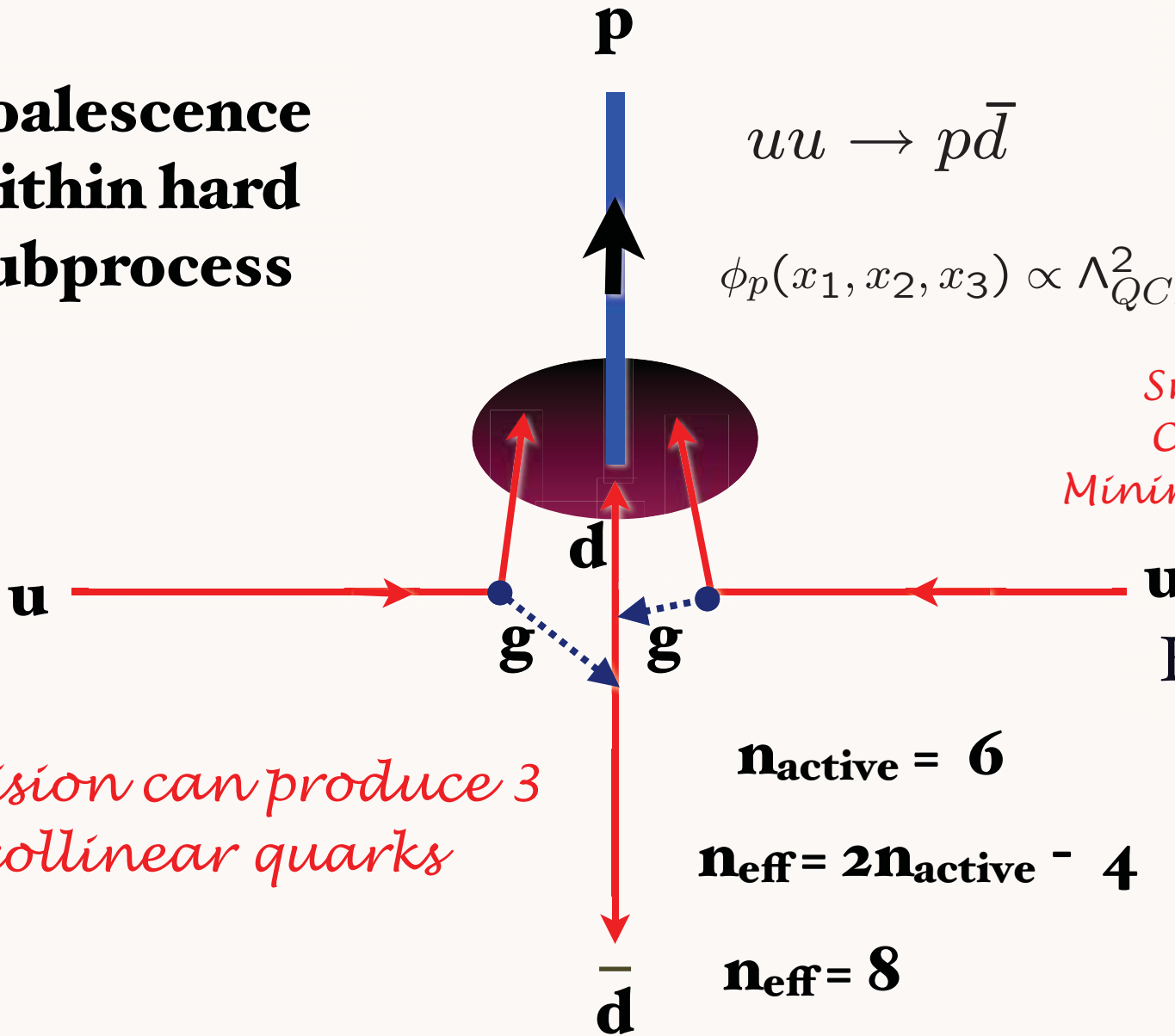
Bjorken  
Blankenbecler, Gunion, sjb  
Berger, sjb  
Hoyer, et al: Semi-Exclusive

$$uu \rightarrow p\bar{d}$$

$$\phi_p(x_1, x_2, x_3) \propto \Lambda_{QCD}^2$$

**Sickles; sjb**

*Small color-singlet  
Color Transparent  
Minimal same-side energy*



Baryon anomaly

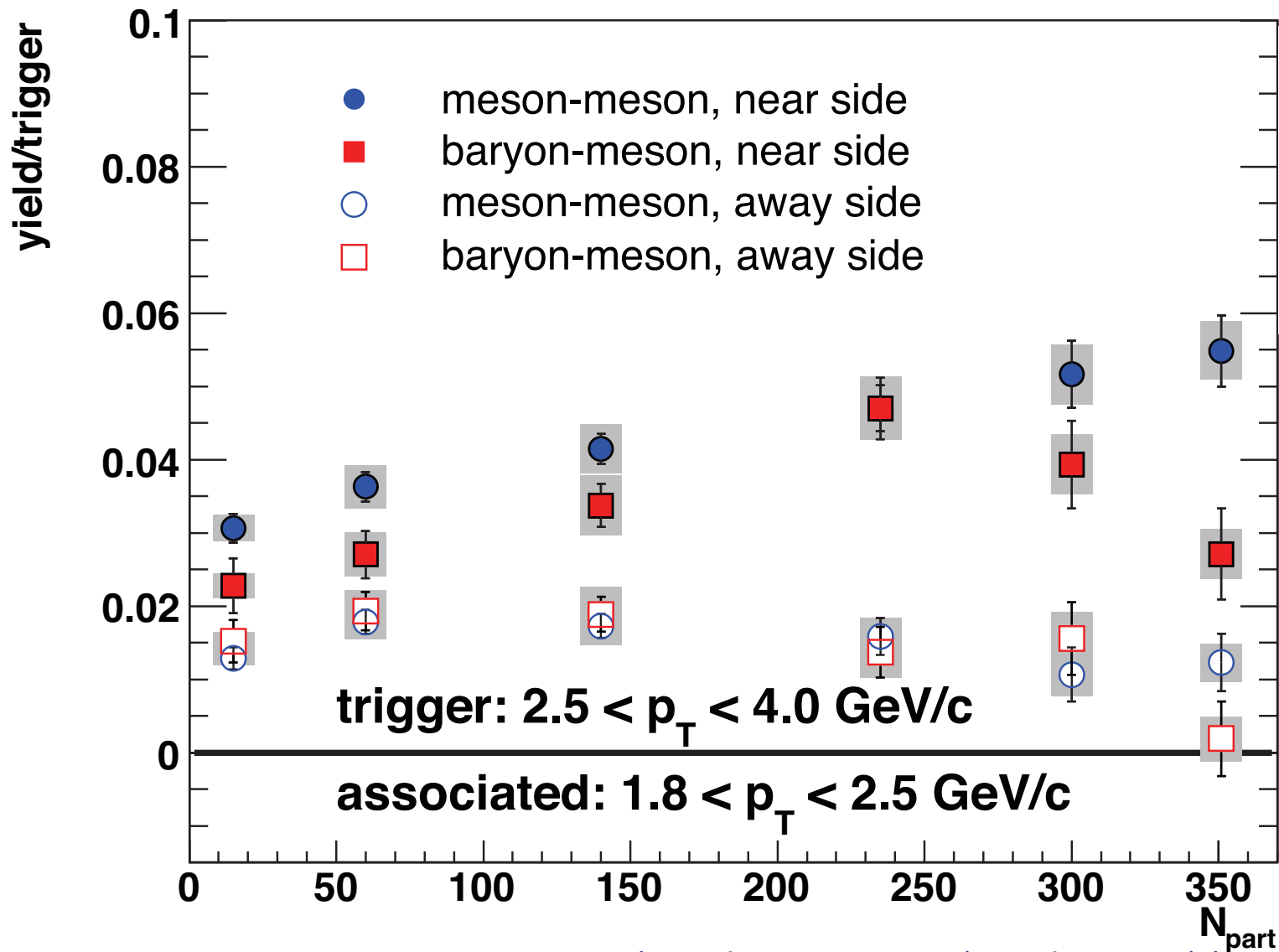
$$qq \rightarrow B\bar{q}$$

*Collision can produce 3  
collinear quarks*

$$\mathbf{n}_{\text{active}} = 6$$

$$\mathbf{n}_{\text{eff}} = 2\mathbf{n}_{\text{active}} - 4$$

$$\mathbf{n}_{\text{eff}} = 8$$



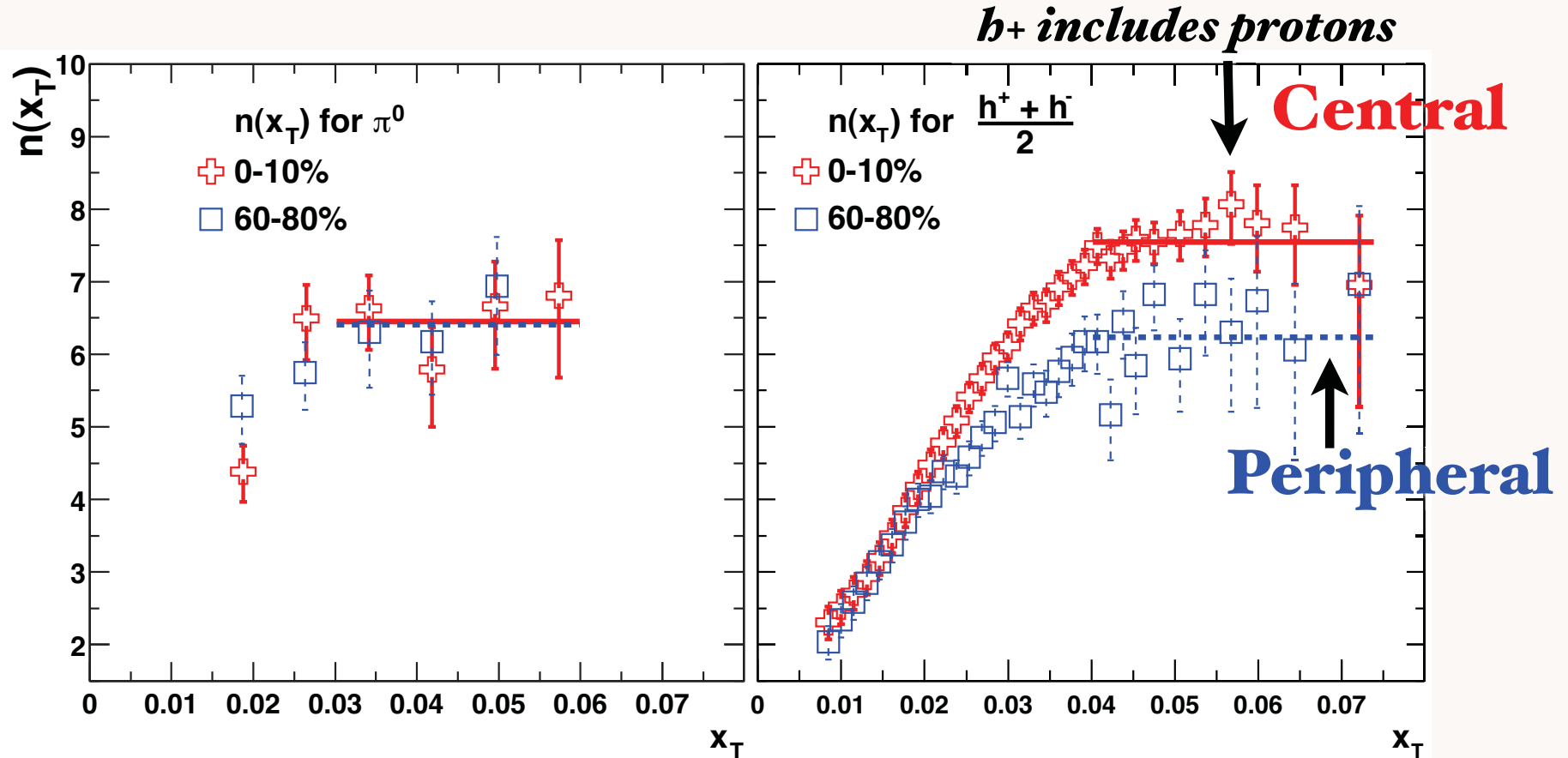
proton trigger:  
# same-side  
particles  
*decreases* with  
centrality



**Proton production more dominated by  
color-transparent direct high- $n_{eff}$  subprocesses**

Power-law exponent  $n(x_T)$  for  $\pi^0$  and  $h$  spectra in central and peripheral Au+Au collisions at  $\sqrt{s_{NN}} = 130$  and 200 GeV

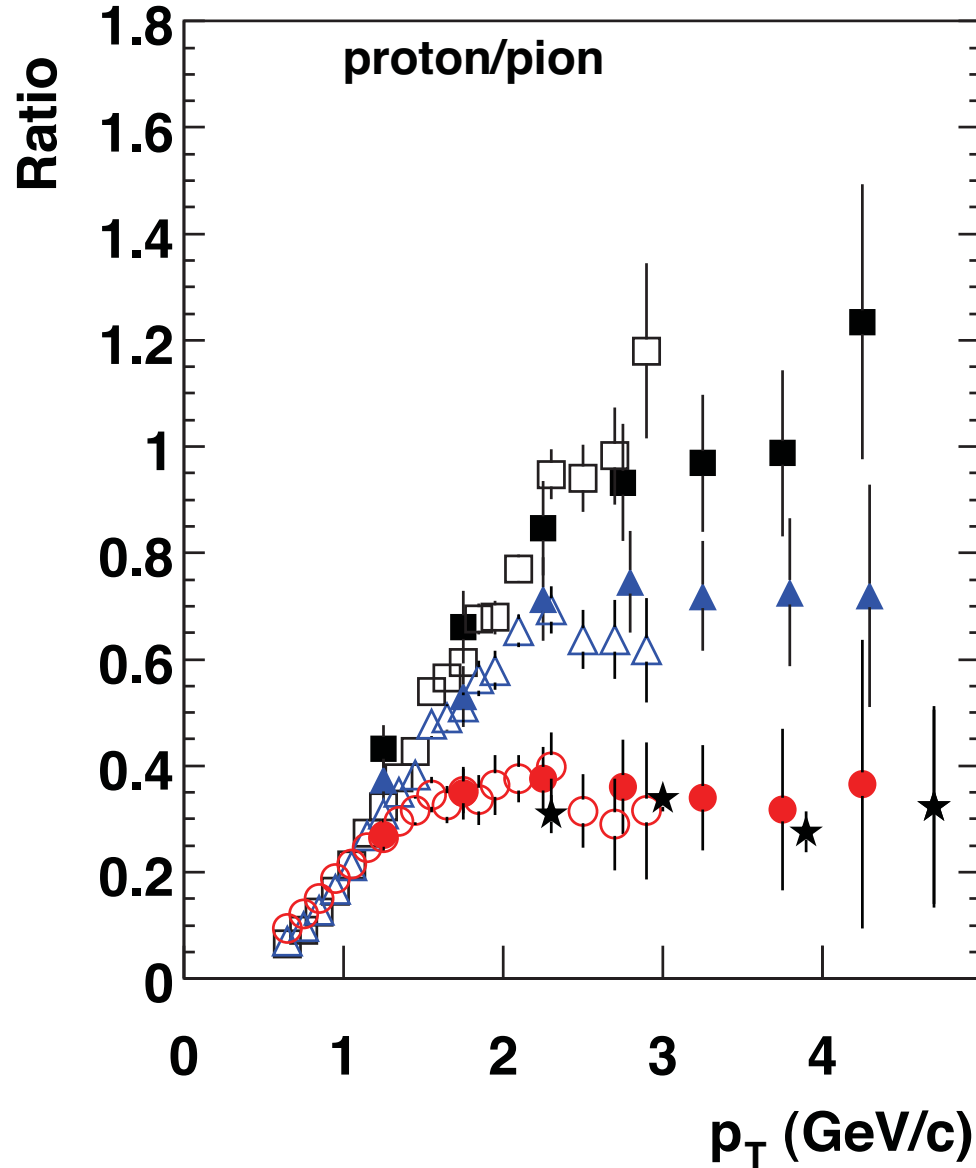
S. S. Adler, *et al.*, PHENIX Collaboration, *Phys. Rev. C* **69**, 034910 (2004) [nucl-ex/0308006].



*Proton power changes with centrality !*

*Proton production dominated by color-transparent direct high  $n_{eff}$  subprocesses*

*Particle ratio changes with centrality!*



*Protons less absorbed  
in nuclear collisions than pions  
because of dominant  
color transparent higher twist process*

← **Central**

- ■ Au+Au 0-10%
- △ ▲ Au+Au 20-30%
- ● Au+Au 60-92%
- ★ p+p,  $\sqrt{s} = 53$  GeV, ISR
- e<sup>+</sup>e<sup>-</sup>, gluon jets, DELPHI
- ..... e<sup>+</sup>e<sup>-</sup>, quark jets, DELPHI

← **Peripheral**

*Tannenbaum:  
Baryon Anomaly:*

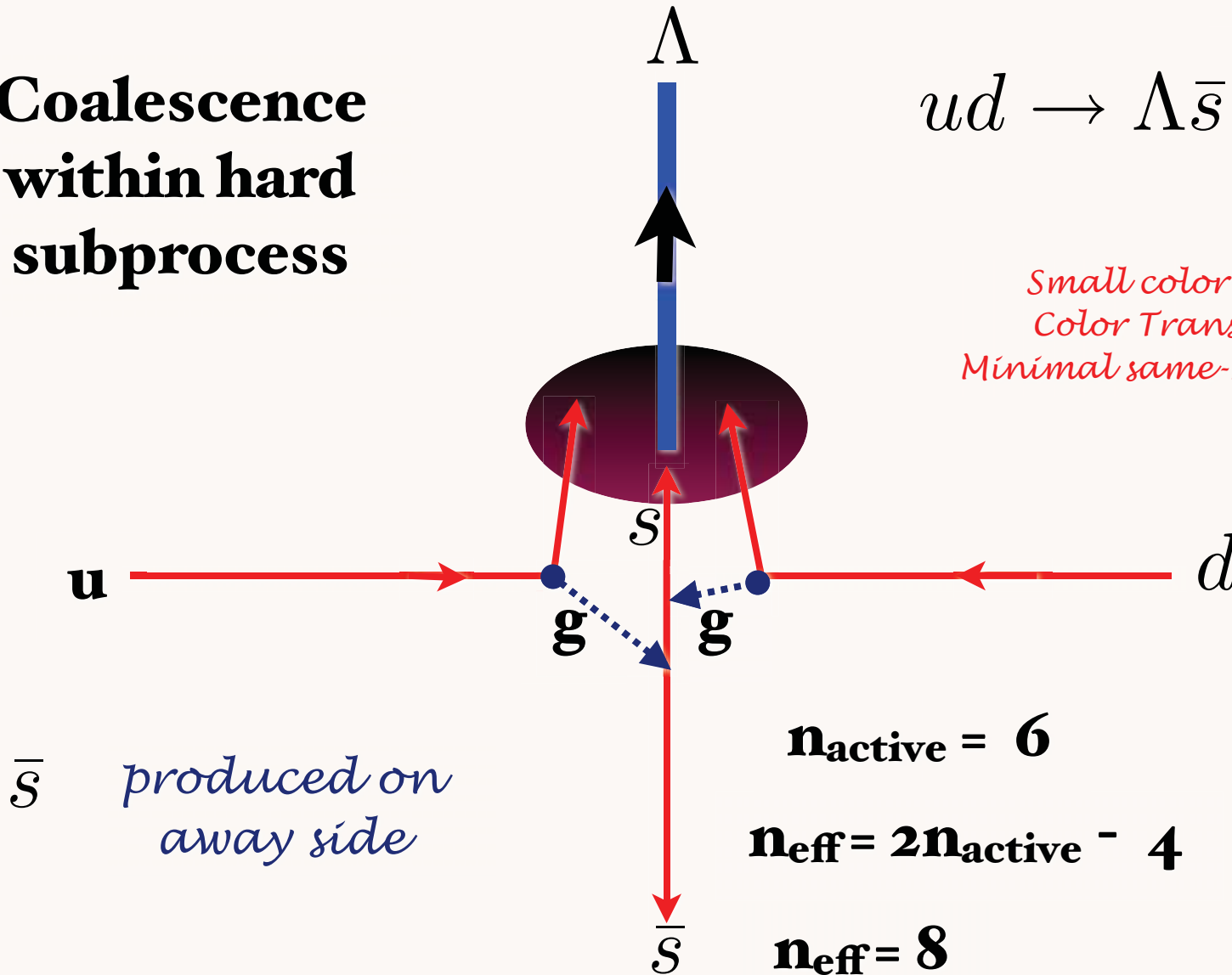
*Lambda can be made directly within hard subprocess*

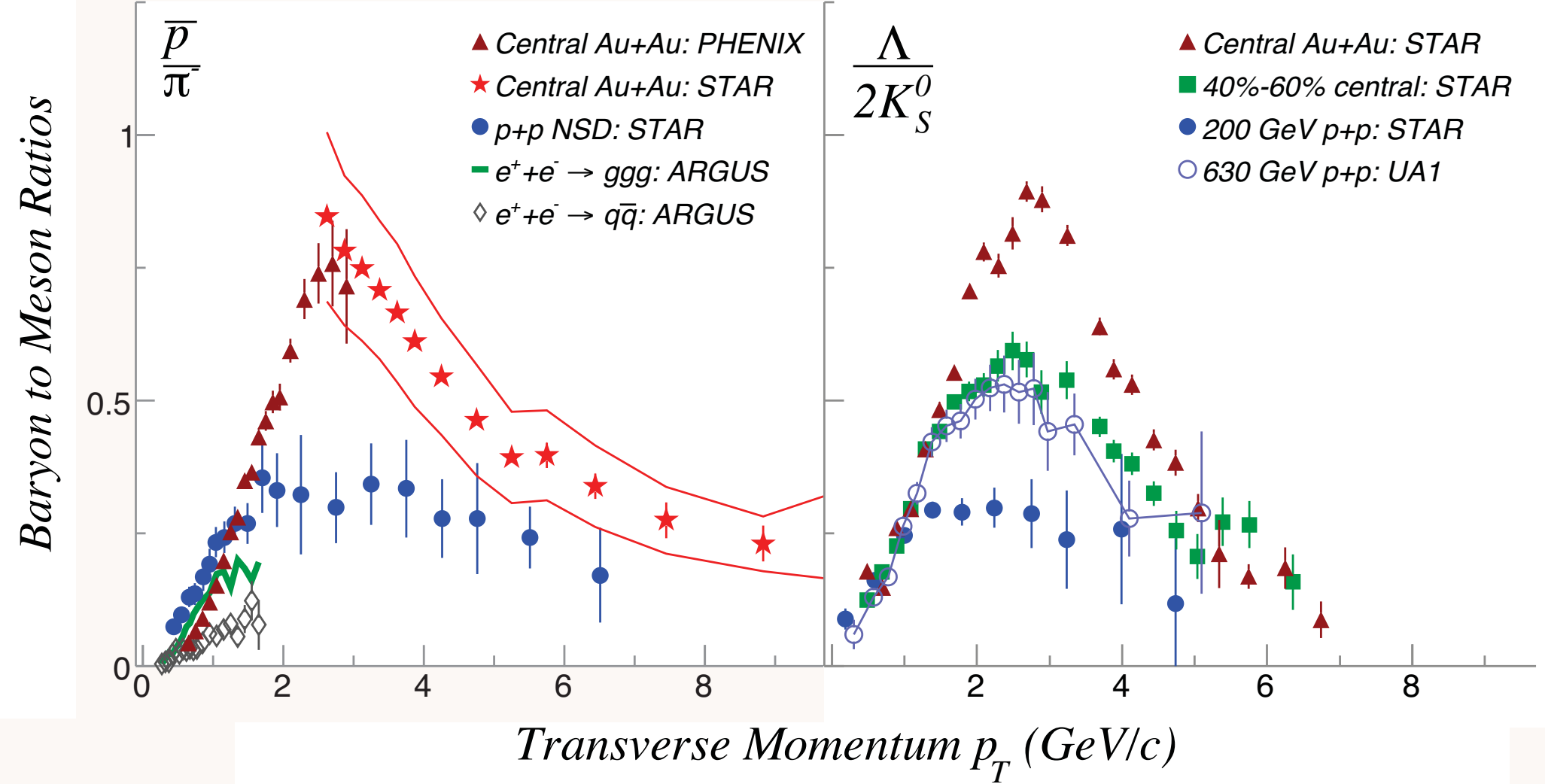
Anne Sickles, sjb

**Coalescence  
within hard  
subprocess**

$$ud \rightarrow \Lambda \bar{s}$$

*Small color-singlet  
Color Transparent  
Minimal same-side energy*







# *Baryon Anomaly: Evidence for Direct, Higher-Twist Subprocesses*

- **Explains anomalous power behavior at fixed  $x_T$**
- **Protons more likely to come from direct higher-twist subprocess than pions**
- **Protons less absorbed than pions in central nuclear collisions because of color transparency**
- **Predicts increasing proton to pion ratio in central collisions**
- **Proton power  $n_{\text{eff}}$  increases with centrality since leading twist contribution absorbed**
- **Fewer same-side hadrons for proton trigger at high centrality**
- **Exclusive-inclusive connection at  $x_T = 1$**

Anne Sickles, sjb

# *Higher Twist at the LHC*

- Fixed  $x_T$ : powerful analysis of PQCD
- Insensitive to modeling
- Higher twist terms energy efficient since no wasted fragmentation energy
- Evaluate at minimal  $x_1$  and  $x_2$  where structure functions are maximal
- Higher Twist competitive despite faster fall-off in  $p_T$
- Direct processes can confuse new physics searches

# Isolated hadrons

## Leading twist

Hadrons accompanied by a significant hadronic activity  $\Rightarrow$  inside jets

## Higher twist

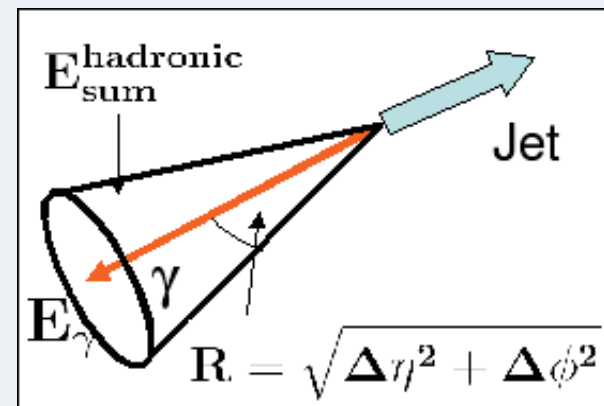
Color-singlet produced in the hard process  $\Rightarrow$  “isolated” hadrons

Idea: use isolation criteria to filter the leading twist component

$$E_{\perp}^{\text{had}} \leq E_{\perp}^{\text{max}} = \varepsilon p_{\perp}^h$$

for particles inside a cone

$$(\eta - \eta_{\gamma})^2 + (\phi - \phi_{\gamma})^2 \leq R^2$$



## Consequence

Enhanced scaling exponent for isolated hadrons

$$n_{\text{isolated}}^h > n_{\text{inclusive}}^h$$

$$|p, S_z\rangle = \sum_{n=3} \Psi_n(x_i, \vec{k}_{\perp i}, \lambda_i) |n; \vec{k}_{\perp i}, \lambda_i\rangle$$

*sum over states with  $n=3, 4, \dots$  constituents*

The Light Front Fock State Wavefunctions

$$\Psi_n(x_i, \vec{k}_{\perp i}, \lambda_i)$$

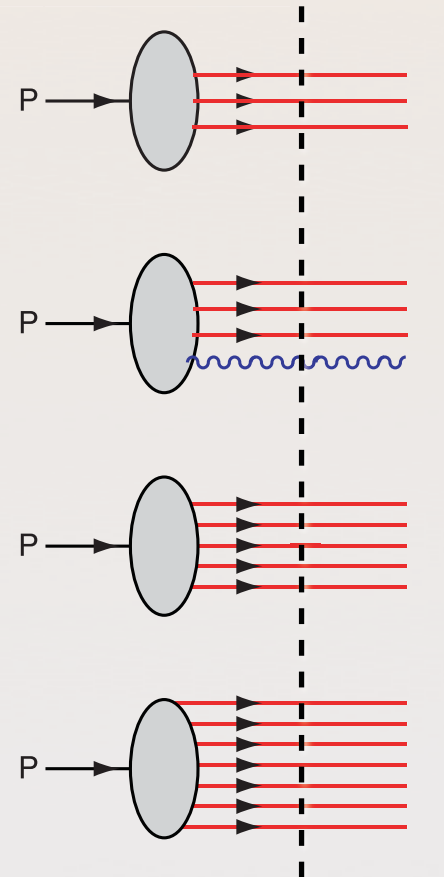
are boost invariant; they are independent of the hadron's energy and momentum  $P^\mu$ .

The light-cone momentum fraction

$$x_i = \frac{k_i^+}{p^+} = \frac{k_i^0 + k_i^z}{P^0 + P^z}$$

are boost invariant.

$$\sum_i^n k_i^+ = P^+, \quad \sum_i^n x_i = 1, \quad \sum_i^n \vec{k}_{i\perp} = \vec{0}^\perp.$$



*Fixed LF time*

*Intrinsic heavy quarks*  
 **$c(x), b(x)$  at high  $x$ !**

$$\bar{s}(x) \neq s(x)$$

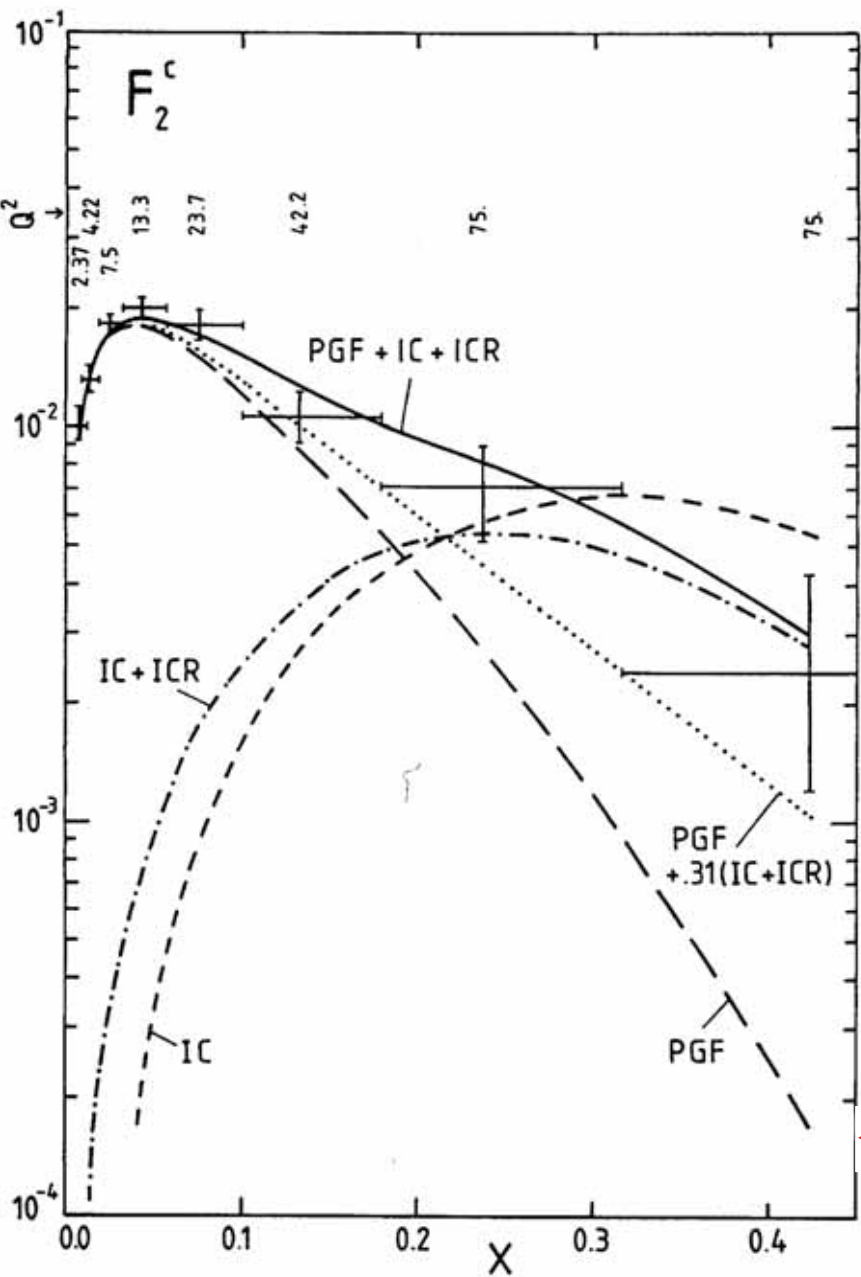
$$\bar{u}(x) \neq \bar{d}(x)$$

**Mueller: gluon Fock states<sub>128</sub>BFKL**

*Hidden Color*

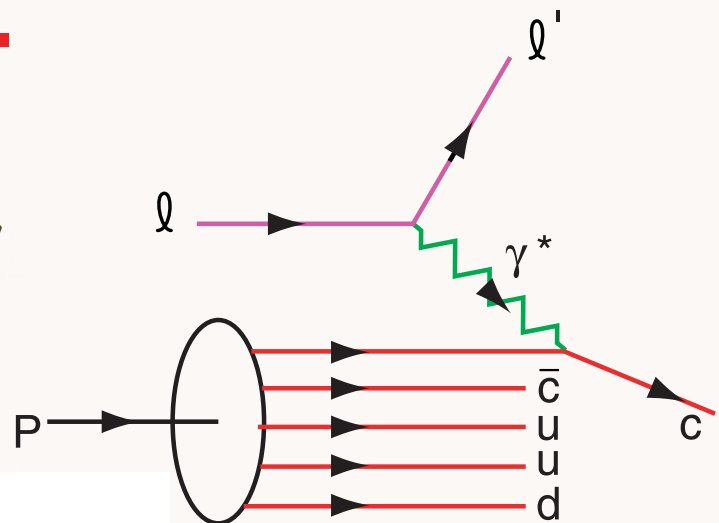
# Measurement of Charm Structure Function

J. J. Aubert et al. [European Muon Collaboration], "Production Of Charmed Particles In 250-GeV Mu<sup>+</sup> - Iron Interactions," Nucl. Phys. B 213, 31 (1983).



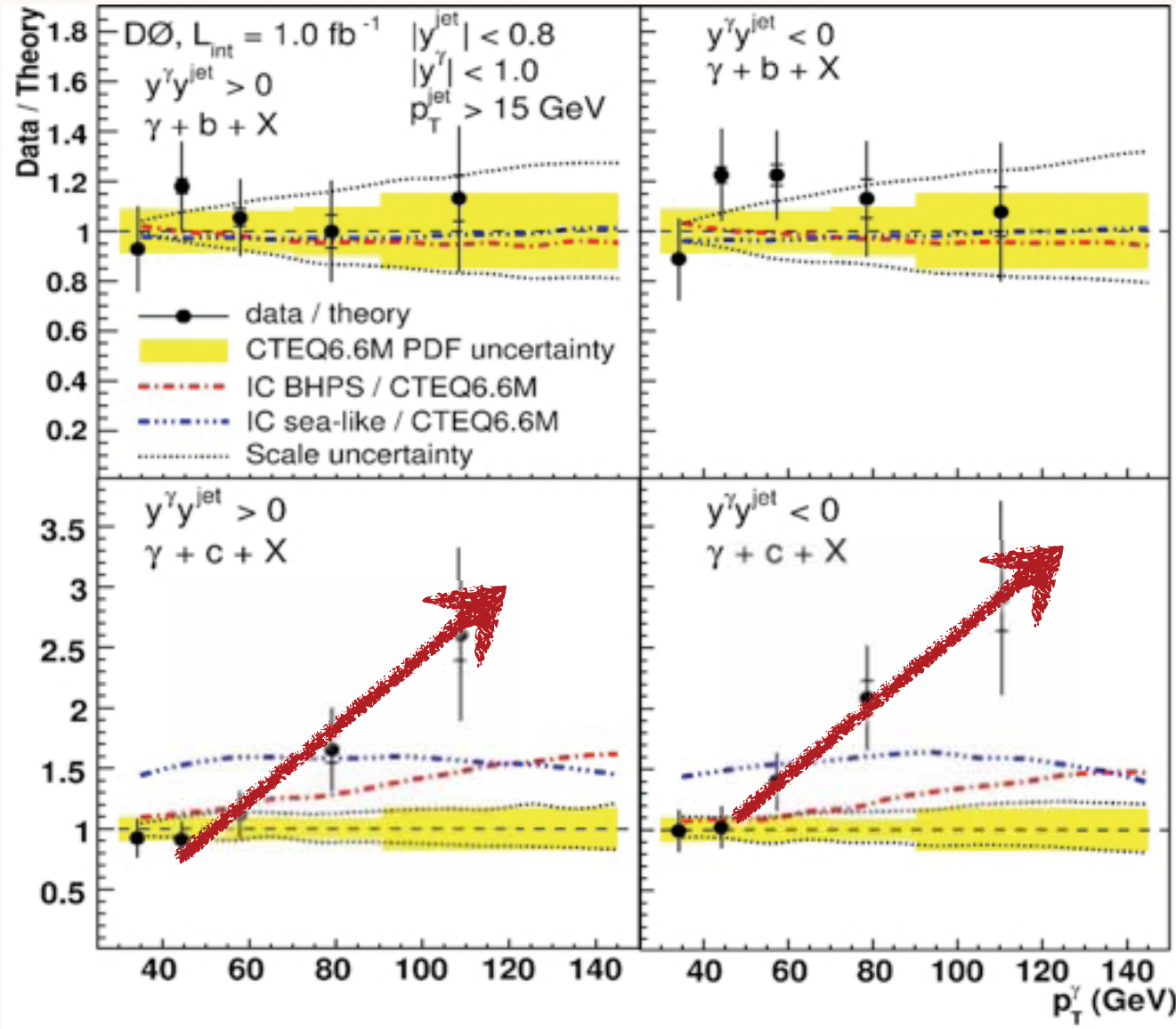
## First Evidence for Intrinsic Charm

factor of 30!



**DGLAP / Photon-Gluon Fusion: factor of 30 too small**

Measurement of  $\gamma + b + X$  and  $\gamma + c + X$  Production Cross Sections  
in  $p\bar{p}$  Collisions at  $\sqrt{s} = 1.96$  TeV

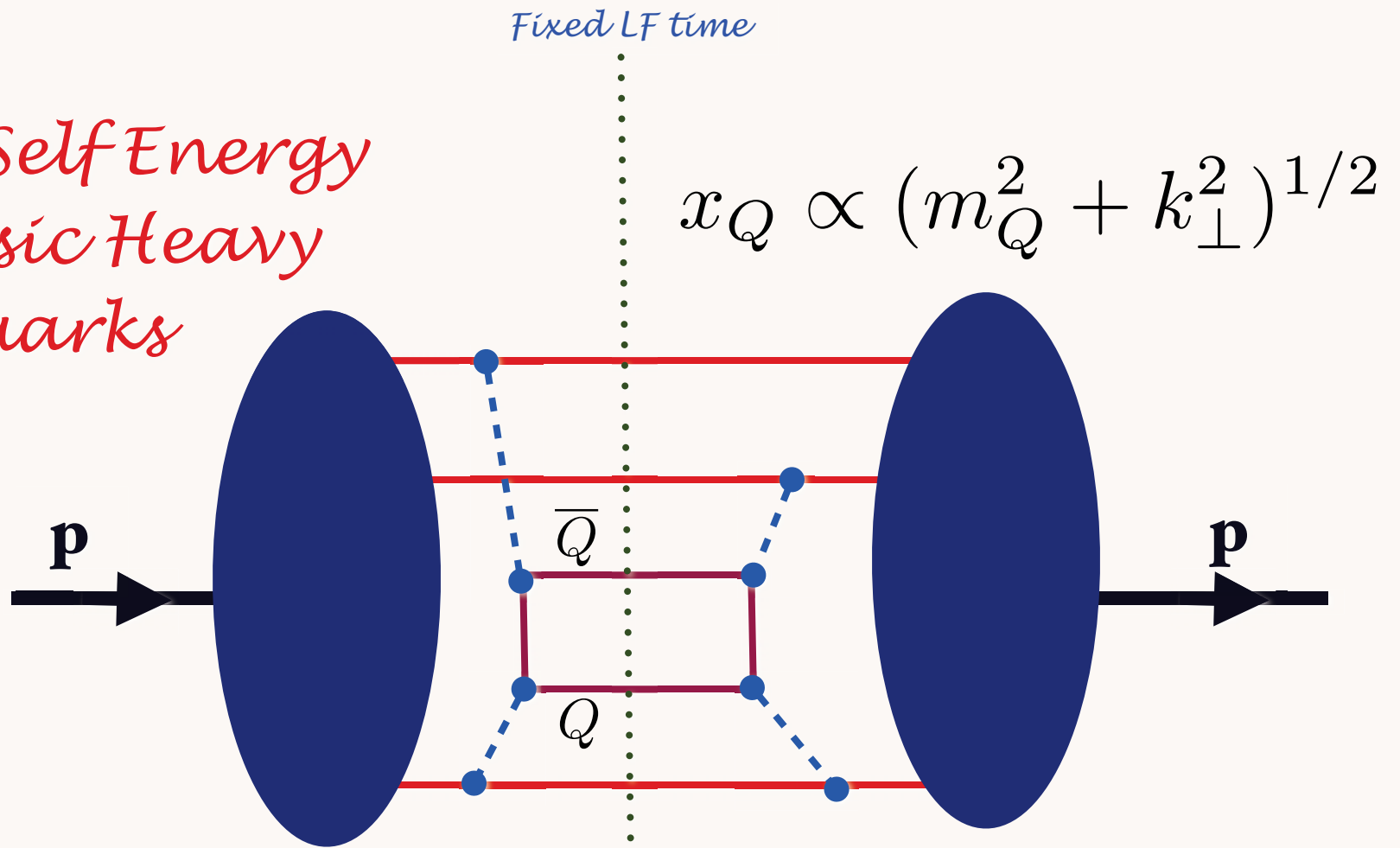


$$\frac{\Delta\sigma(\bar{p}p \rightarrow \gamma c X)}{\Delta\sigma(\bar{p}p \rightarrow \gamma b X)}$$

**Ratio  
insensitive to  
gluon PDF,  
scales**

**Signal for  
significant IC  
at  $x > 0.1$  ?**

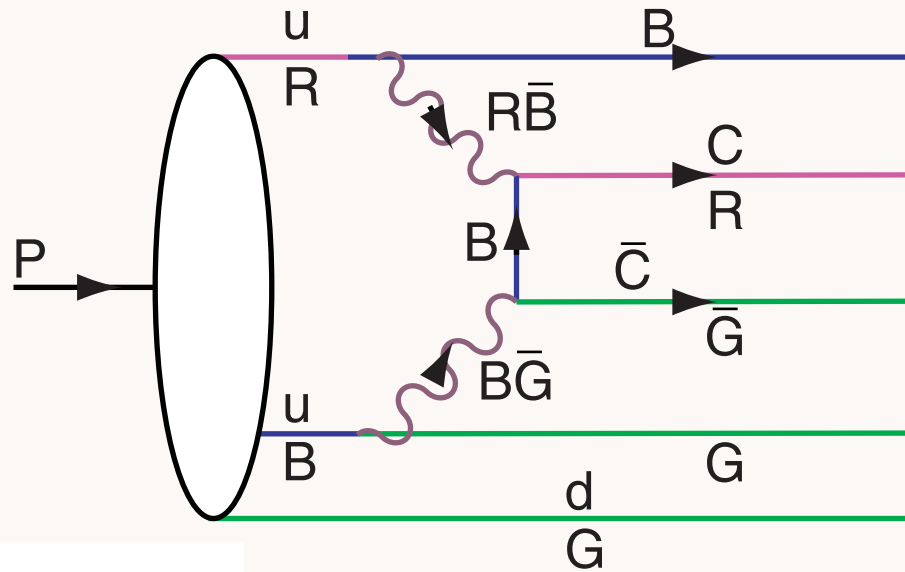
*Proton Self Energy  
Intrinsic Heavy  
Quarks*



Probability (QED)  $\propto \frac{1}{M_{\ell}^4}$

Probability (QCD)  $\propto \frac{1}{M_Q^2}$

**Collins, Ellis, Gunion, Mueller, sjb  
M. Polyakov**



$|uudc\bar{c}\rangle$  Fluctuation in Proton

QCD: Probability  $\sim \frac{\Lambda_{QCD}^2}{M_Q^2}$

$|e^+e^-\ell^+\ell^-\rangle$  Fluctuation in Positronium

QED: Probability  $\sim \frac{(m_e\alpha)^4}{M_\ell^4}$

OPE derivation - M.Polyakov et al.

$$\langle p | \frac{G_{\mu\nu}^3}{m_Q^2} | p \rangle \text{ vs. } \langle p | \frac{F_{\mu\nu}^4}{m_\ell^4} | p \rangle$$

$c\bar{c}$  in Color Octet

Distribution peaks at equal rapidity (velocity)  
Therefore heavy particles carry the largest momentum fractions

$$\hat{x}_i = \frac{m_{\perp i}}{\sum_j^n m_{\perp j}}$$

*High x charm!*

*Charm at Threshold*

**Action Principle: Minimum KE, maximal potential**



## INTRINSIC CHEVROLETS AT THE SSC

Stanley J. Brodsky

Stanford Linear Accelerator Center, Stanford University, Stanford CA 94305

John C. Collins

Department of Physics, Illinois Institute of Technology, Chicago IL 60616  
and  
High Energy Physics Division, Argonne National Laboratory, Argonne IL 60439

Stephen D. Ellis

Department of Physics, FM-15, University of Washington, Seattle WA 98195

John F. Gunion

Department of Physics, University of California, Davis CA 95616

Alfred H. Mueller

Department of Physics, Columbia University, New York NY 10027



$$\mathcal{L}_{QCD}^{eff} = -\frac{1}{4}F_{\mu\nu a}F^{\mu\nu a} - \frac{g^2 N_C}{120\pi^2 M_Q^2} D_\alpha F_{\mu\nu a} D^\alpha F^{\mu\nu a} + C \frac{g^2 N_C}{120\pi^2 M_Q^2} F_\mu^{a\nu} F_\nu^{b\tau} F_\tau^{c\mu} f_{abc} + \mathcal{O}\left(\frac{1}{M_Q^4}\right)$$

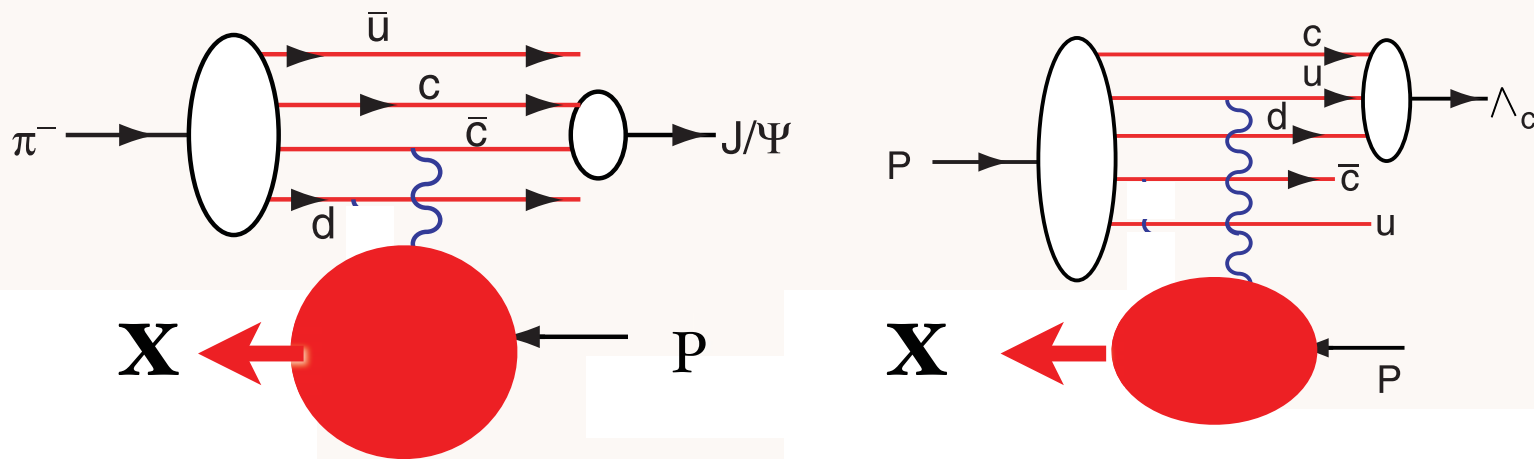
*Probability of Intrinsic Heavy Quarks  $\sim 1/M_Q^2$*

- EMC data:  $c(x, Q^2) > 30 \times \text{DGLAP}$   
 $Q^2 = 75 \text{ GeV}^2, x = 0.42$
- High  $x_F$   $pp \rightarrow J/\psi X$
- High  $x_F$   $pp \rightarrow J/\psi J/\psi X$
- High  $x_F$   $pp \rightarrow \Lambda_c X$
- High  $x_F$   $pp \rightarrow \Lambda_b X$
- High  $x_F$   $pp \rightarrow \Xi(ccd) X$  (SELEX)

## IC Structure Function: Critical Measurement for EIC

**Many interesting spin, charge asymmetry, spectator effects**

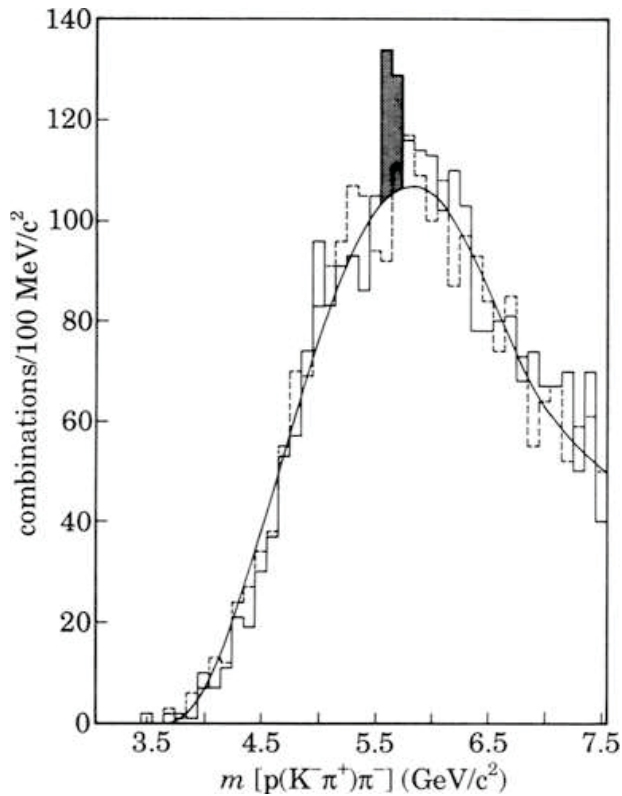
# Leading Hadron Production from Intrinsic Charm



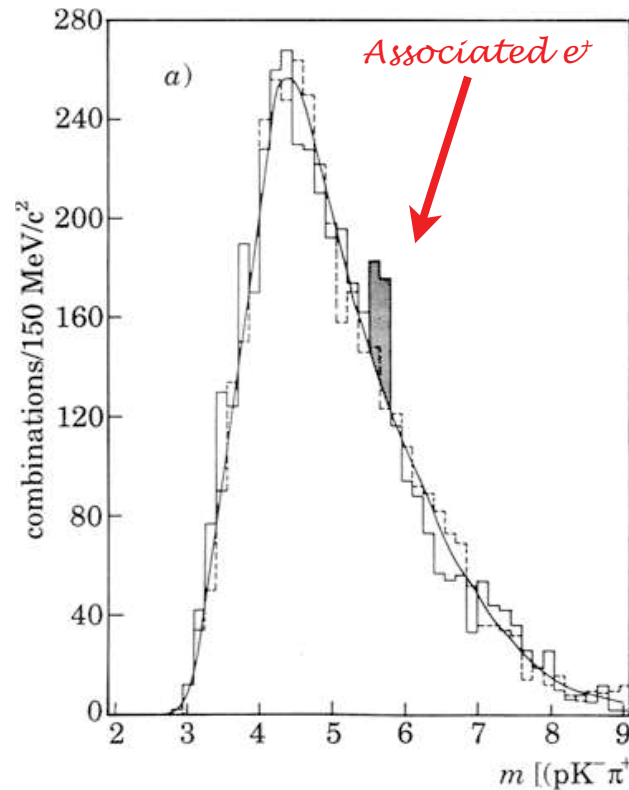
Coalescence of Comoving Charm and Valence Quarks  
Produce  $J/\psi$ ,  $\Lambda_c$  and other Charm Hadrons at High  $x_F$

$$pp \rightarrow \Lambda_b(bud)B(\bar{b}q)X \text{ at large } x_F$$

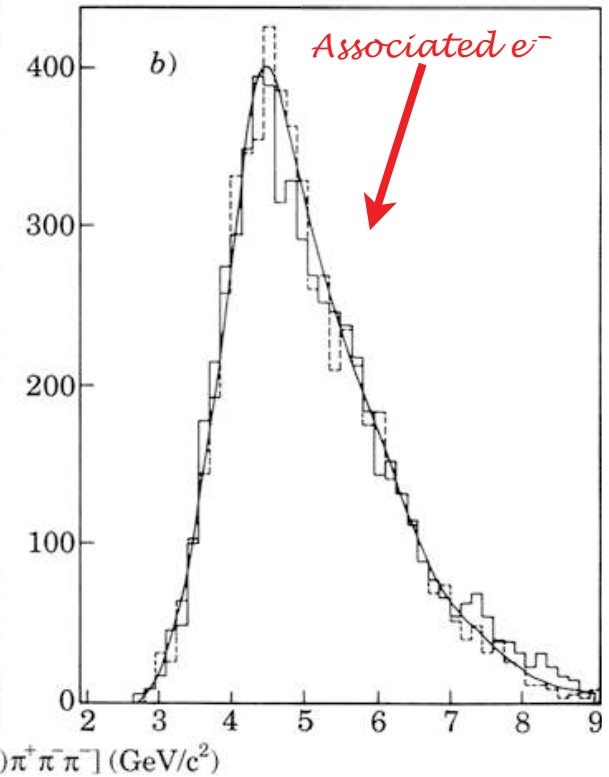
## CERN-ISR R422 (Split Field Magnet), 1988/1991



$$\Lambda_b^0 \rightarrow p D^0 \pi^-$$

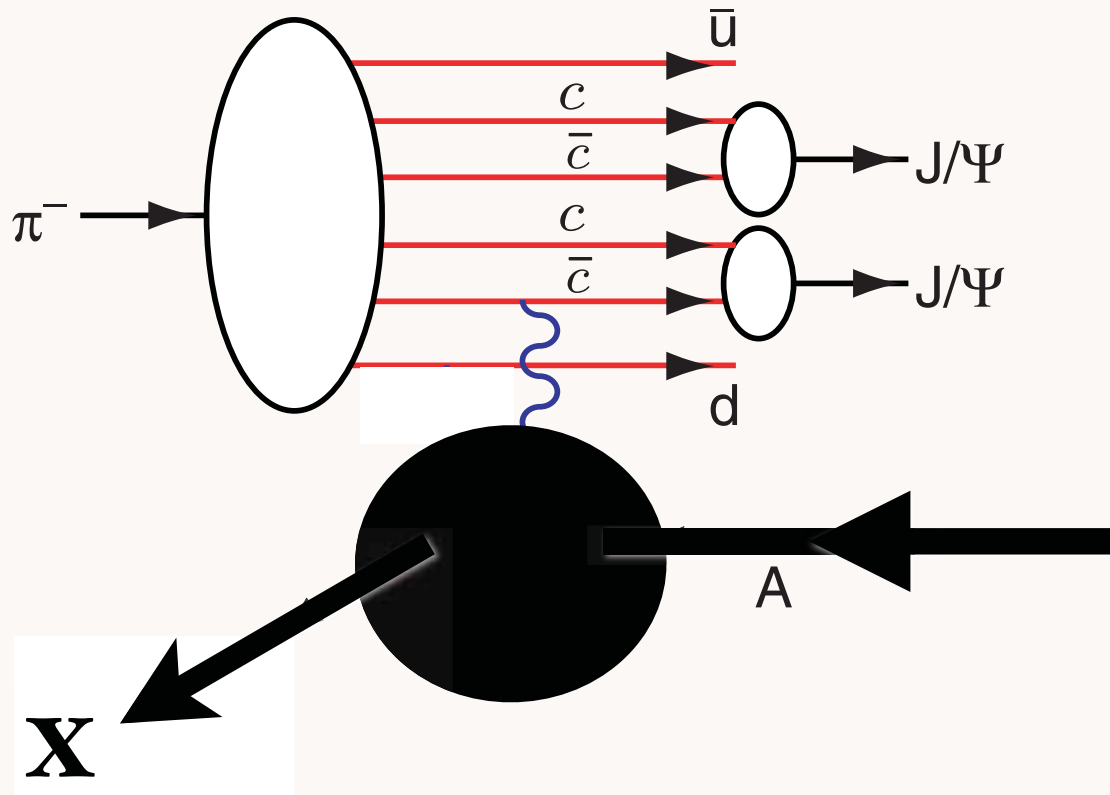


$$\Lambda_b^0 \rightarrow \Lambda_c^+ \pi^+ \pi^- \pi^-$$



Il Nuovo Cimento 104, 1787

# Production of Two Charmonia at High $x_F$



All events have  $x_{\psi\psi}^F > 0.4$  !

**Excludes 'color drag' model**

$$\pi A \rightarrow J/\psi J/\psi X$$

Intrinsic charm contribution to double quarkonium hadroproduction \*

R. Vogt<sup>a</sup>, S.J. Brodsky<sup>b</sup>

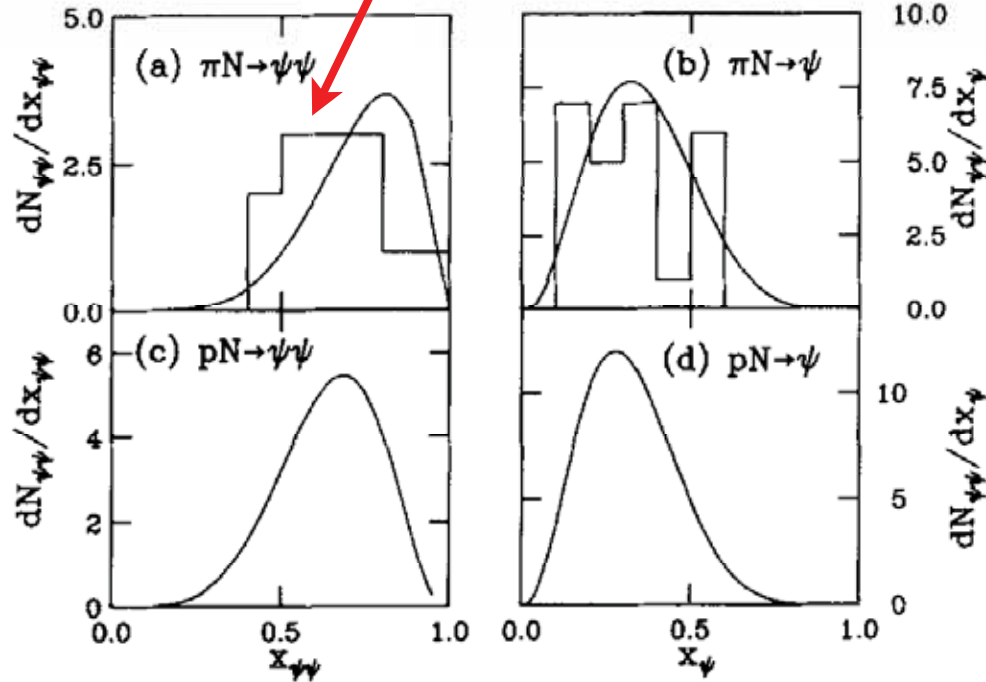
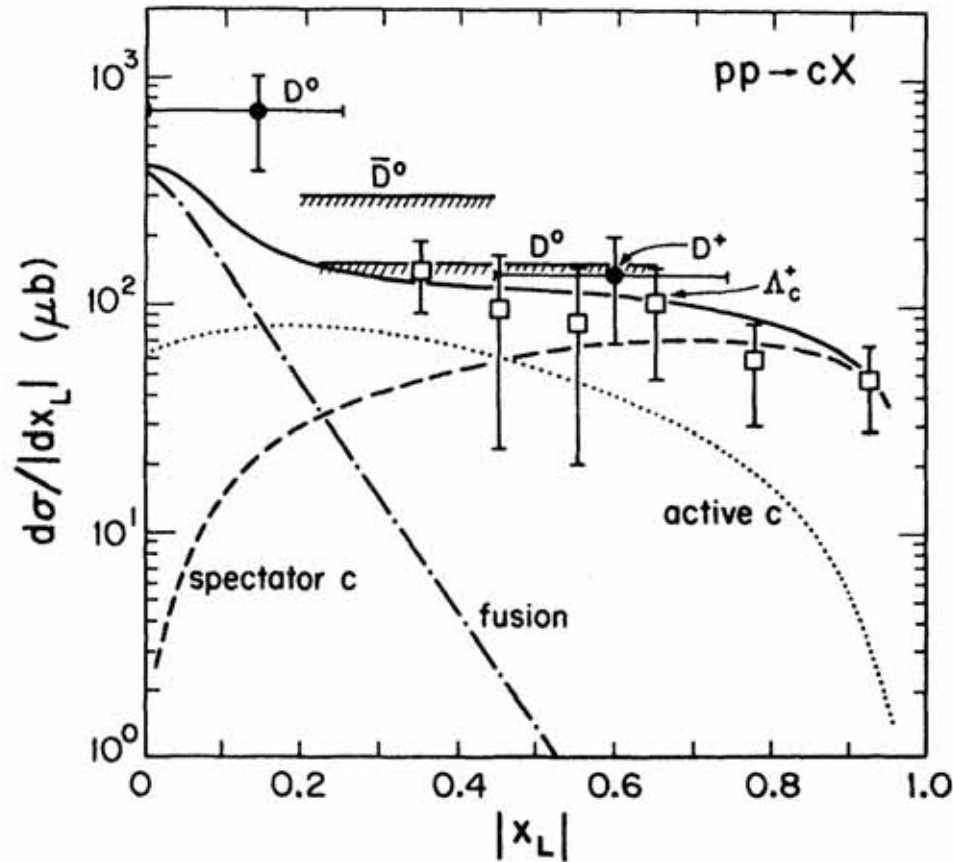


Fig. 3. The  $\psi\psi$  pair distributions are shown in (a) and (c) for the pion and proton projectiles. Similarly, the distributions of  $J/\psi$ 's from the pairs are shown in (b) and (d). Our calculations are compared with the  $\pi^- N$  data at 150 and 280 GeV/c [1]. The  $x_{\psi\psi}$  distributions are normalized to the number of pairs from both pion beams (a) and the number of pairs from the 400 GeV proton measurement (c). The number of single  $J/\psi$ 's is twice the number of pairs.

The probability distribution for a general  $n$ -parton intrinsic  $c\bar{c}$  Fock state as a function of  $x$  and  $k_T$  written as

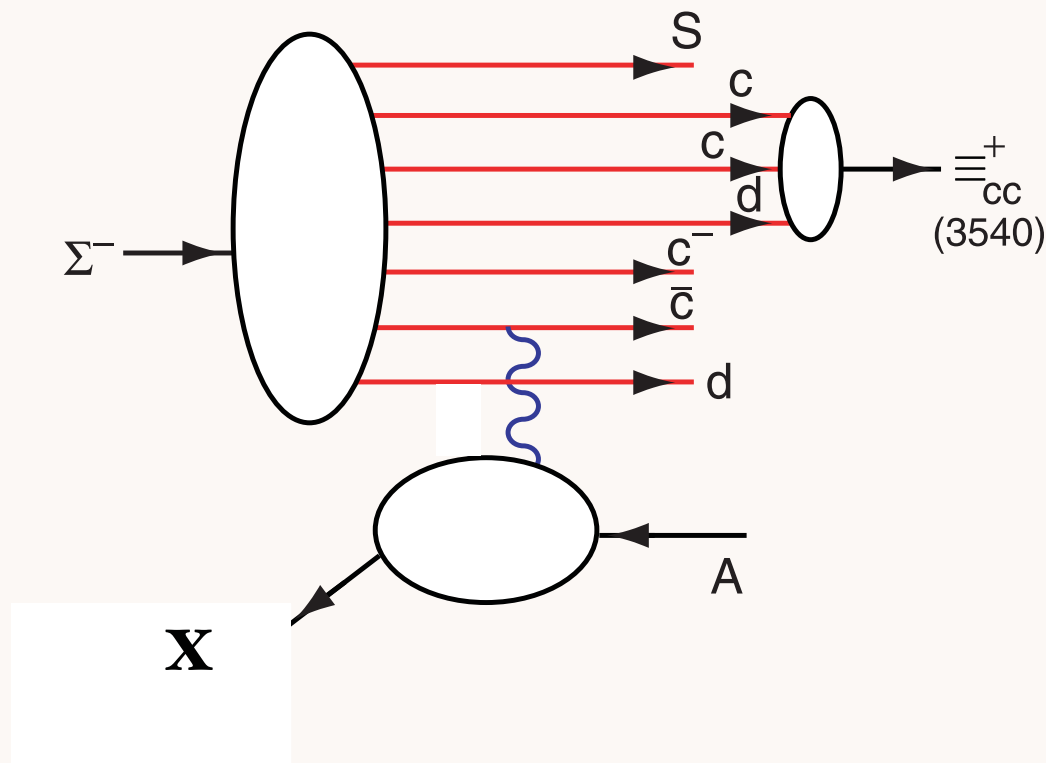
$$\frac{dP_{ic}}{\prod_{i=1}^n dx_i d^2k_{T,i}} = N_n \alpha_s^4 (M_{c\bar{c}}) \frac{\delta(\sum_{i=1}^n k_{T,i}) \delta(1 - \sum_{i=1}^n x_i)}{(m_h^2 - \sum_{i=1}^n (m_{T,i}^2/x_i))^2},$$

**NA3 Data**



*Model similar to  
Intrinsic Charm*

V. D. Barger, F. Halzen and W. Y. Keung,  
 “The Central And Diffractive Components Of Charm Pro-  
 duction,”  
 Phys. Rev. D 25, 112 (1982).



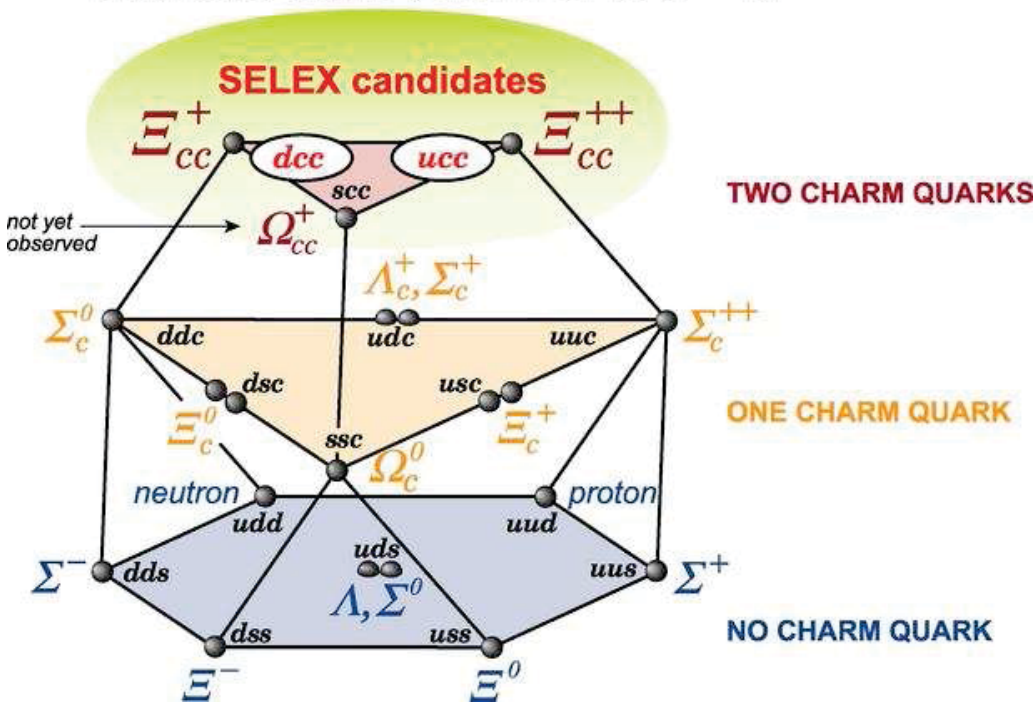
## *Production of a Double-Charm Baryon*

**SELEX high  $x_F$**        $\langle x_F \rangle = 0.33$

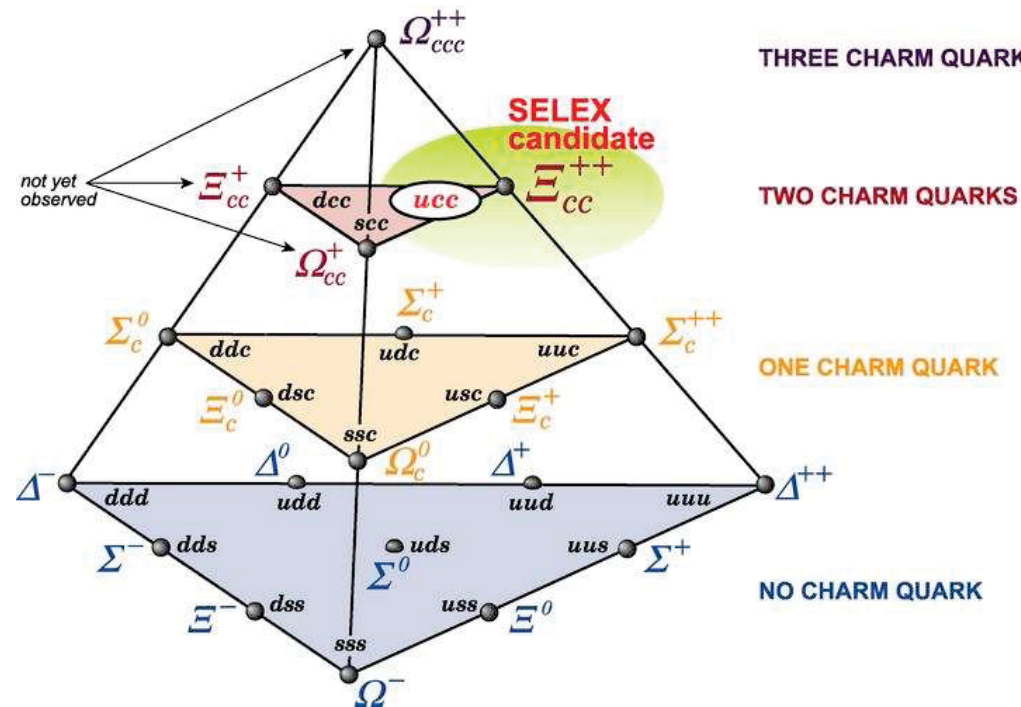


# Doubly Charmed Baryons

BARYONS WITH LOWEST SPIN ( $J = 1/2$ )

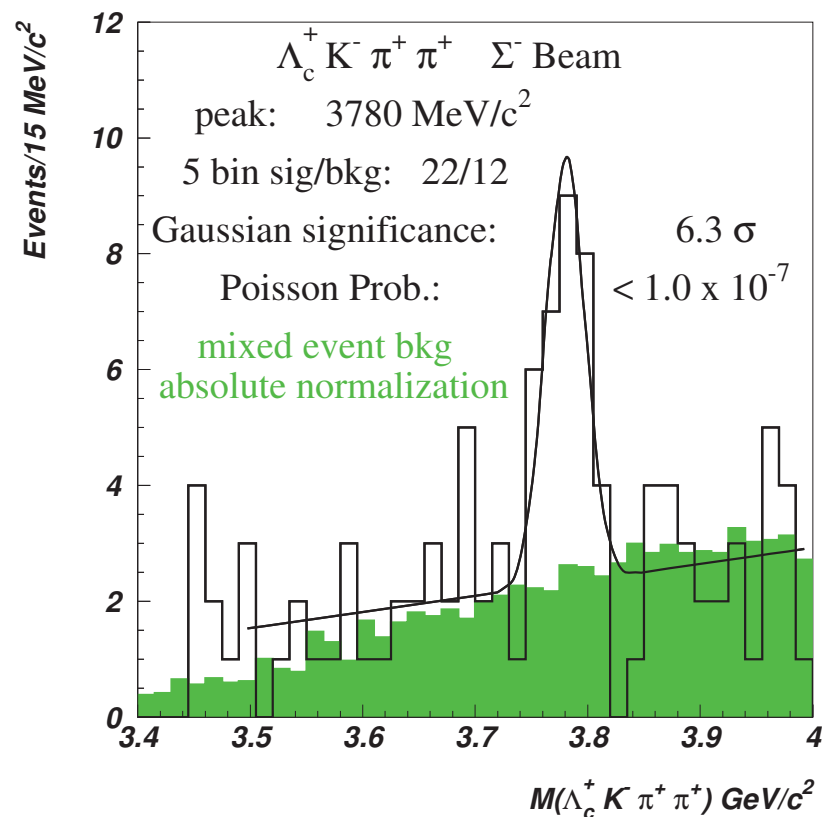


BARYONS WITH HIGHEST SPIN ( $J = 3/2$ )

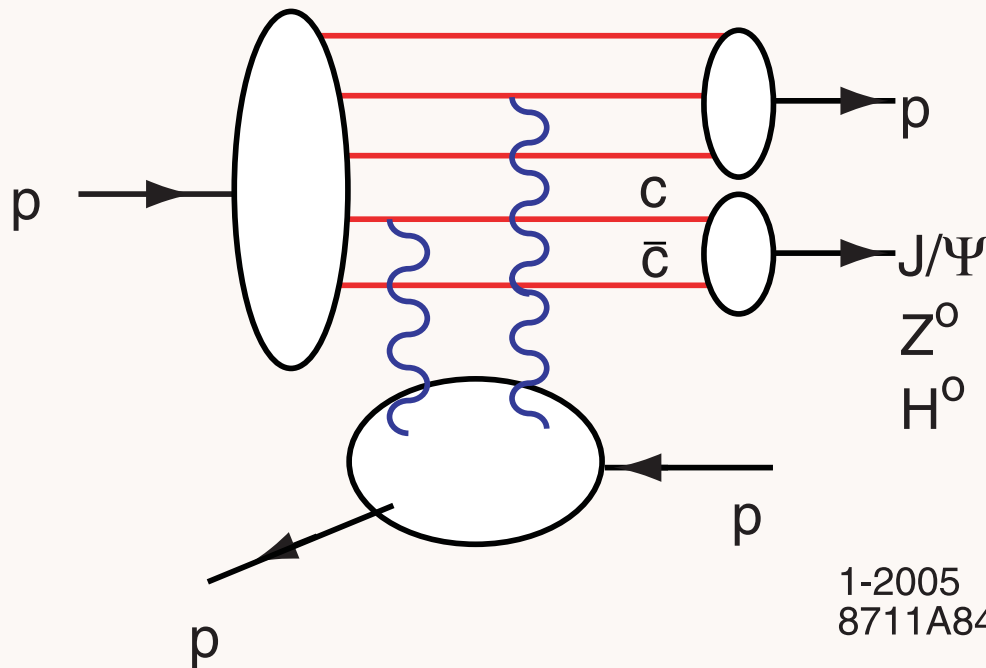


$$\Xi_{cc}(3780)^{++} \rightarrow \Lambda_c^+ K^- \pi^+ \pi^+$$

- Re-Analyzed Data
- Restrict to  $\Sigma^-$ -Beam
- Peak wider than Resolution
- Half decay to  $\Xi_{cc}^+(3520)$
- Still working on Details



# Intrinsic Charm Mechanism for Exclusive Diffraction Production



$$p p \rightarrow J/\psi p p$$

$$x_{J/\psi} = x_c + x_{\bar{c}}$$

Exclusive Diffractive  
High- $X_F$  Higgs Production

Kopeliovitch, Schmidt, Soffer, sjb

1-2005  
8711A84

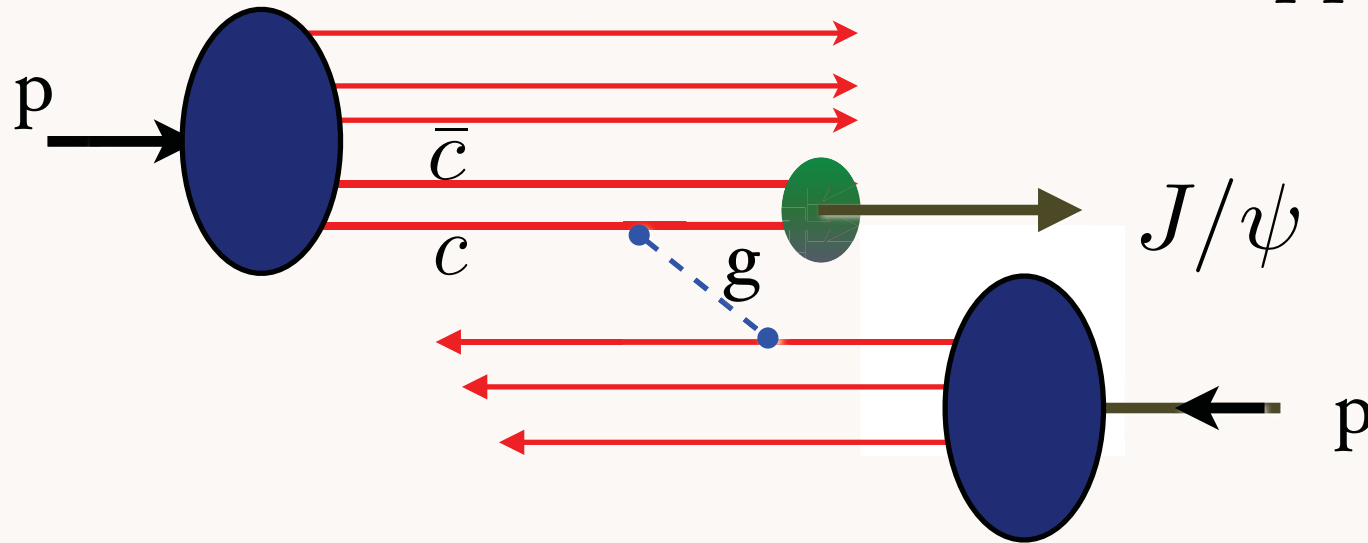
Intrinsic  $c\bar{c}$  pair formed in color octet  $8_C$  in proton wavefunction Large Color Dipole

Collision produces color-singlet  $J/\psi$  through color exchange

RHIC Experiment

# Intrinsic Charm Mechanism for Inclusive High- $x_F$ Quarkonium Production

$$pp \rightarrow J/\psi X$$



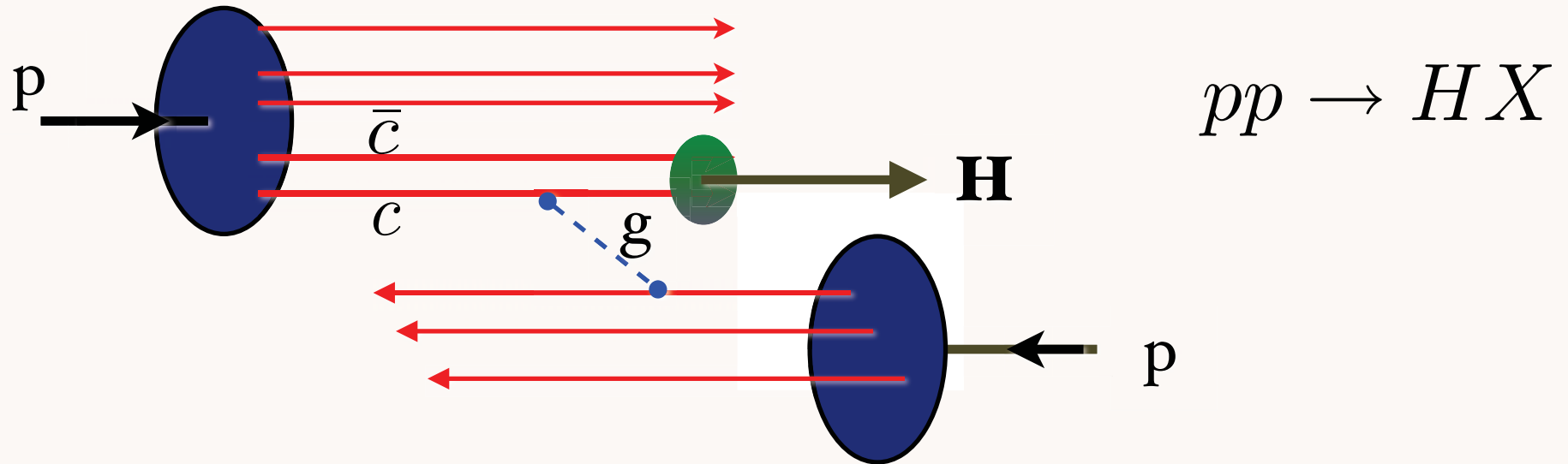
Goldhaber, Kopeliovich, Soffer, Schmidt, sjb

**Quarkonia can have 80% of Proton Momentum!**

*Color-octet IC interacts at front surface of nucleus*

**IC can explain large excess of quarkonia at large  $x_F$ , A-dependence**

# Intrinsic Charm Mechanism for Inclusive High- $X_F$ Higgs Production



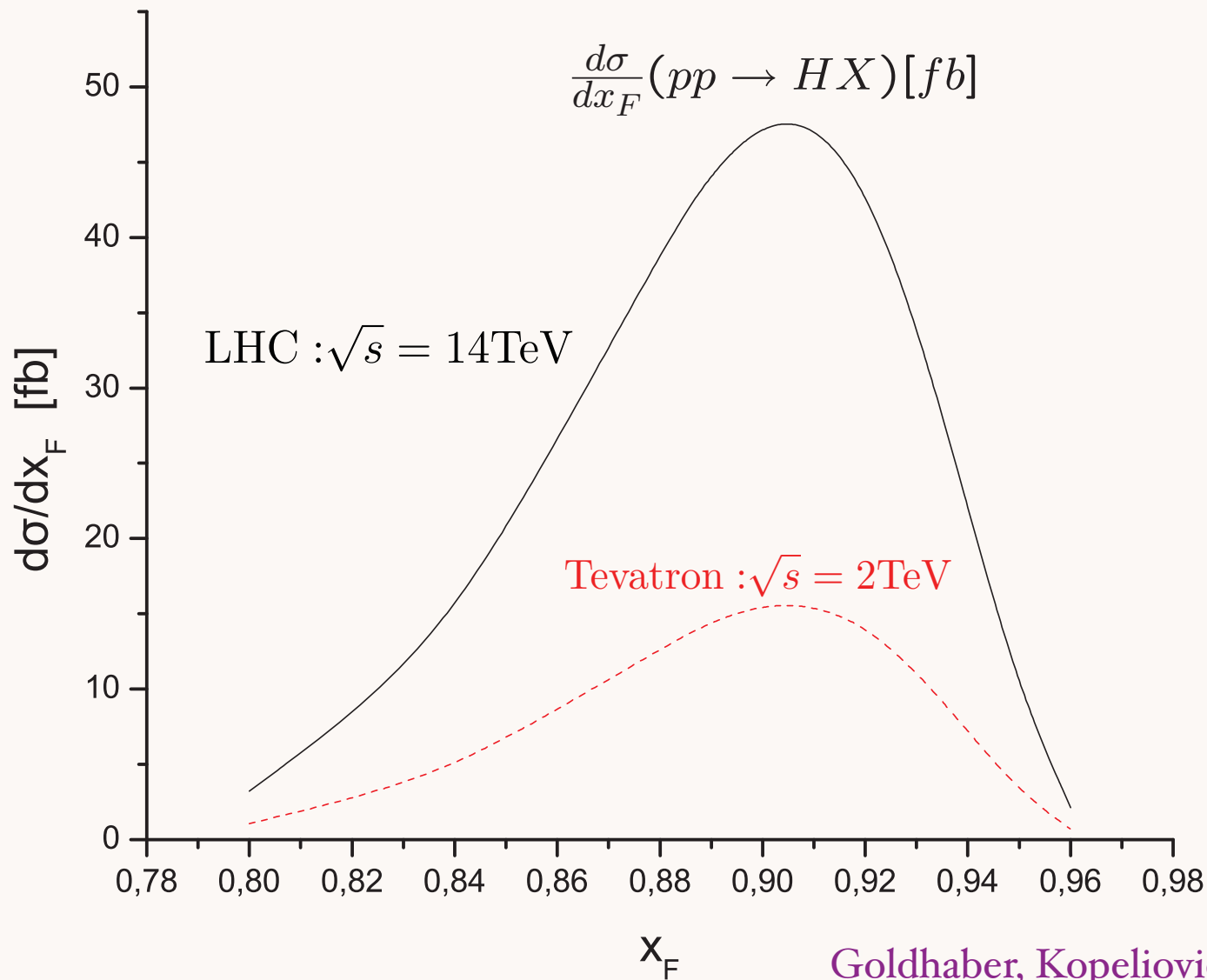
Goldhaber, Kopeliovich, Schmidt, sjb

**Also: intrinsic bottom, top**

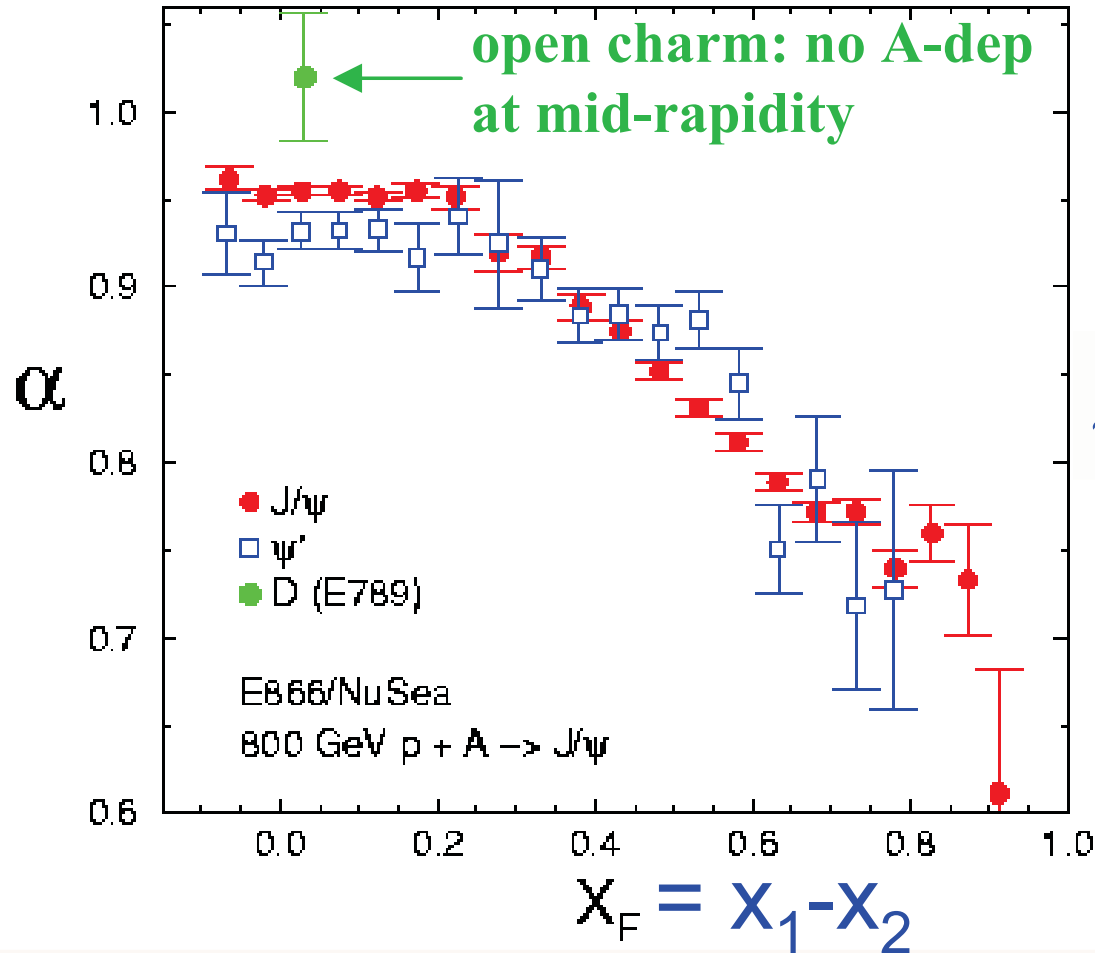
**Higgs can have 80% of Proton Momentum!**

*New search strategy for Higgs*

# Intrinsic Bottom Contribution to Inclusive Higgs Production



800 GeV p-A (FNAL)  $\sigma_A = \sigma_p * A^\alpha$   
*PRL 84, 3256 (2000); PRL 72, 2542 (1994)*



$$\frac{d\sigma}{dx_F} (pA \rightarrow J/\psi X)$$

*Remarkably Strong Nuclear Dependence for Fast Charmonium*

*Violation of PQCD Factorization*

Violation of factorization in charm hadroproduction.

[P. Hoyer](#), [M. Vanttinen](#) ([Helsinki U.](#)), [U. Sukhatme](#) ([Illinois U., Chicago](#)) . HU-TFT-90-14, May 1990. 7pp.

Published in Phys.Lett.B246:217-220,1990

**IC Explains large excess of quarkonia at large  $x_F$ , A-dependence**

# Heavy Quark Anomalies

Nuclear dependence of  $J/\psi$  hadroproduction

Violates PQCD Factorization:  $A^\alpha(x_F)$  not  $A^\alpha(x_2)$

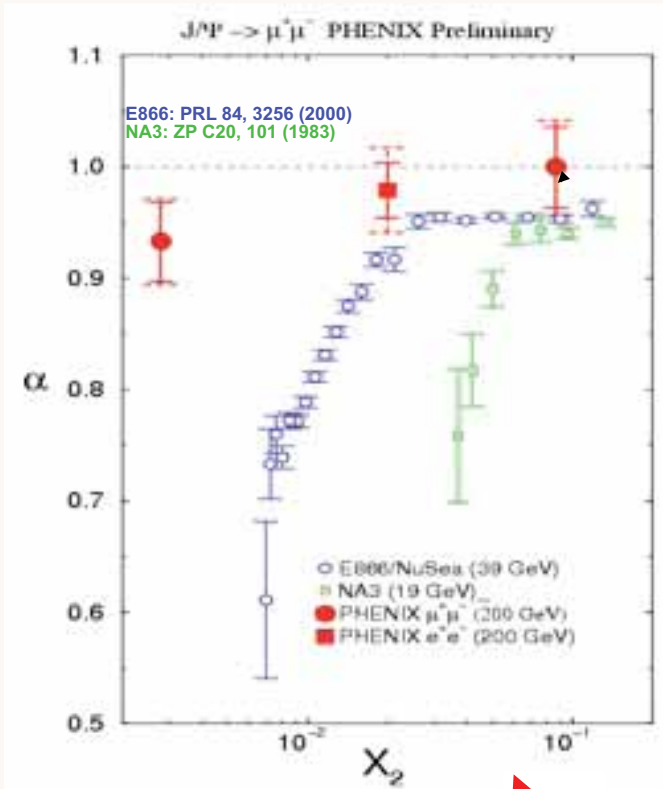
Huge  $A^{2/3}$  effect at large  $x_F$



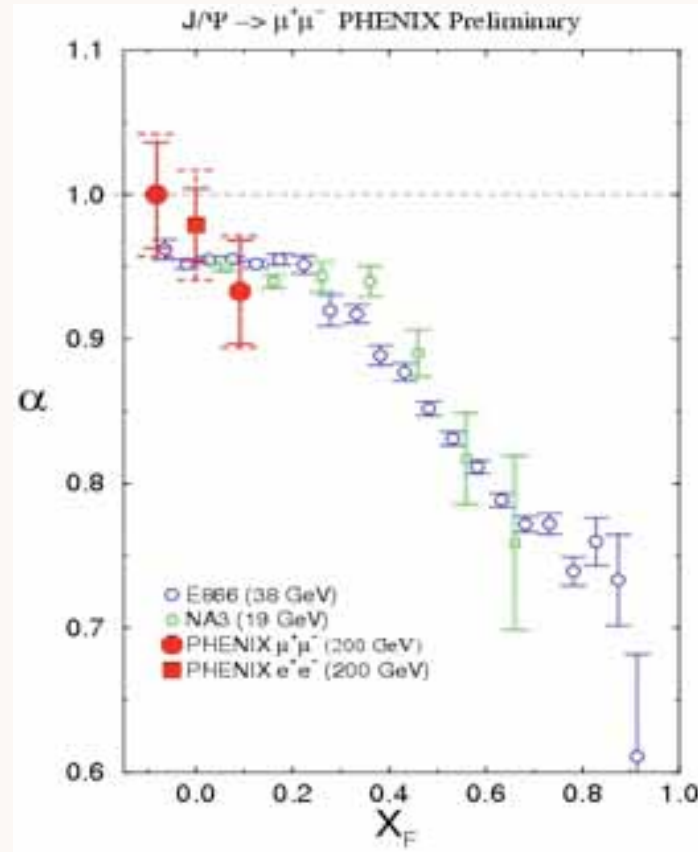
# J/ψ nuclear dependence vrs rapidity, $x_{Au}$ , $x_F$

M. Leitch

## PHENIX compared to lower energy measurements



Klein, Vogt, PRL 91:142301, 2003  
Kopeliovich, NP A696:669, 2001



Huge  
“absorption”  
effect



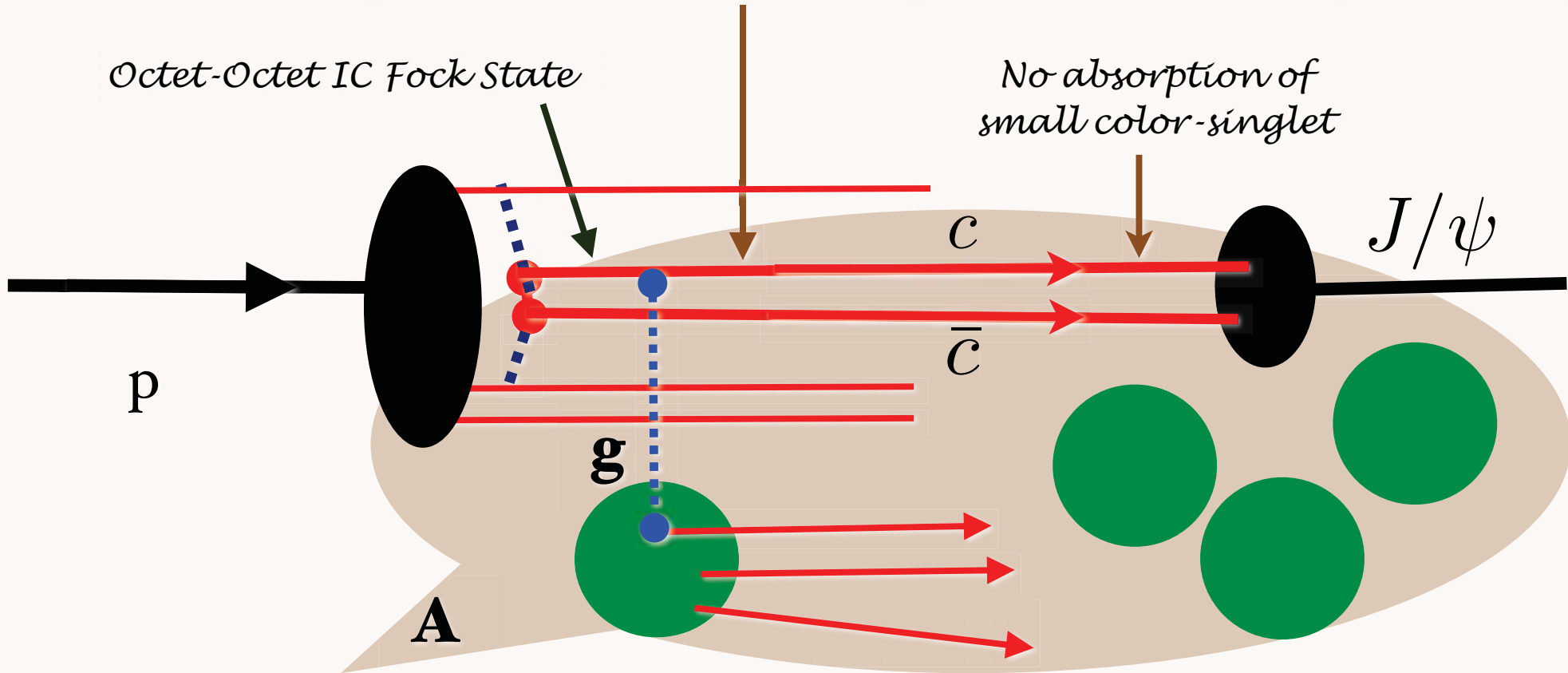
*Violates PQCD  
factorization!*

$$\frac{d\sigma}{dx_F}(pA \rightarrow J/\psi X)$$

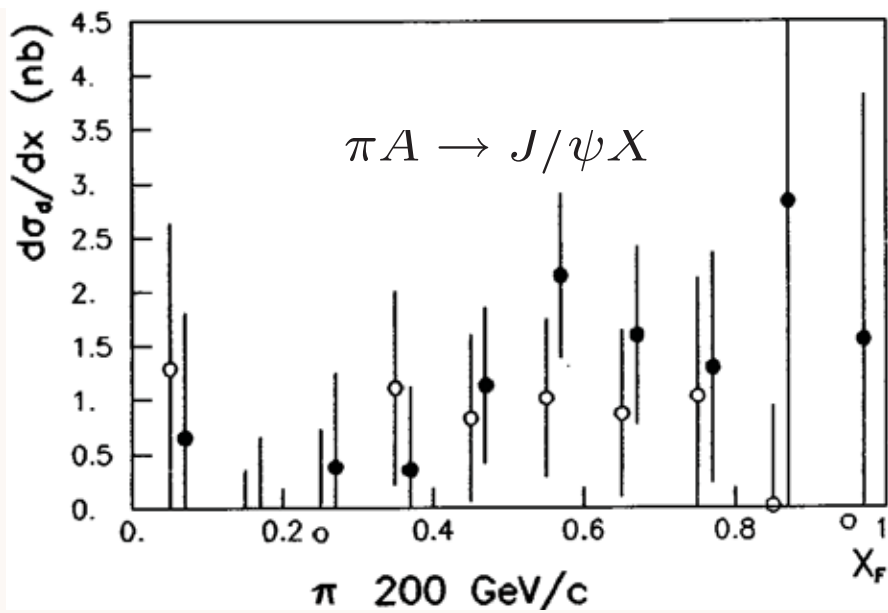
Hoyer, Sukhatme, Vanttinen

*Color-Opaque IC Fock state  
interacts on nuclear front surface*

*Scattering on front-face nucleon produces color-singlet  $c\bar{c}$  pair*

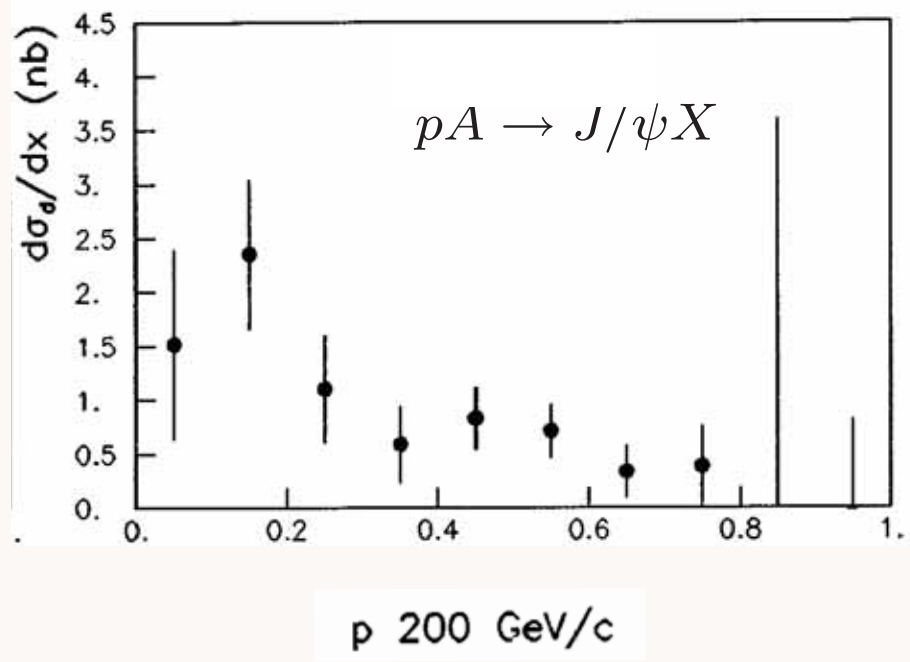


$$\frac{d\sigma}{dx_F}(pA \rightarrow J/\psi X) = A^{2/3} \times \frac{d\sigma}{dx_F}(pN \rightarrow J/\psi X)$$



$A^{2/3}$  component

J. Badier et al, NA3



$$\frac{d\sigma}{dx_F}(pA \rightarrow J/\psi X) = A^1 \frac{d\sigma_1}{dx_F} + A^{2/3} \frac{d\sigma_{2/3}}{dx_F}$$

**Excess beyond conventional PQCD subprocesses**

- IC Explains Anomalous  $\alpha(x_F)$  not  $\alpha(x_2)$  dependence of  $pA \rightarrow J/\psi X$   
(Mueller, Gunion, Tang, SJB)
- Color Octet IC Explains  $A^{2/3}$  behavior at high  $x_F$  (NA3, Fermilab) *Color Opacity*  
(Kopeliovitch, Schmidt, Soffer, SJB)
- IC Explains  $J/\psi \rightarrow \rho\pi$  puzzle  
(Karliner, SJB)
- IC leads to new effects in  $B$  decay  
(Gardner, SJB)

## Higgs production at $x_F = 0.8$

## *Why is Intrinsic Charm Important for Flavor Physics?*

- **New perspective on fundamental nonperturbative hadron structure**
- **Charm structure function at high  $x$**
- **Dominates high  $x_F$  charm and charmonium production**
- **Hadroproduction of new heavy quark states such as  $ccu$ ,  $ccd$  at high  $x_F$**
- **Intrinsic charm -- long distance contribution to penguin mechanisms for weak decay**
- **Novel Nuclear Effects from color structure of IC, Heavy Ion Collisions**
- **New mechanisms for high  $x_F$  Higgs hadroproduction**
- **Dynamics of  $b$  production: LHCb**
- **Fixed target program at LHC: produce  $bbb$  states**

# Light-Front Wavefunctions

Dirac's Front Form: Fixed  $\tau = t + z/c$

$$\Psi(x, k_{\perp}) \quad x_i = \frac{k_i^+}{P^+}$$

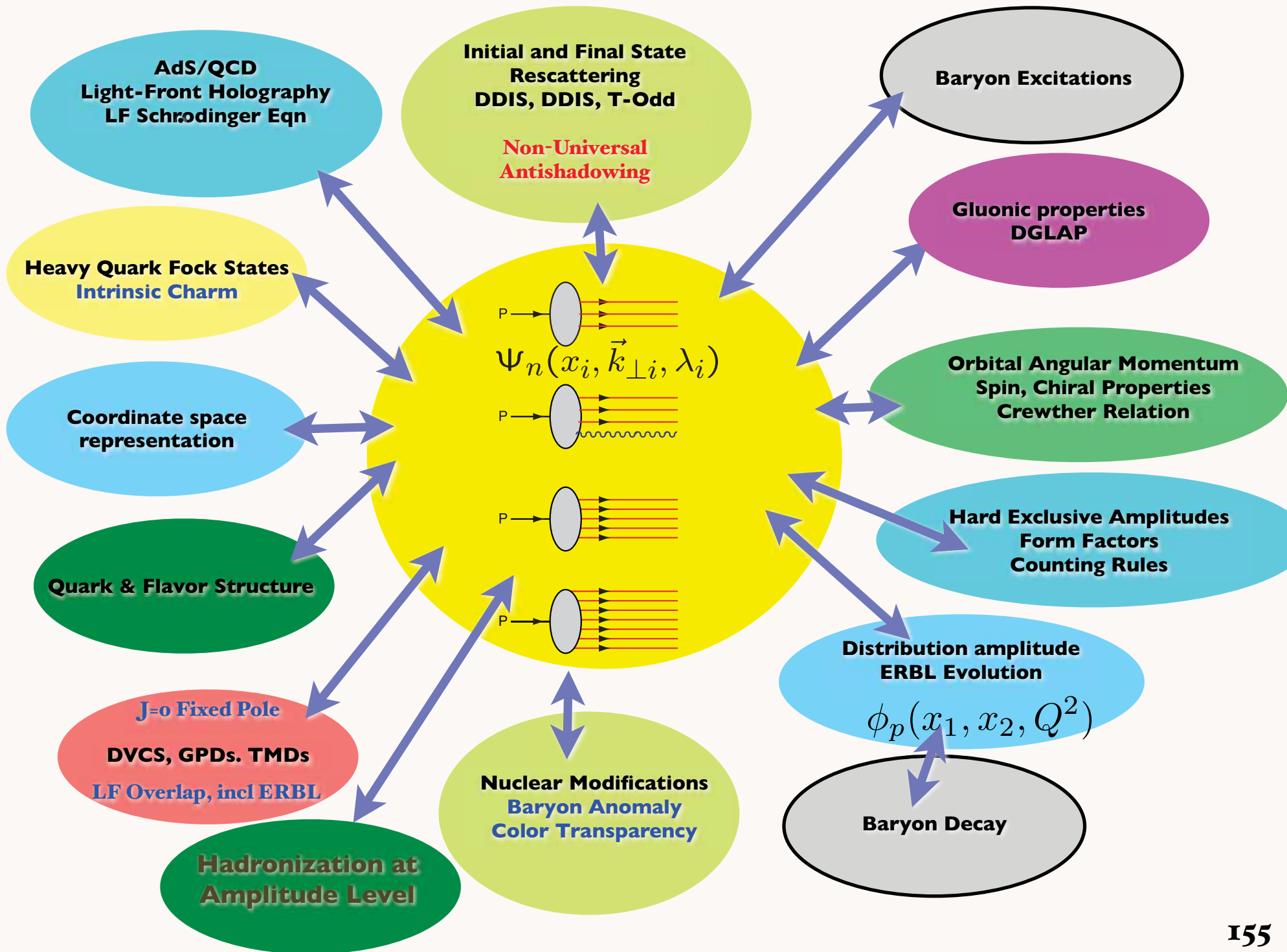
*Invariant under boosts. Independent of  $P^{\mu}$*

$$H_{LF}^{QCD} |\psi\rangle = M^2 |\psi\rangle$$

*Direct connection to QCD Lagrangian*

*Remarkable new insights from AdS/CFT,  
the duality between conformal field theory  
and Anti-de Sitter Space*

# QCD and the LF Hadron Wavefunctions



# *Goal: an analytic first approximation to QCD*

- **As Simple as Schrödinger Theory in Atomic Physics**
- **Relativistic, Frame-Independent, Color-Confining**
- **QCD Coupling at all scales**
- **Hadron Spectroscopy**
- **Light-Front Wavefunctions**
- **Form Factors, Hadronic Observables, Constituent Counting Rules**
- **Insight into QCD Condensates**
- **Systematically improvable**

**de Teramond, Deur, Shrock, Roberts, Tandy**



# Light-Front QCD

## Heisenberg Matrix Formulation

Physical gauge:  $A^+ = 0$

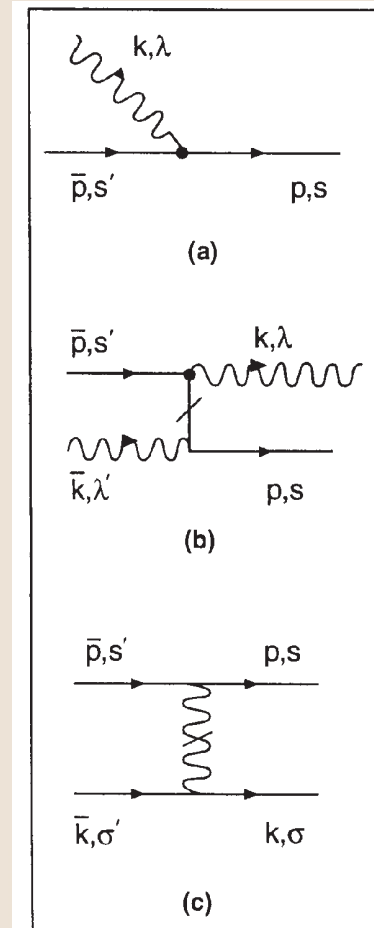
$$L^{QCD} \rightarrow H_{LF}^{QCD}$$

$$H_{LF}^{QCD} = \sum_i \left[ \frac{m^2 + k_{\perp}^2}{x} \right]_i + H_{LF}^{int}$$

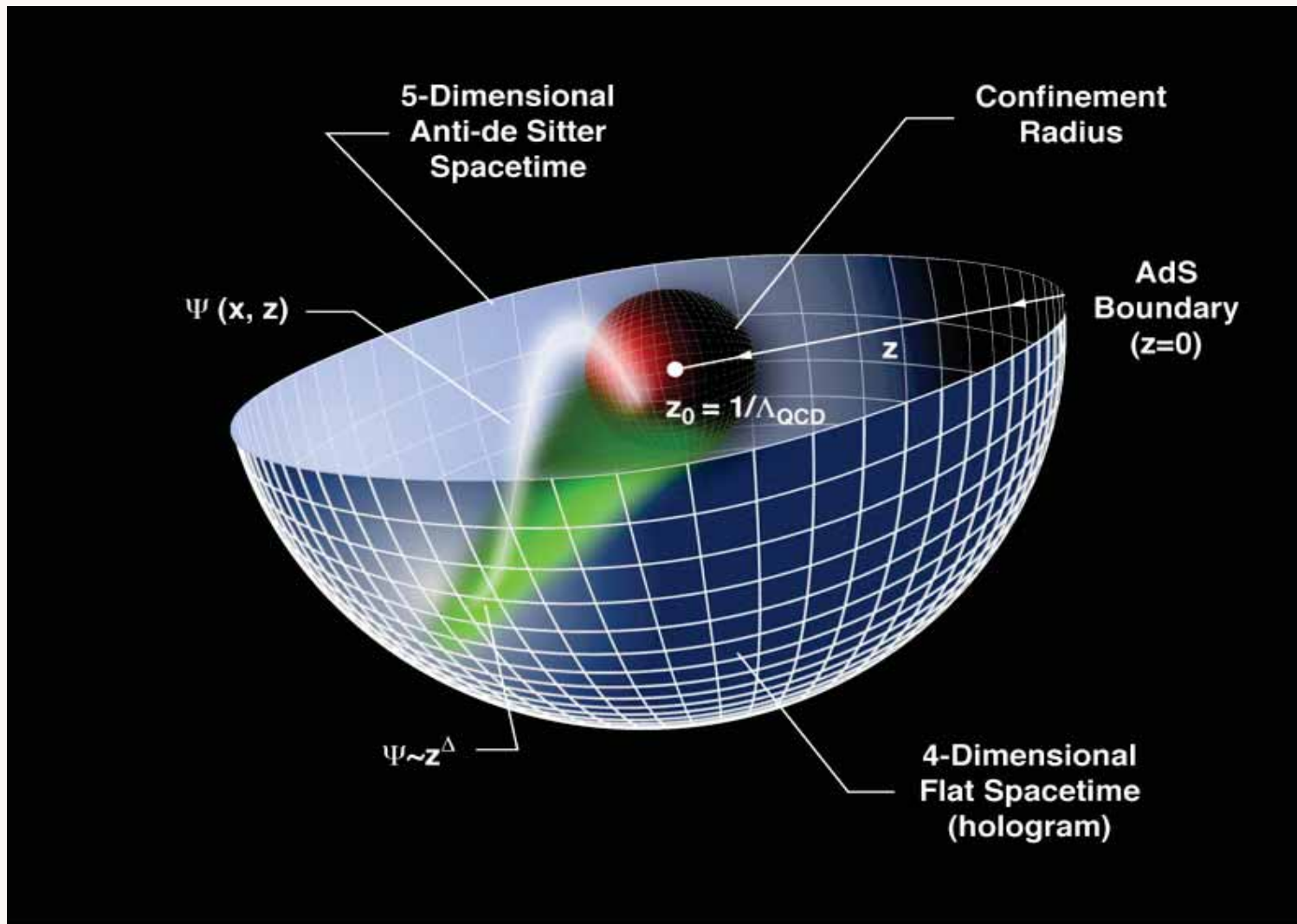
$H_{LF}^{int}$ : Matrix in Fock Space

$$H_{LF}^{QCD} |\Psi_h\rangle = \mathcal{M}_h^2 |\Psi_h\rangle$$

Eigenvalues and Eigensolutions give Hadron Spectrum and Light-Front wavefunctions



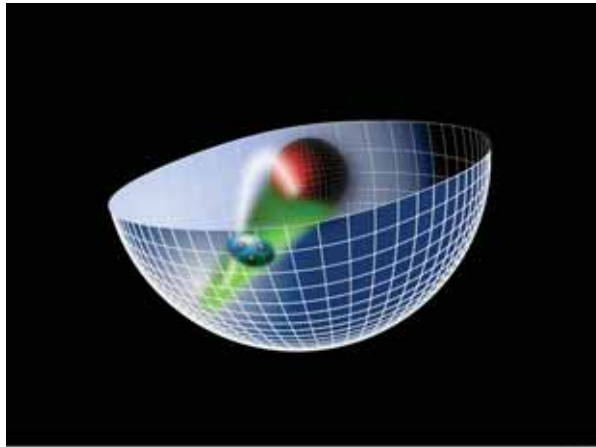
# Applications of AdS/CFT to QCD



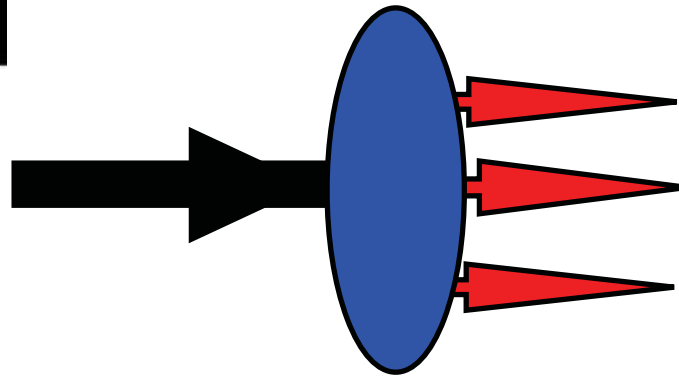
*Changes in physical length scale mapped to evolution in the 5th dimension  $z$*

**in collaboration with Guy de Teramond**

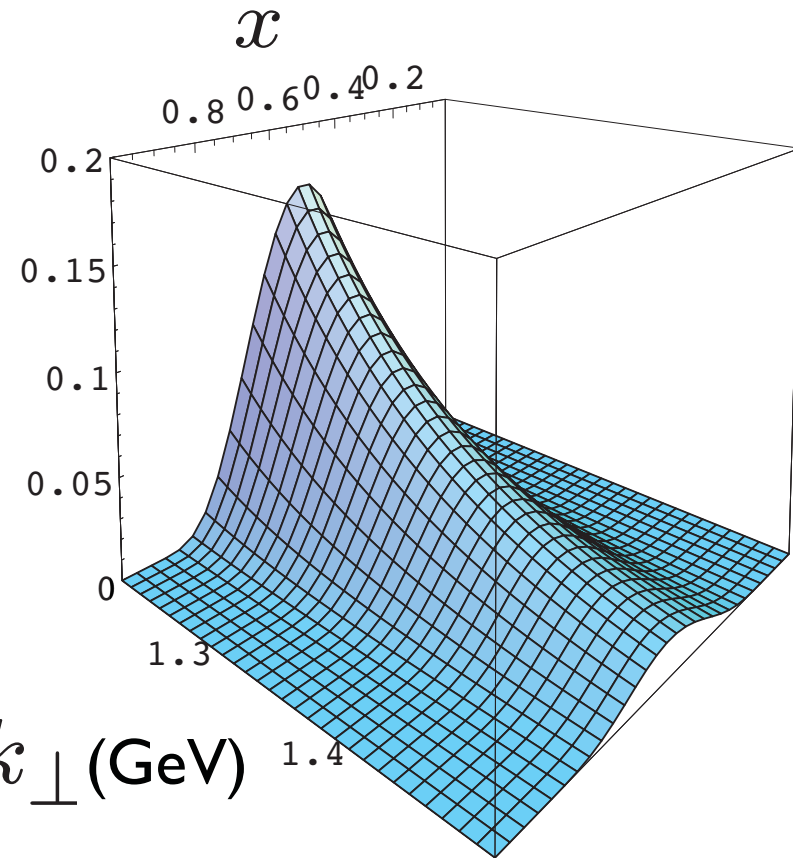
$$\phi(z)$$



- *Light-Front Holography*



$$\Psi_n(x_i, \vec{k}_{\perp i}, \lambda_i)$$



- *Light Front Wavefunctions:*

Schrödinger Wavefunctions  
of Hadron Physics

String Theory



AdS/CFT

Mapping of Poincare' and Conformal  $SO(4,2)$  symmetries of 3+1 space to AdS5 space

Goal: First Approximant to QCD

Counting rules for Hard Exclusive Scattering  
Regge Trajectories

Conformal behavior at short distances  
+ Confinement at large distance

AdS/QCD

QCD at the Amplitude Level

Semi-Classical QCD / Wave Equations

Holography

Boost Invariant 3+1 Light-Front Wave Equations

$J=0, 1, 1/2, 3/2$  plus  $L$

Integrable!

Hadron Spectra, Wavefunctions, Dynamics

*LF(3+1)*

*AdS<sub>5</sub>*

$$\psi(x, \vec{b}_\perp)$$

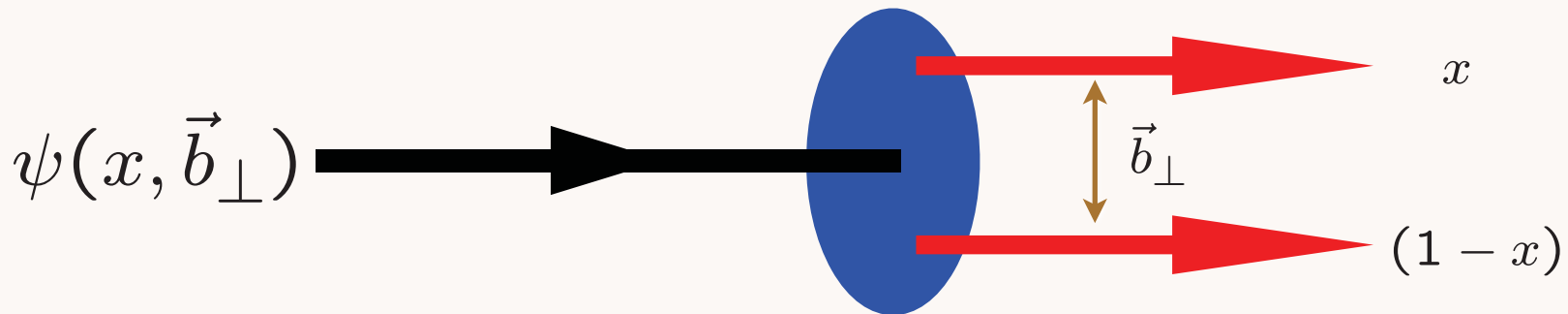


$$\phi(z)$$

$$\zeta = \sqrt{x(1-x)} \vec{b}_\perp^2$$



$$z$$



$$\psi(x, \zeta) = \sqrt{x(1-x)} \zeta^{-1/2} \phi(\zeta)$$

*Light-Front Holography: Unique mapping derived from equality of LF and AdS formula for current matrix elements*

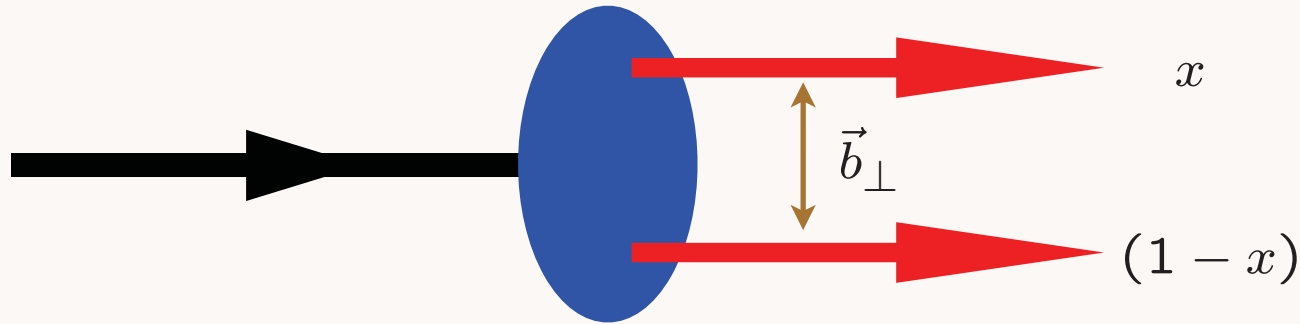
# Light-Front Holography: Map AdS/CFT to 3+1 LF Theory

Relativistic LF radial equation

Frame Independent

$$\left[ -\frac{d^2}{d\zeta^2} + \frac{1 - 4L^2}{4\zeta^2} + U(\zeta) \right] \phi(\zeta) = \mathcal{M}^2 \phi(\zeta)$$

$$\zeta^2 = x(1-x)b_{\perp}^2.$$



G. de Teramond, sjb

$$U(\zeta) = \kappa^4 \zeta^2$$

*soft wall  
confining potential:*

# Light-Front Holography: Map AdS/CFT to 3+1 LF Theory

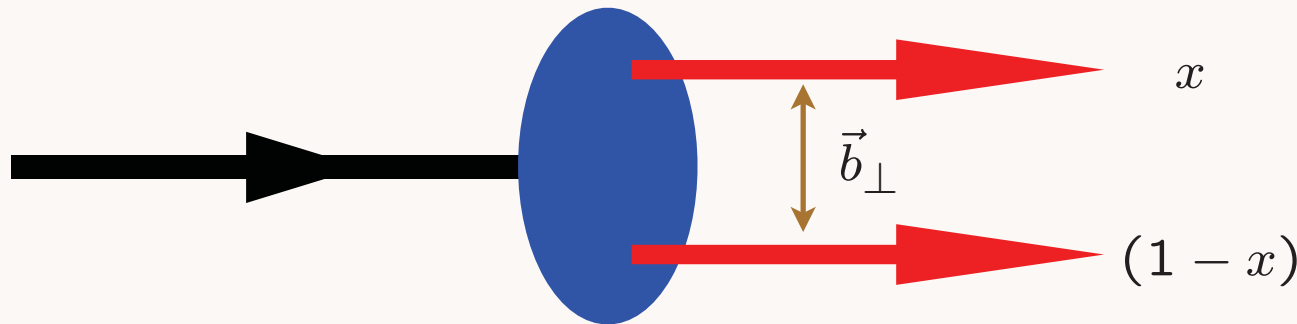
Relativistic LF radial equation

Frame Independent

$$\left[ -\frac{d^2}{d\zeta^2} + V(\zeta) \right] \phi(\zeta) = \mathcal{M}^2 \phi(\zeta)$$

$$\zeta^2 = x(1-x)b_{\perp}^2.$$

G. de Teramond, sjb



Effective conformal potential:

$$V(\zeta) = -\frac{1 - 4L^2}{4\zeta^2}$$

From LFKE

$$+ \kappa^4 \zeta^2$$

confining potential:

$$H_{QED}$$

*QED atoms: positronium  
and muonium*

$$(H_0 + H_{int}) |\Psi\rangle = E |\Psi\rangle$$

*Coupled Fock states*

$$\left[ -\frac{\Delta^2}{2m_{\text{red}}} + V_{\text{eff}}(\vec{S}, \vec{r}) \right] \psi(\vec{r}) = E \psi(\vec{r})$$

*Effective two-particle equation*

**Includes Lamb Shift, quantum corrections**

$$\left[ -\frac{1}{2m_{\text{red}}} \frac{d^2}{dr^2} + \frac{1}{2m_{\text{red}}} \frac{l(l+1)}{r^2} + V_{\text{eff}}(r, S, l) \right] \psi(r) = E \psi(r)$$

*Spherical Basis  $r, \theta, \phi$*

$$V_{\text{eff}} \rightarrow V_C(r) = -\frac{\alpha}{r}$$

*Coulomb potential*

**Bohr Spectrum**

*Semiclassical first approximation to QED*



$$H_{QCD}^{LF}$$

QCD Meson Spectrum

$$(H_{LF}^0 + H_{LF}^I) |\Psi\rangle = M^2 |\Psi\rangle$$

Coupled Fock states

$$\left[ \frac{\vec{k}_\perp^2 + m^2}{x(1-x)} + V_{\text{eff}}^{LF} \right] \psi_{LF}(x, \vec{k}_\perp) = M^2 \psi_{LF}(x, \vec{k}_\perp)$$

Effective two-particle equation

$$\zeta^2 = x(1-x)b_\perp^2$$

$$\left[ -\frac{d^2}{d\zeta^2} + \frac{-1 + 4L^2}{\zeta^2} + U(\zeta, S, L) \right] \psi_{LF}(\zeta) = M^2 \psi_{LF}(\zeta)$$

Azimuthal Basis  $\zeta, \phi$

$$U(\zeta, S, L) = \kappa^2 \zeta^2 + \kappa^2 (L + S - 1/2)$$

Semiclassical first approximation to QCD

Confining AdS/QCD potential

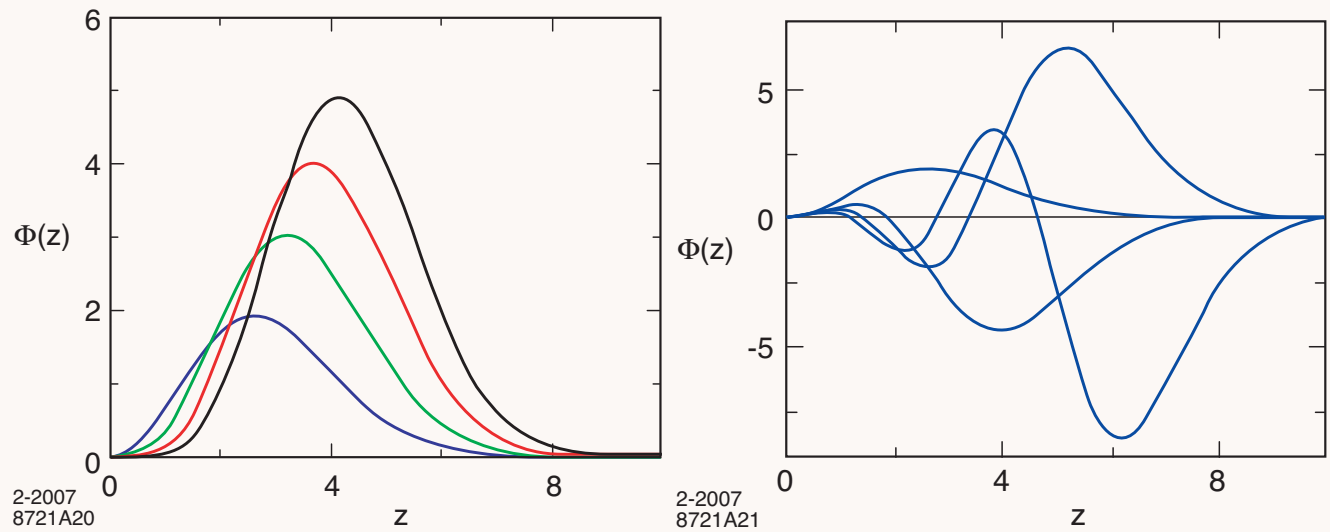
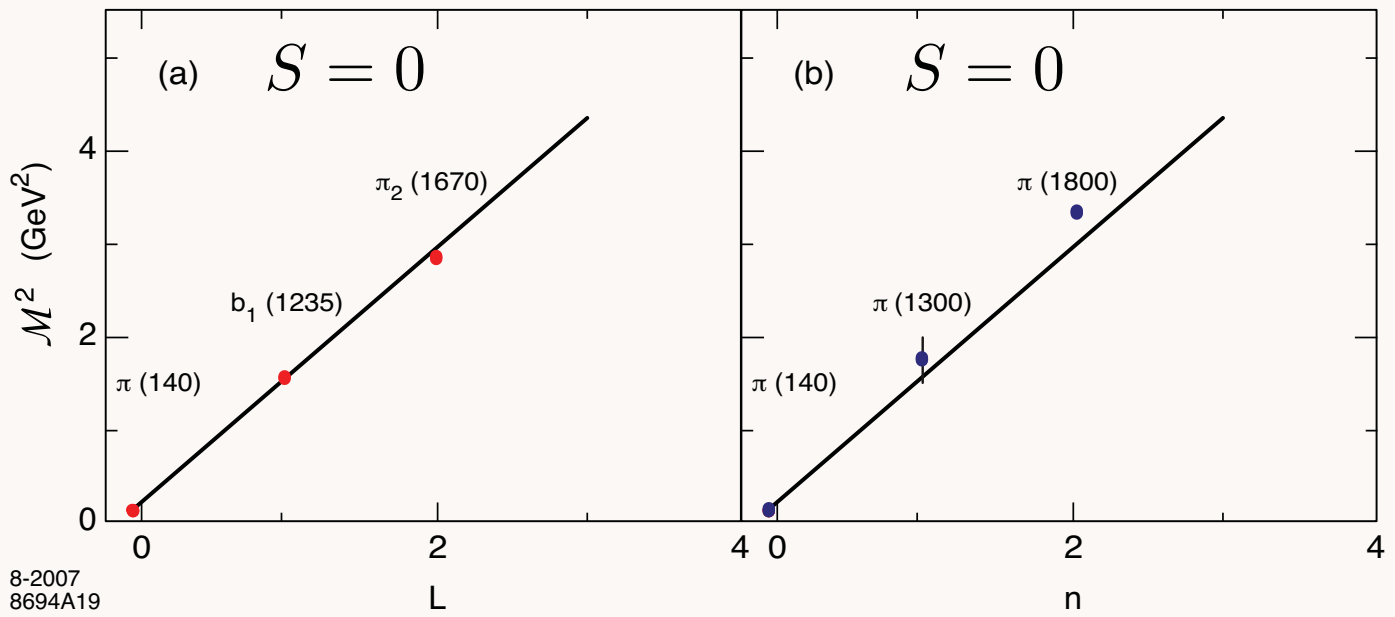


Fig: Orbital and radial AdS modes in the soft wall model for  $\kappa = 0.6 \text{ GeV}$ .

*Soft Wall Model*



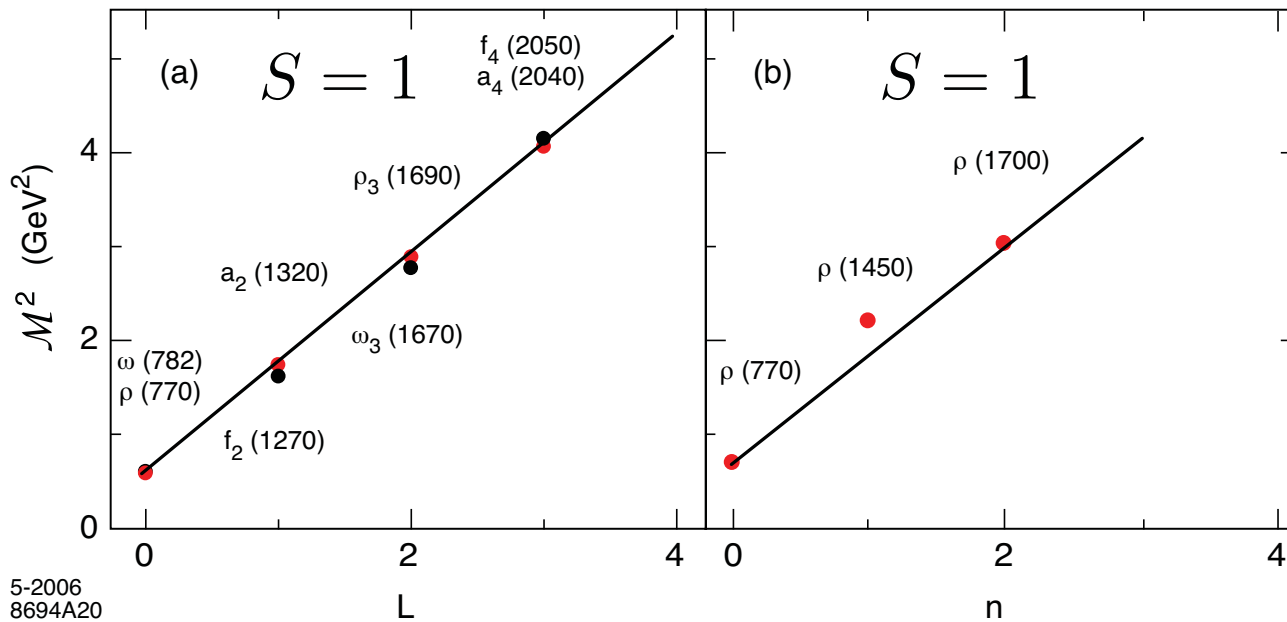
Light meson orbital (a) and radial (b) spectrum for  $\kappa = 0.6 \text{ GeV}$ .

- Effective LF Schrödinger wave equation

$$\left[ -\frac{d^2}{dz^2} - \frac{1 - 4L^2}{4z^2} + \kappa^4 z^2 + 2\kappa^2(L + S - 1) \right] \phi_S(z) = \mathcal{M}^2 \phi_S(z)$$

with eigenvalues  $\mathcal{M}^2 = 2\kappa^2(2n + 2L + S)$ . *Same slope in n and L*

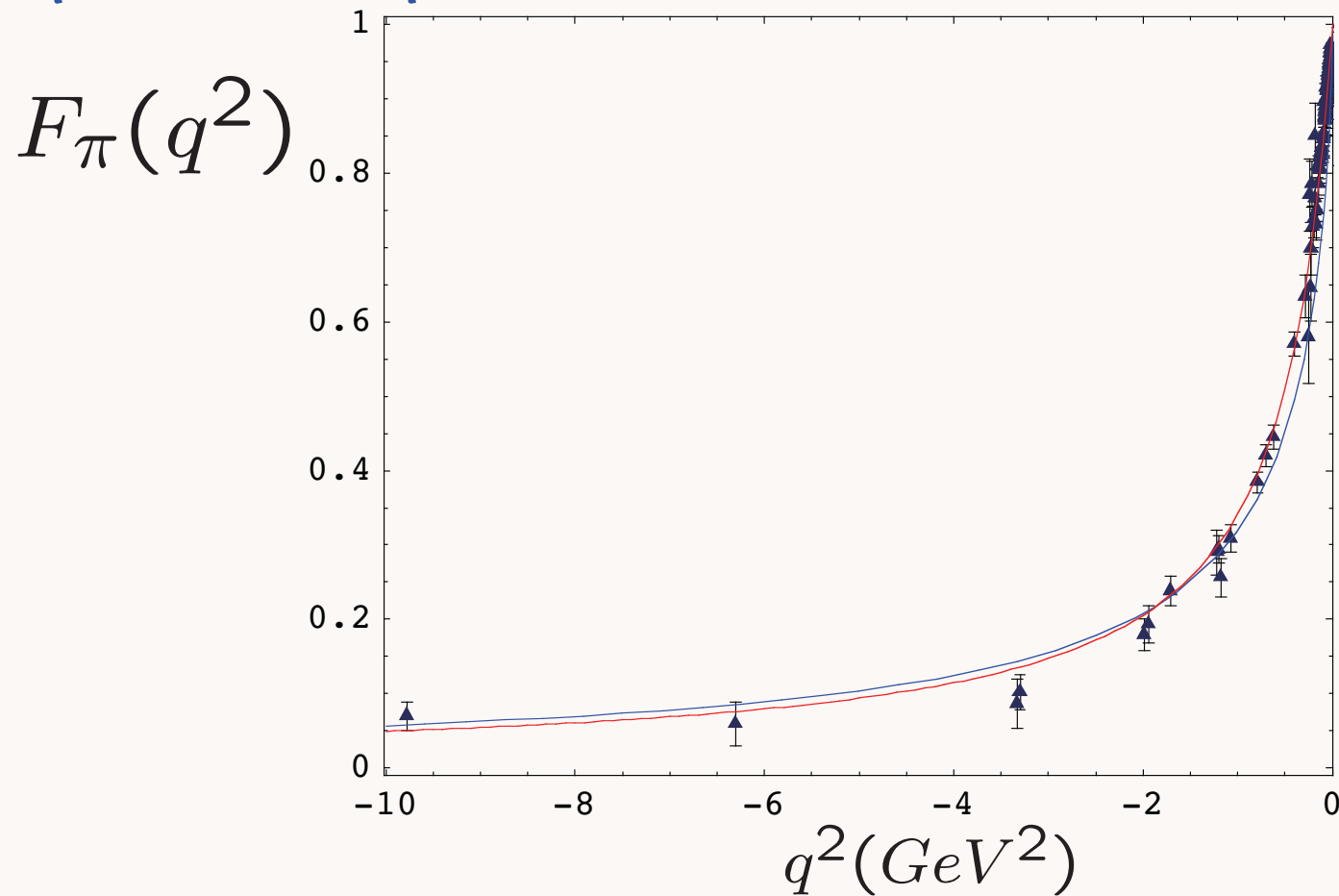
- Compare with Nambu string result (rotating flux tube):  $M_n^2(L) = 2\pi\sigma (n + L + 1/2)$ .



Vector mesons orbital (a) and radial (b) spectrum for  $\kappa = 0.54$  GeV.

- Glueballs in the bottom-up approach: (HW) Boschi-Filho, Braga and Carrion (2005); (SW) Colangelo, De Fazio, Jugeau and Nicotri( 2007).

# Spacelike pion form factor from AdS/CFT



Data Compilation  
Baldini, Kloe and Volmer

— Soft Wall: Harmonic Oscillator Confinement

— Hard Wall: Truncated Space Confinement

*One parameter - set by pion decay constant*

de Teramond, sjb

See also: Radyushkin

# Non-Conformal Extension of Algebraic Structure (Soft Wall Model)

- We write the Dirac equation

$$(\alpha\Pi(\zeta) - \mathcal{M})\psi(\zeta) = 0,$$

in terms of the matrix-valued operator  $\Pi$

$$\nu = L + 1$$

$$\Pi_\nu(\zeta) = -i \left( \frac{d}{d\zeta} - \frac{\nu + \frac{1}{2}}{\zeta} \gamma_5 - \kappa^2 \zeta \gamma_5 \right),$$

and its adjoint  $\Pi^\dagger$ , with commutation relations

$$\left[ \Pi_\nu(\zeta), \Pi_\nu^\dagger(\zeta) \right] = \left( \frac{2\nu + 1}{\zeta^2} - 2\kappa^2 \right) \gamma_5.$$

- Solutions to the Dirac equation

$$\psi_+(\zeta) \sim z^{\frac{1}{2}+\nu} e^{-\kappa^2 \zeta^2 / 2} L_n^\nu(\kappa^2 \zeta^2),$$

$$\psi_-(\zeta) \sim z^{\frac{3}{2}+\nu} e^{-\kappa^2 \zeta^2 / 2} L_n^{\nu+1}(\kappa^2 \zeta^2).$$

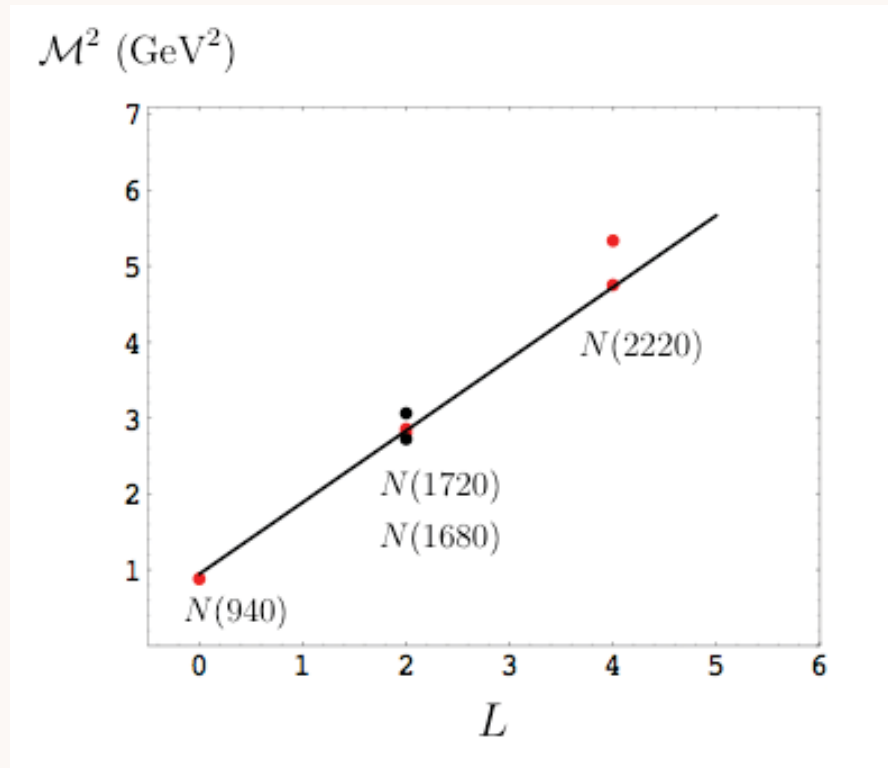
- Eigenvalues

$$\mathcal{M}^2 = 4\kappa^2(n + \nu + 1).$$

- Baryon: twist-dimension  $3 + L$  ( $\nu = L + 1$ )

$$\mathcal{O}_{3+L} = \psi D_{\{\ell_1 \dots D_{\ell_q} \psi D_{\ell_{q+1}} \dots D_{\ell_m}\}} \psi, \quad L = \sum_{i=1}^m \ell_i.$$

$$\mathcal{M}^2 = 4\kappa^2(n + L + 1).$$

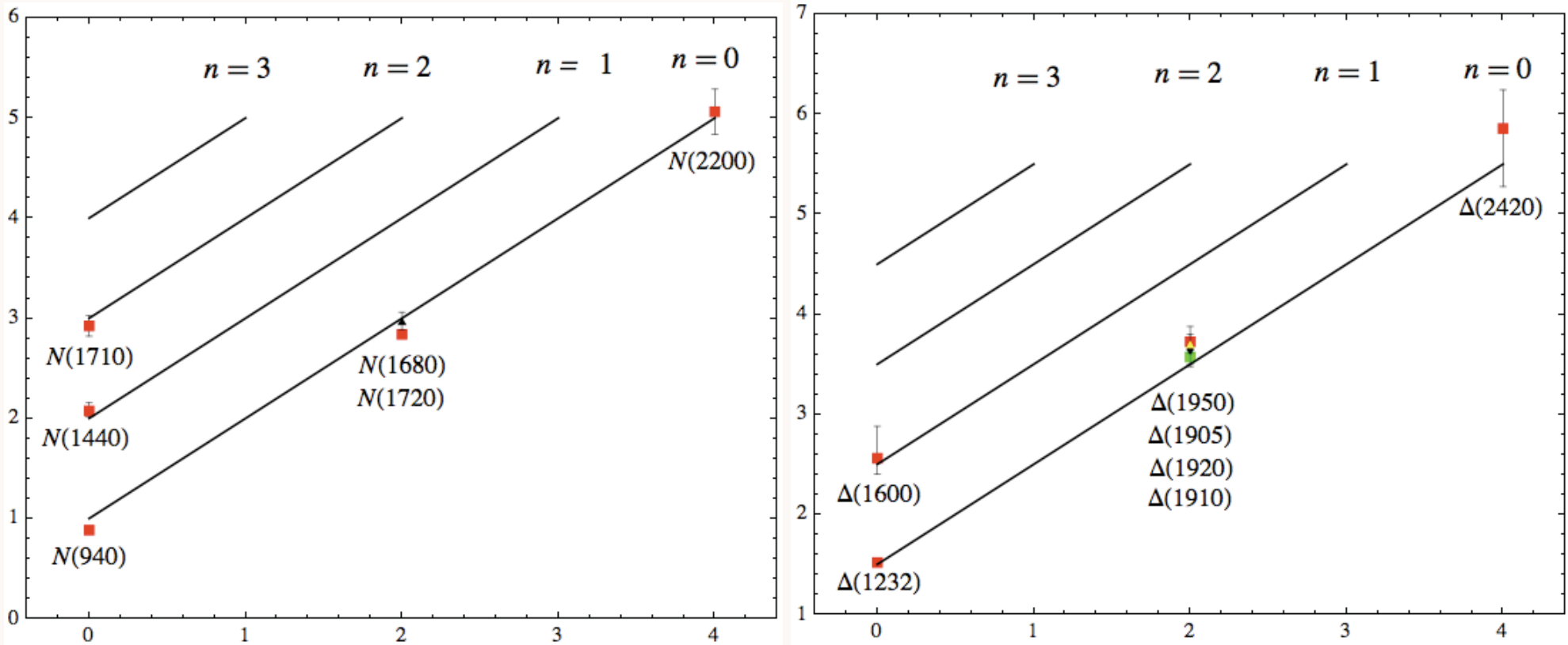


Proton Regge Trajectory  $\kappa = 0.49\text{GeV}$

•  $\Delta$  spectrum identical to Forkel and Klempt, Phys. Lett. B 679, 77 (2009)

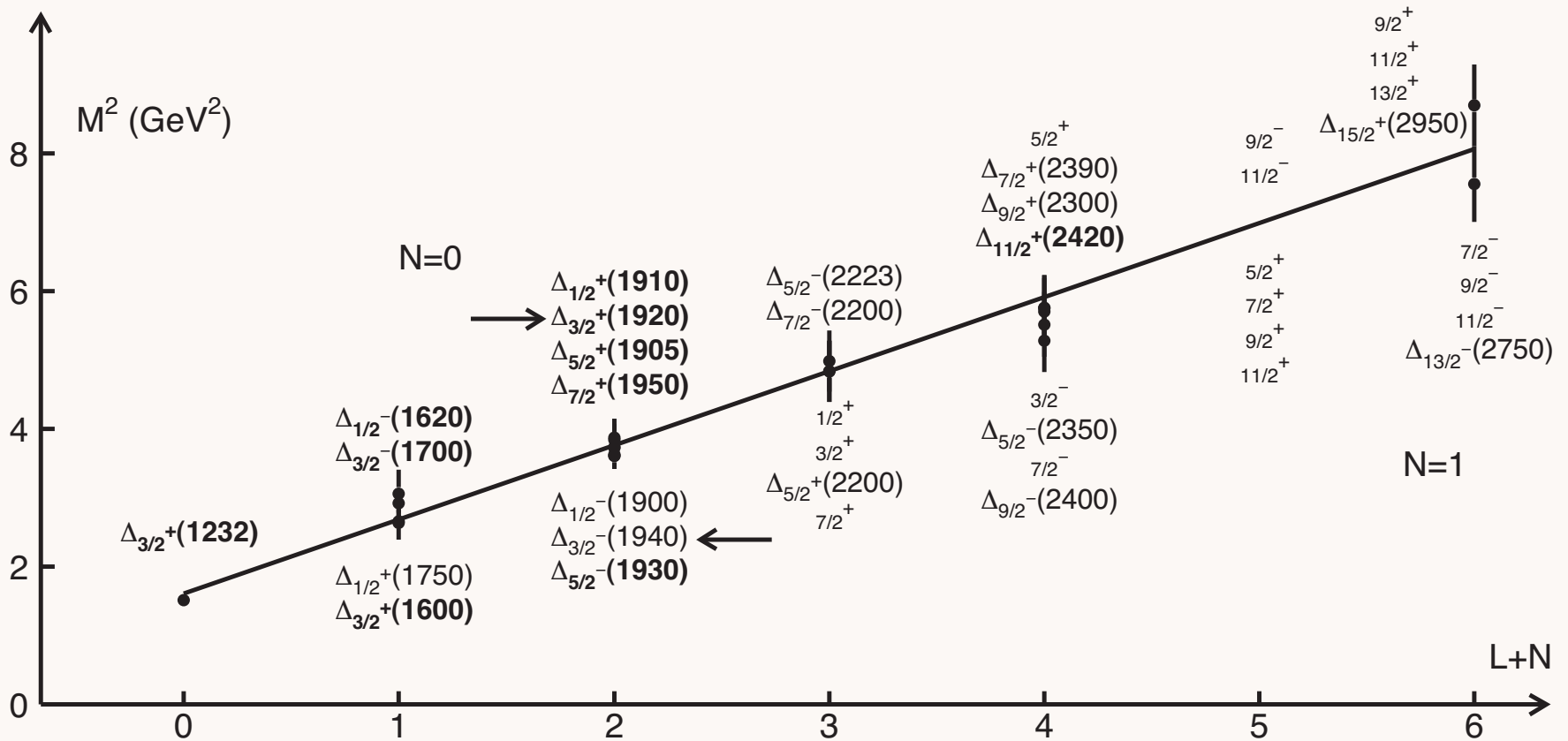
$4\kappa^2$  for  $\Delta n = 1$   
 $4\kappa^2$  for  $\Delta L = 1$   
 $2\kappa^2$  for  $\Delta S = 1$

$\mathcal{M}^2$



$L$

Parent and daughter 56 Regge trajectories for the  $N$  and  $\Delta$  baryon families for  $\kappa = 0.5$  GeV



E. Klempt *et al.*:  $\Delta^*$  resonances, quark models, chiral symmetry and AdS/QCD

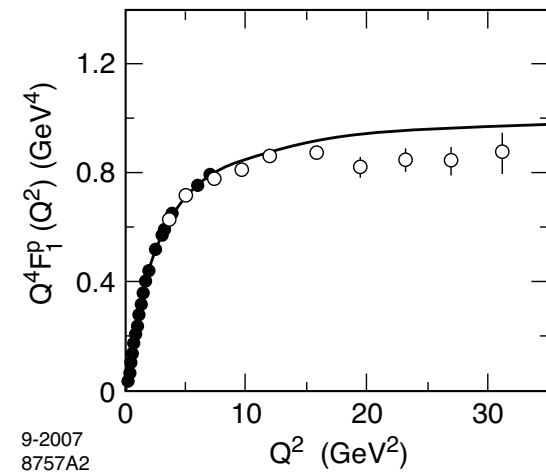
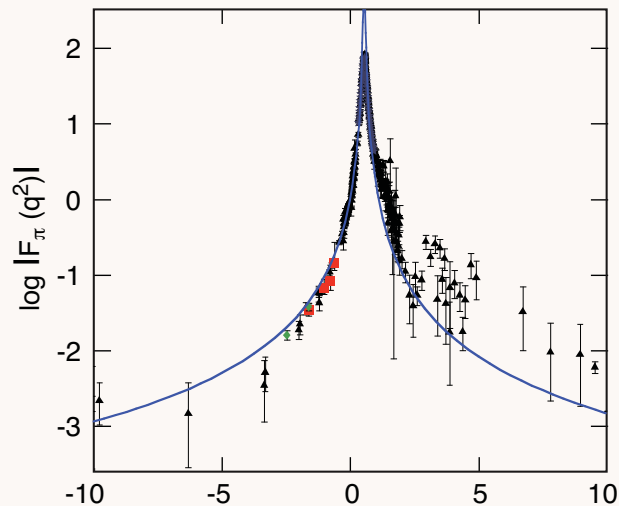
H. Forkel, M. Beyer and T. Frederico, JHEP **0707** (2007) 077.

H. Forkel, M. Beyer and T. Frederico, Int. J. Mod. Phys. E **16** (2007) 2794.



## Other Applications of Light-Front Holography

- Light baryon spectrum
- Light meson spectrum
- Nucleon form-factors: space-like region
- Pion form-factors: space and time-like regions
- Gravitational form factors of composite hadrons
- $n$ -parton holographic mapping
- Heavy flavor mesons



9-2007  
8757A2

hep-th/0501022  
hep-ph/0602252  
arXiv:0707.3859  
arXiv:0802.0514  
arXiv:0804.0452

## Space-Like Dirac Proton Form Factor

- Consider the spin non-flip form factors

$$F_+(Q^2) = g_+ \int d\zeta J(Q, \zeta) |\psi_+(\zeta)|^2,$$

$$F_-(Q^2) = g_- \int d\zeta J(Q, \zeta) |\psi_-(\zeta)|^2,$$

where the effective charges  $g_+$  and  $g_-$  are determined from the spin-flavor structure of the theory.

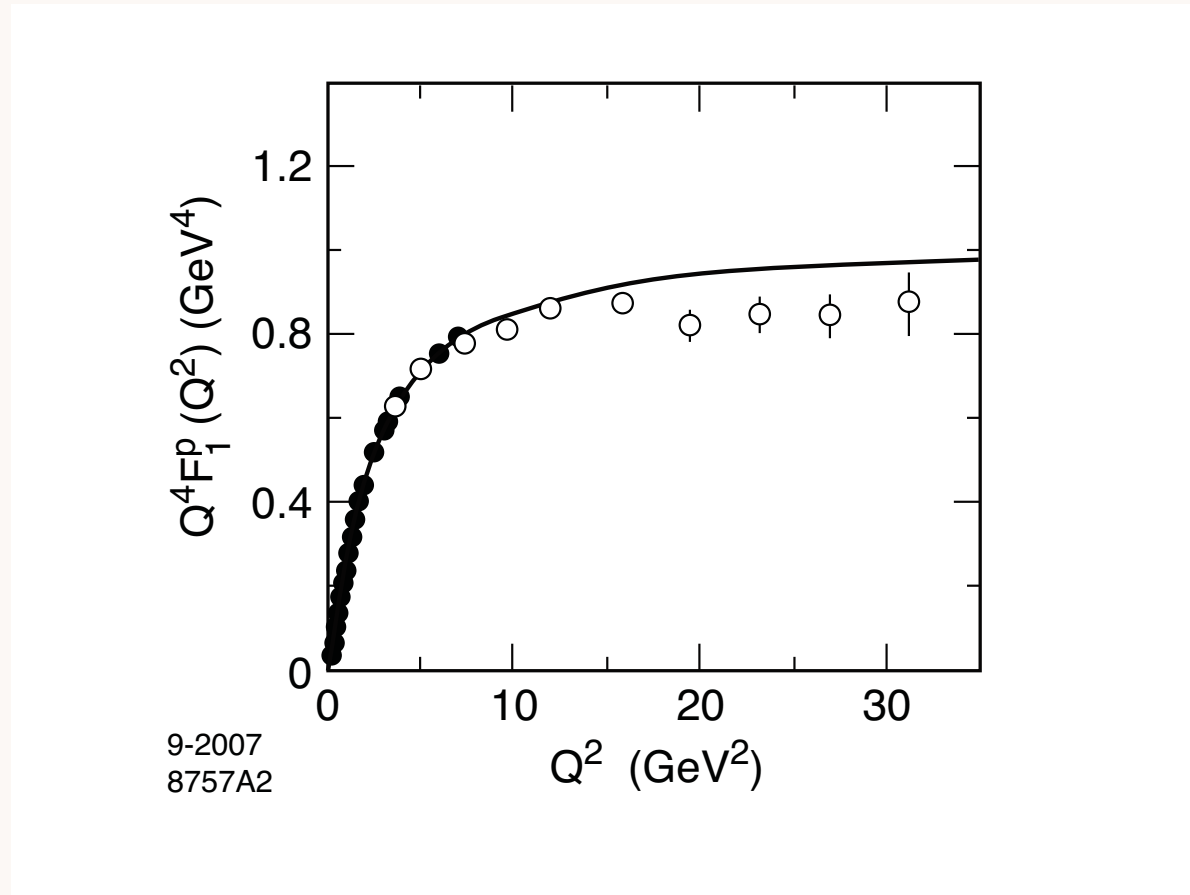
- Choose the struck quark to have  $S^z = +1/2$ . The two AdS solutions  $\psi_+(\zeta)$  and  $\psi_-(\zeta)$  correspond to nucleons with  $J^z = +1/2$  and  $-1/2$ .
- For  $SU(6)$  spin-flavor symmetry

$$F_1^p(Q^2) = \int d\zeta J(Q, \zeta) |\psi_+(\zeta)|^2,$$

$$F_1^n(Q^2) = -\frac{1}{3} \int d\zeta J(Q, \zeta) [|\psi_+(\zeta)|^2 - |\psi_-(\zeta)|^2],$$

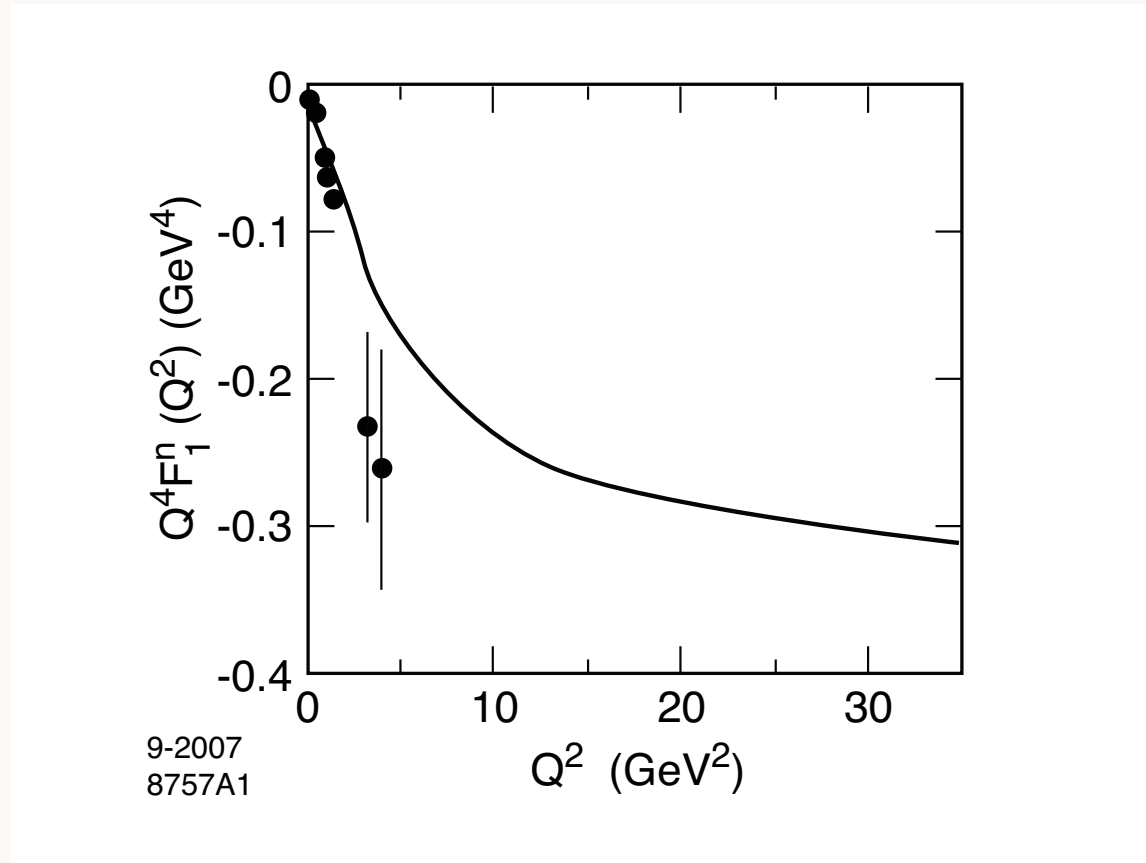
where  $F_1^p(0) = 1$ ,  $F_1^n(0) = 0$ .

- Scaling behavior for large  $Q^2$ :  $Q^4 F_1^p(Q^2) \rightarrow \text{constant}$  Proton  $\tau = 3$



SW model predictions for  $\kappa = 0.424$  GeV. Data analysis from: M. Diehl *et al.* Eur. Phys. J. C **39**, 1 (2005).

- Scaling behavior for large  $Q^2$ :  $Q^4 F_1^n(Q^2) \rightarrow \text{constant}$  Neutron  $\tau = 3$



SW model predictions for  $\kappa = 0.424$  GeV. Data analysis from M. Diehl *et al.* Eur. Phys. J. C **39**, 1 (2005).