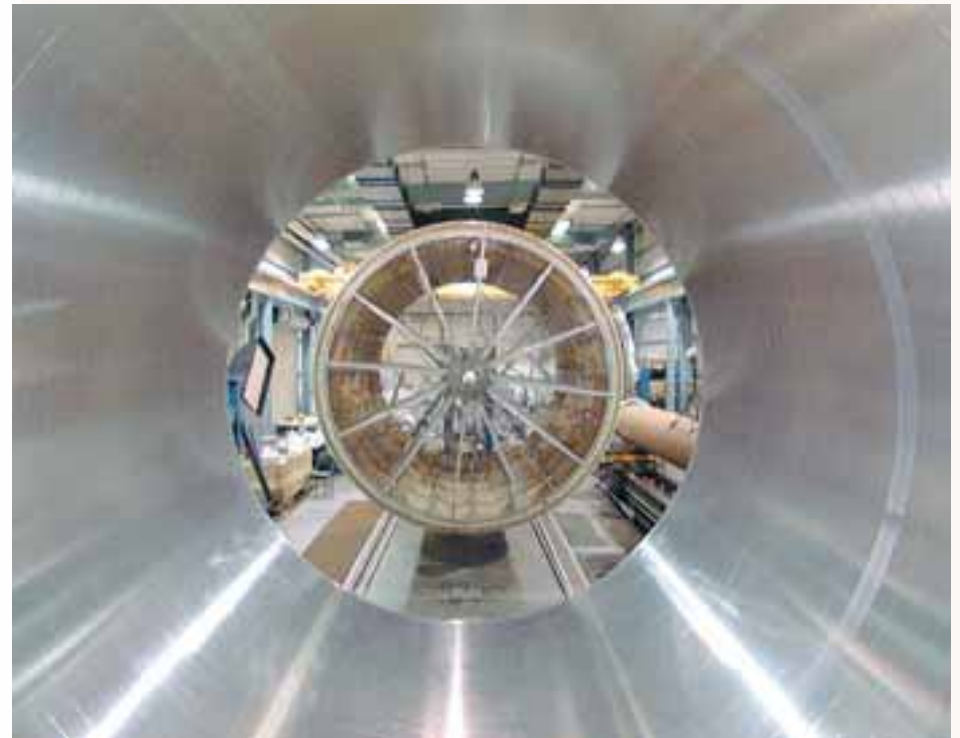


# *Novel QCD Phenomena*

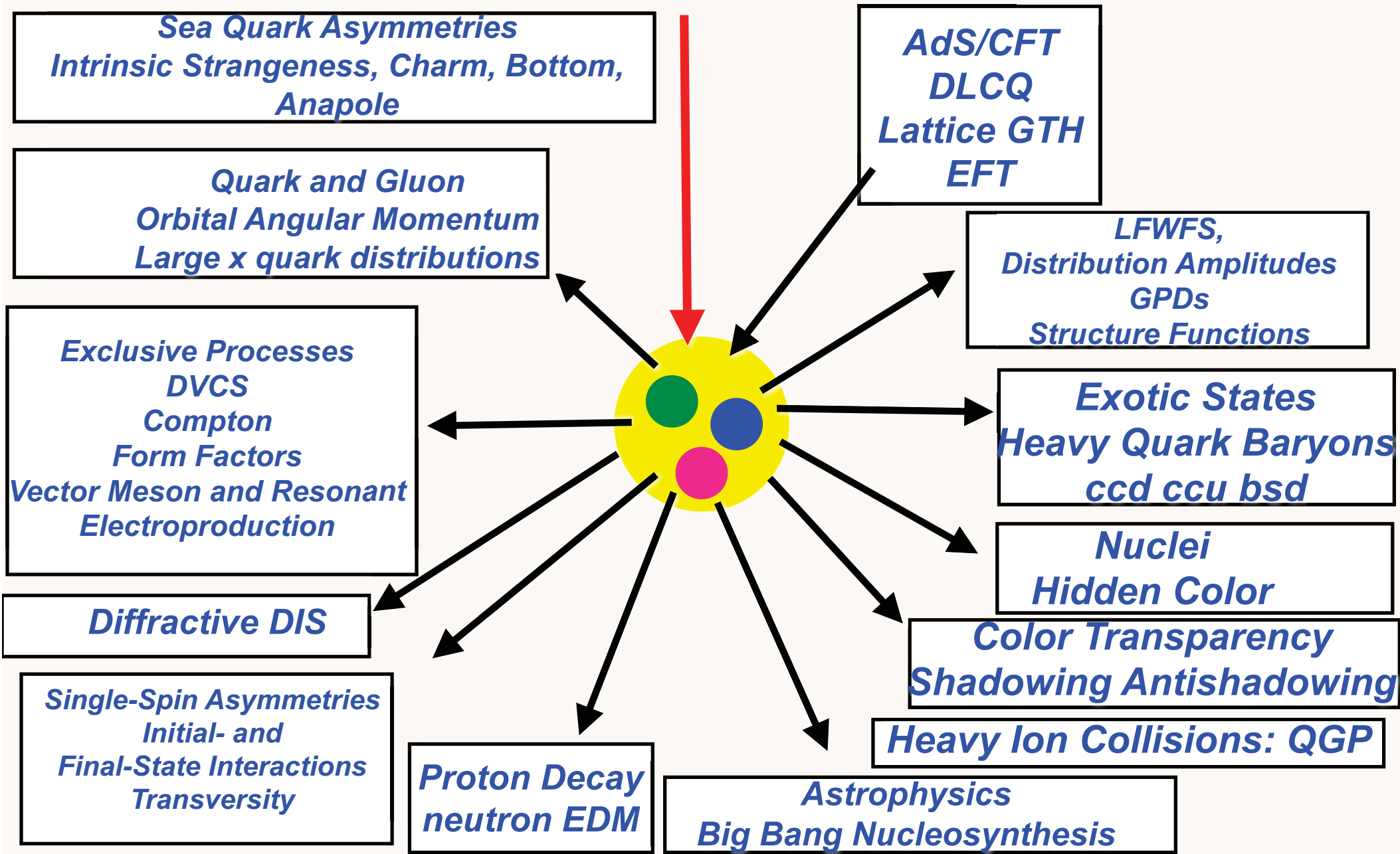
**Stan Brodsky, SLAC**

**January 8, 2008**

**BNL**

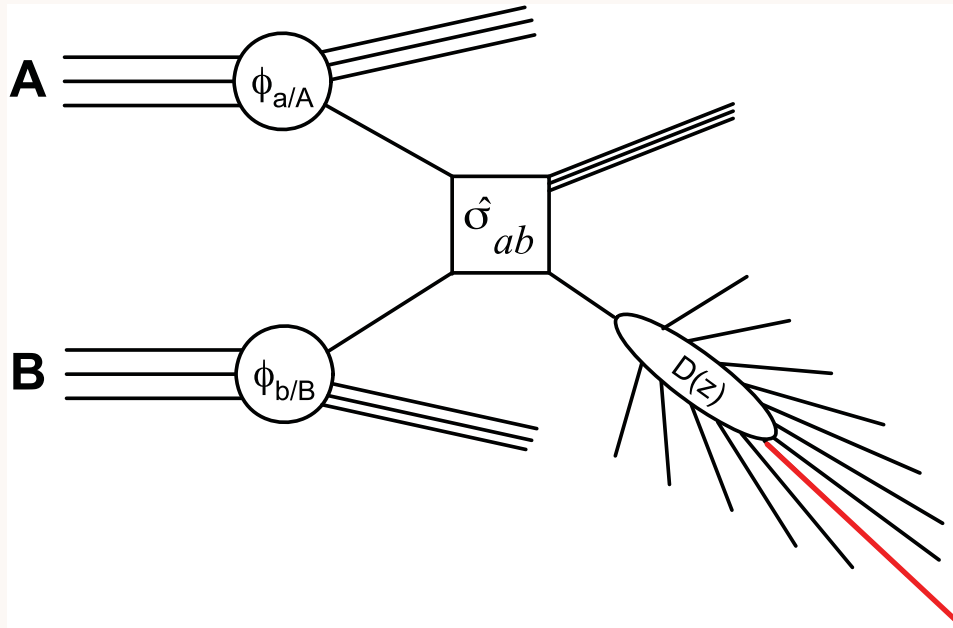


# QCD Lagrangian



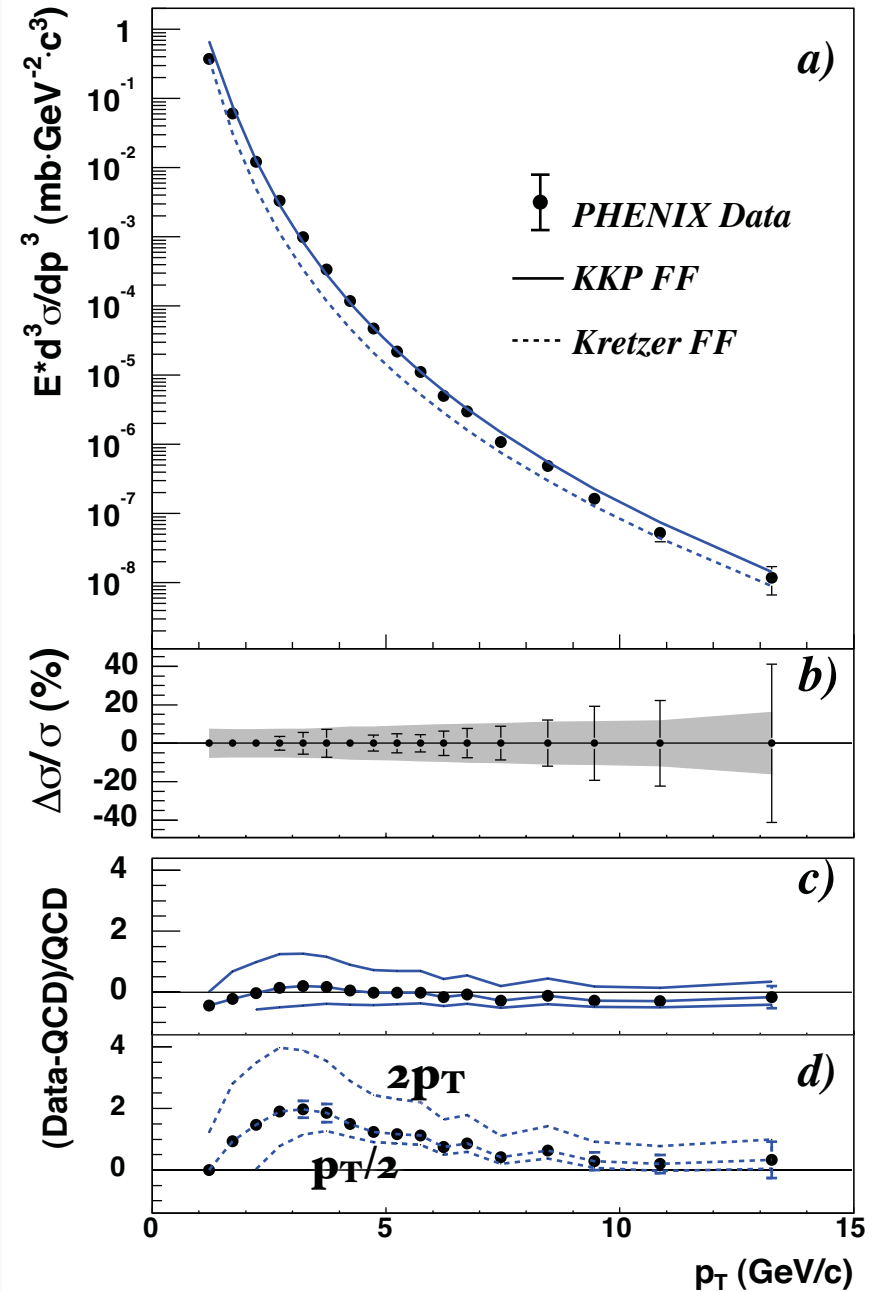
$$E \frac{d\sigma}{d^3p} (pp \rightarrow \pi^0 X)$$

$$\sqrt{s} = 200 \text{ GeV}$$



**NLO pQCD predictions**  
**Vogelsang**

**Assumes equal factorization**  
**and renormalization scales:**  
 $p_T/2, p_T, 2p_T$



# Challenging Conventional Wisdom

- ➔ • **Renormalization scale is arbitrary**
- **Initial and final-state interactions are power suppressed in a hard QCD reaction**
- **Heavy quark distributions derive exclusively from gluon splitting**
- **Nuclear parton distributions are universal**
- **Hadroproduction at large transverse momentum derives exclusively from 2 to 2 scattering subprocesses**

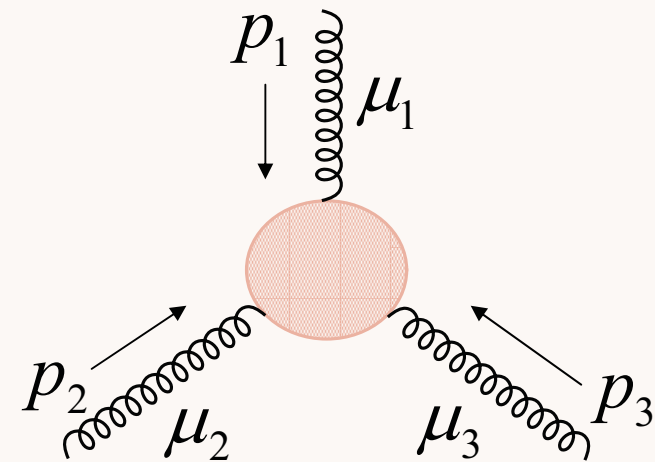
# The Renormalization Scale Problem

$$\rho(Q^2) = C_0 + C_1\alpha_s(\mu_R) + C_2\alpha_s^2(\mu_R) + \dots$$

$$\mu_R^2 = CQ^2$$

*Is there a way to set the renormalization scale  $\mu_R$ ?*

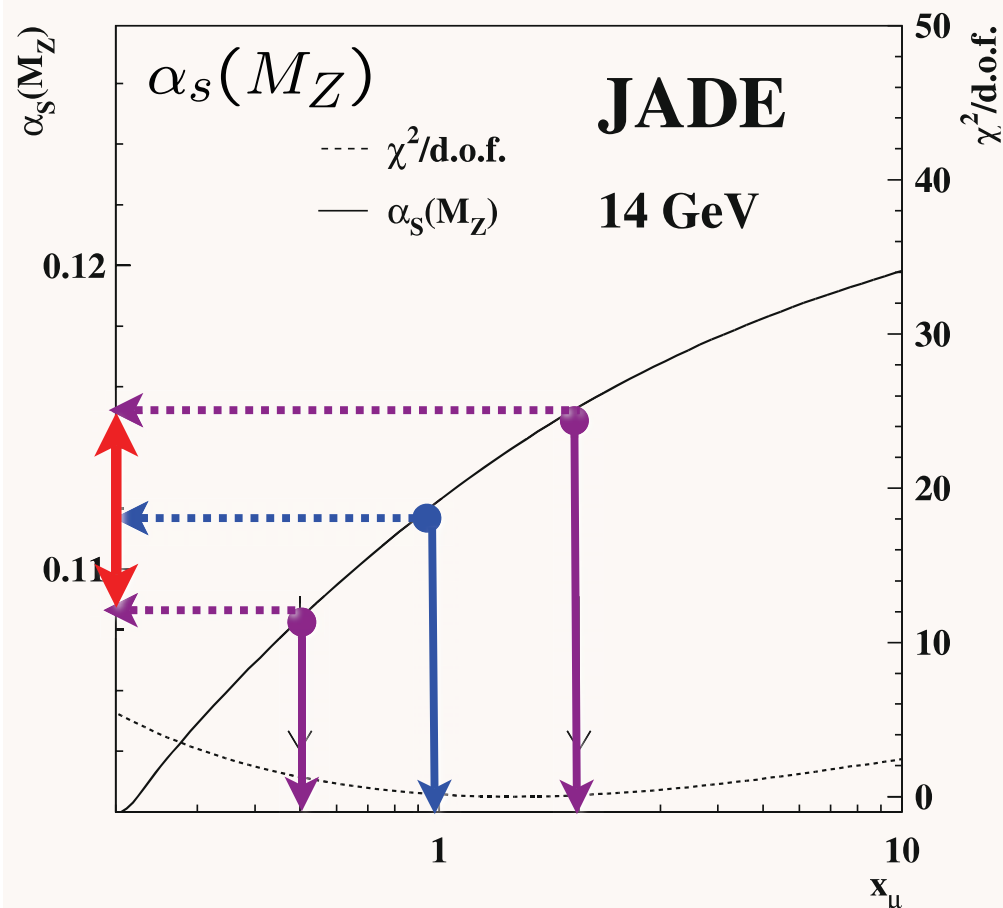
*What happens if there are multiple physical scales?*



# Measurement of the strong coupling $\alpha_s$ from the four-jet rate in $e^+e^-$ annihilation using JADE data

J. Schieck<sup>1,a</sup>, S. Bethke<sup>1</sup>, O. Biebel<sup>2</sup>, S. Kluth<sup>1</sup>, P.A.M. Fernández<sup>3</sup>, C. Pahl<sup>1</sup>,  
The JADE Collaboration<sup>b</sup>

Eur. Phys. J. C 48, 3–13 (2006)



$$x_\mu = \frac{\mu_R}{\sqrt{s}}$$

No PMS

$\alpha_s(M_{Z^0})$  and the  $\chi^2/\text{d.o.f.}$  of the fit to the four-jet rate as a function of the renormalization scale  $x_\mu$  for  $\sqrt{s} = 14$  GeV to 43.8 GeV. The arrows indicate the variation of the renormalization scale factor used for the determination of the systematic uncertainties

The theoretical uncertainty, associated with missing higher order terms in the theoretical prediction, is assessed by varying the renormalization scale factor  $x_\mu$ . The predictions of a complete QCD calculation would be independent of  $x_\mu$ , but a finite-order calculation such as that used here retains some dependence on  $x_\mu$ . The renormalization scale factor  $x_\mu$  is set to 0.5 and two. The larger deviation from the default value of  $\alpha_s$  is taken as systematic uncertainty.

# Conventional wisdom in QCD concerning scale setting

- Renormalization scale “unphysical”: No optimal physical scale
- Can ignore possibility of multiple physical scales
- Accuracy of PQCD prediction can be judged by taking arbitrary guess  $\mu_R = Q$  with an arbitrary range  $Q/2 < \mu_R < 2Q$
- Factorization scale should be taken equal to renormalization scale  $\mu_F = \mu_R$

**These assumptions are untrue in QED  
and thus they cannot be true for QCD**

# Electron-Electron Scattering in QED



$$\alpha(t) = \frac{\alpha(0)}{1 - \Pi(t)}$$

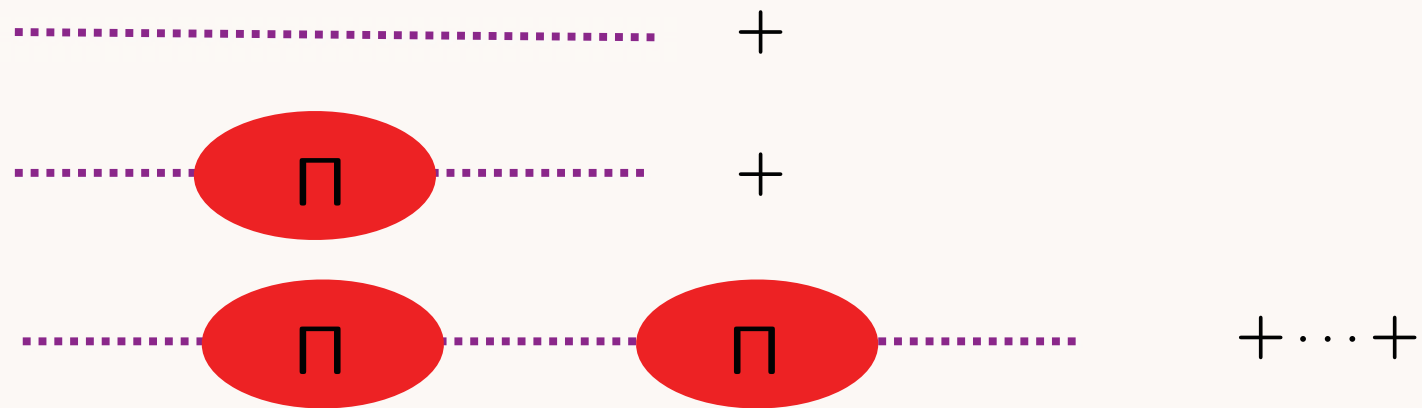
## Gell Mann-Low Effective Charge



# QED Effective Charge

$$\alpha(t) = \frac{\alpha(0)}{1 - \Pi(t)}$$

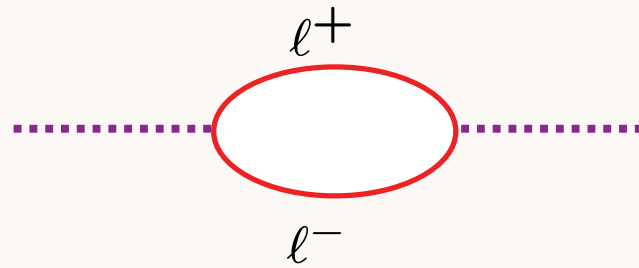
*All-orders lepton loop corrections to dressed photon propagator*



$$\alpha(t) = \frac{\alpha(t_0)}{1 - \Pi(t, t_0)} \quad \Pi(t, t_0) = \frac{\Pi(t) - \Pi(t_0)}{1 - \Pi(t_0)}$$

*Initial scale  $t_0$  is arbitrary -- Variation gives RGE Equations  
Physical renormalization scale  $t$  not arbitrary*

# QED One-Loop Vacuum Polarization



$$t = -Q^2 < 0$$

**(t spacelike)**

$$\Pi(Q^2) = \frac{\alpha(0)}{3\pi} \left[ \frac{5}{3} - \frac{4m^2}{Q^2} - \left(1 - \frac{2m^2}{Q^2}\right) \sqrt{1 + \frac{4m^2}{Q^2}} \log \frac{1 + \sqrt{1 + \frac{4m^2}{Q^2}}}{|1 - \sqrt{1 + \frac{4m^2}{Q^2}}|} \right]$$

**Analytically continue to timelike t: Complex**

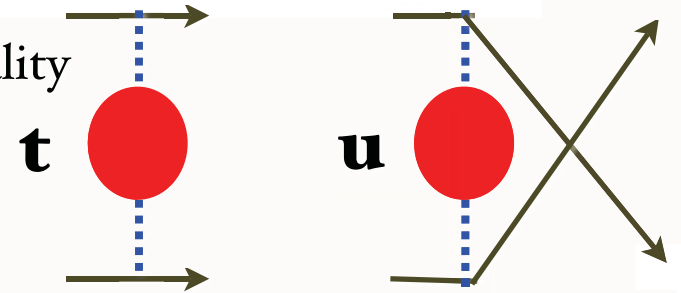
$$\Pi(Q^2) = \frac{\alpha(0)}{15\pi} \frac{Q^2}{m^2} \quad Q^2 \ll 4M^2 \quad \text{Serber-Uehling}$$

$$\Pi(Q^2) = \frac{\alpha(0)}{3\pi} \frac{\log Q^2}{m^2} \quad Q^2 \gg 4M^2 \quad \text{Landau Pole}$$

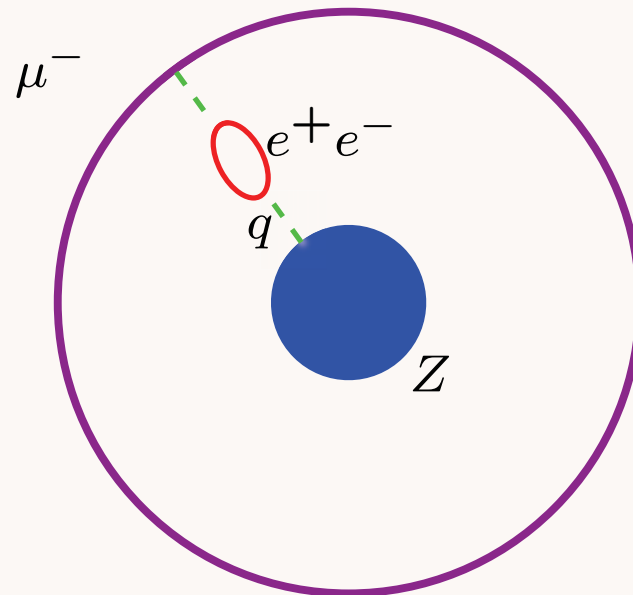
$$\beta = \frac{d\left(\frac{\alpha}{4\pi}\right)}{d \log Q^2} = \frac{4}{3} \left(\frac{\alpha}{4\pi}\right)^2 n_\ell > 0$$

# Electron-Electron Scattering in QED

- Two separate physical scales:  $t, u$  = photon virtuality
- Gauge Invariant. Dressed photon propagator
- Sums all vacuum polarization, non-zero beta terms into running coupling.
- If one chooses a different scale, one can sum an infinite number of graphs -- but always recover same result!
- Number of active leptons correctly set
- Analytic: reproduces correct behavior at lepton mass thresholds
- **No renormalization scale ambiguity!**



# Another Example in QED: Muonic Atoms



$$V(q^2) = -\frac{Z\alpha_{QED}(q^2)}{q^2}$$

$$\mu_R^2 \equiv q^2$$

$$\alpha_{QED}(q^2) = \frac{\alpha_{QED}(0)}{1-\Pi(q^2)}$$

**Scale is unique: Tested to ppm**

Gyulassy: Higher Order VP verified to 0.1% precision in  $\mu$  Pb

$\lim N_C \rightarrow 0$  at fixed  $\alpha = C_F \alpha_s, n_\ell = n_F / C_F$

QCD  $\rightarrow$  Abelian Gauge Theory

*Analytic Feature of  $SU(N_c)$  Gauge Theory*

*Scale-Setting procedure for QCD  
must be applicable to QED*

# *Lessons from QED : Summary*

- Effective couplings are complex analytic functions with the correct threshold structure expected from unitarity
- Multiple “renormalization” scales appear
- The scales are unambiguous since they are physical kinematic invariants
- Optimal improvement of perturbation theory

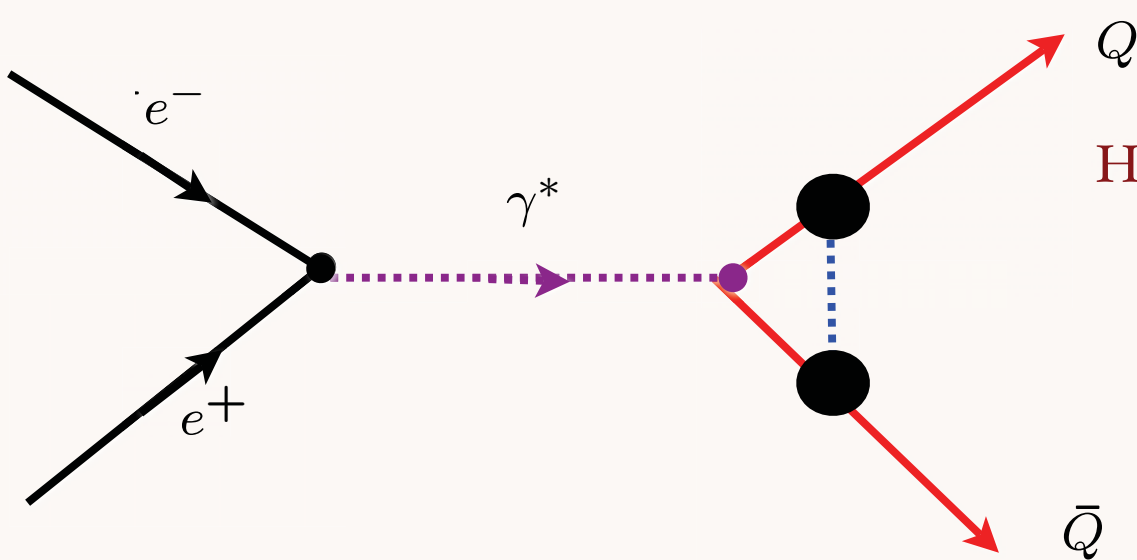
# Features of BLM Scale Setting

On The Elimination Of Scale Ambiguities In Perturbative Quantum Chromodynamics.

Lepage, Mackenzie, sjb

Phys.Rev.D28:228,1983

- All terms associated with non-zero beta function summed into running coupling
- Identical procedure in QED:
- Correct  $N_C = 0$  limit
- Resulting series identical to conformal series
- Renormalon  $n!$  growth of PQCD coefficients from beta function eliminated!
- In general, scale depends on all invariants



Hoang, Kuhn, Teubner, sjb

$$\begin{aligned}
 F_1 + F_2 &= 1 + \frac{\alpha(s \beta^2) \pi}{4 \beta} - 2 \frac{\alpha(s e^{3/4}/4)}{\pi} \\
 &\approx \left( 1 - 2 \frac{\alpha(s e^{3/4}/4)}{\pi} \right) \left( 1 + \frac{\alpha(s \beta^2) \pi}{4 \beta} \right)
 \end{aligned}$$

## *Example of Multiple BLM Scales*

Angular distributions of massive quarks and leptons close to threshold.



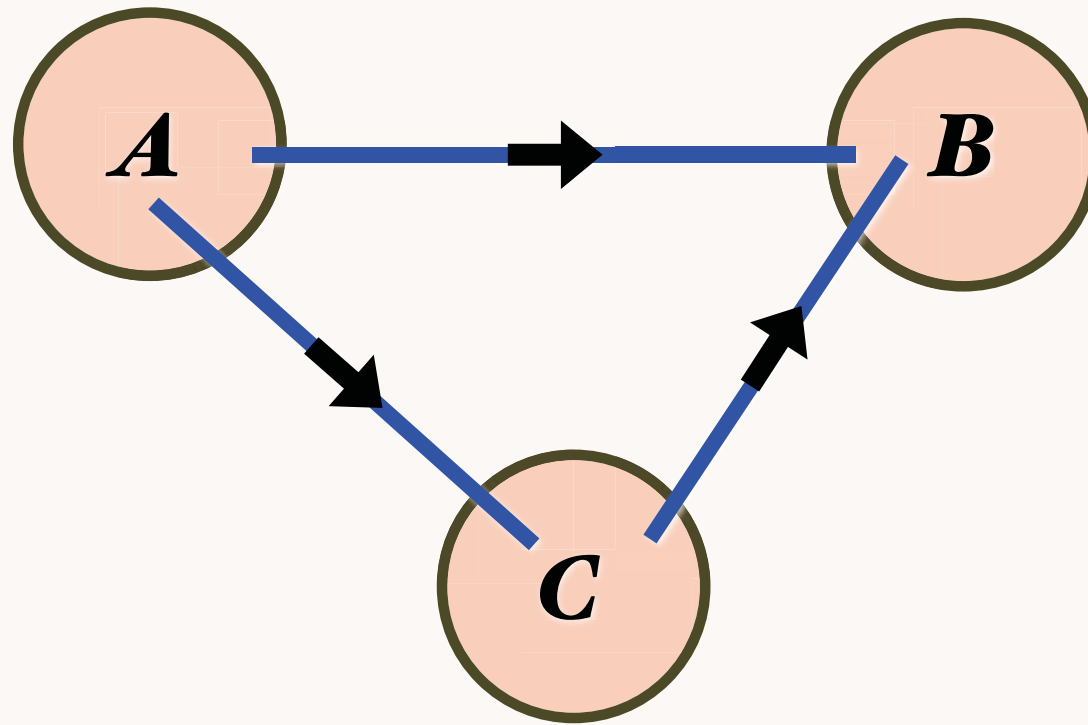
*Three-Jet Rate* T1

Kramer & Lampe

*Other Jet Observables:*

Rathsman

# *Transitivity Property of Renormalization Group*



**$A \rightarrow C$     $C \rightarrow B$    identical to    $A \rightarrow B$**

*Relation of observables independent of intermediate scheme  $C$*

## *Conventional renormalization scale-setting method :*

- Guess arbitrary renormalization scale and take arbitrary range. (Wrong for QED and Precision Electroweak).
- Prediction depends on choice of renormalization scheme
- Variation of result with respect to renormalization scale only sensitive to nonconformal terms; no information on genuine (conformal) higher order terms
- FAC and PMS give unphysical results.
- PMS violates transitivity property of renormalization group
- Renormalization scale not arbitrary! Analytic constraint from flavor thresholds

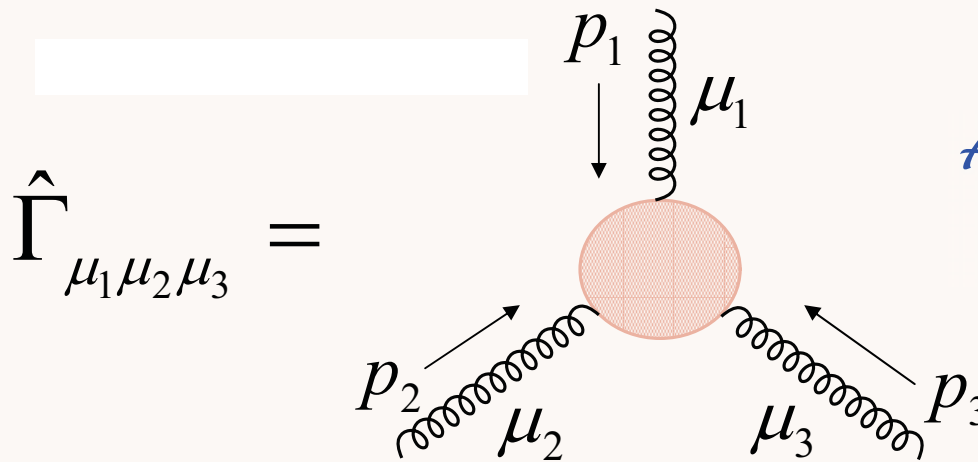
# BLM Method

- Satisfies Transitivity, all aspects of Renormalization Group; scheme independent
- Analytic at Flavor Thresholds
- Preserves Underlying Conformal Template
- Physical Interpretation of Scales; Multiple Scales
- Correct Abelian Limit ( $N_c = 0$ )
- Eliminates unnecessary source of imprecision of PQCD predictions
- Commensurate Scale Relations: Fundamental Tests of QCD free of renormalization scale and scheme ambiguities
- BLM used in many applications, QED, LGTH, BFKL, ...

# General Structure of the Three-Gluon Vertex

"THE FORM-FACTORS OF THE GAUGE-INVARIANT THREE-GLUON VERTEX"

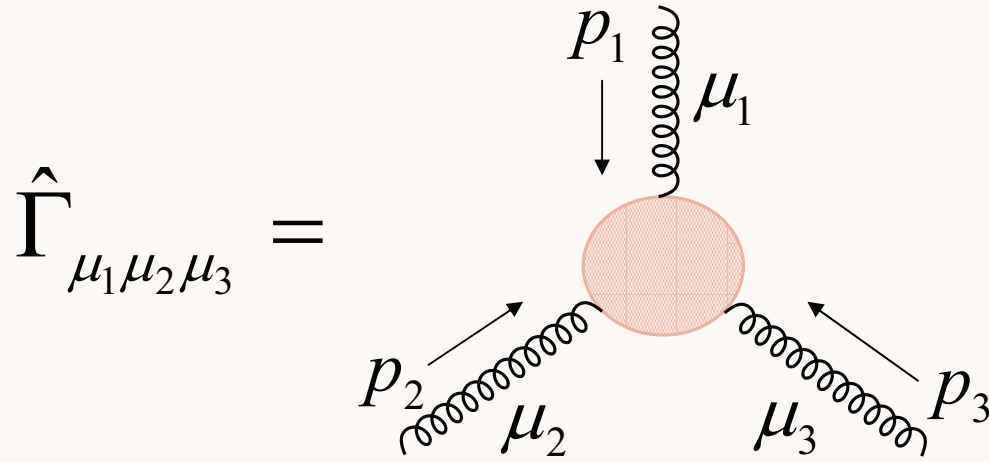
M. Binger, sjb



*Analytic calculation:  
general masses, spin*

3 index tensor  $\hat{\Gamma}_{\mu_1\mu_2\mu_3}$  built out of  $g_{\mu\nu}$  and  $p_1, p_2, p_3$   
with  $p_1 + p_2 + p_3 = 0$

➔ 14 basis tensors and form factors



H. J. Lu

$$\mu_R^2 \simeq \frac{p_{min}^2 p_{med}^2}{p_{max}^2}$$

## 3 Scale Effective Charge

$$\tilde{\alpha}(a,b,c) \equiv \frac{\tilde{g}^2(a,b,c)}{4\pi} \quad (\text{First suggested by H.J. Lu})$$

$$\frac{1}{\tilde{\alpha}(a,b,c)} = \frac{1}{\alpha_{bare}} + \frac{1}{4\pi} \beta_0 \left( L(a,b,c) - \frac{1}{\epsilon} + \dots \right)$$

$$\frac{1}{\tilde{\alpha}(a,b,c)} = \frac{1}{\tilde{\alpha}(a_0,b_0,c_0)} + \frac{1}{4\pi} \beta_0 [L(a,b,c) - L(a_0,b_0,c_0)]$$

$L(a,b,c)$  = 3-scale “log-like” function

$L(a,a,a)$  =  $\log(a)$

# Mass Effects

Binger, sjb

Calculated for all form factors

$$\text{SUSY relations } F_{MG} + 4F_{MQ} + (9-d)F_{MS} = 0$$

FF of tree level tensor structure



Effective Charge

Massive “log-like” function :  $L_{MQ}\left(\frac{a}{M^2}, \frac{b}{M^2}, \frac{c}{M^2}\right)$

$$L_{MQ}\left(\frac{a}{M^2}, \frac{b}{M^2}, \frac{c}{M^2}\right) \approx 5.125 \text{ for } M^2 \gg |a|, |b|, |c|$$

$$L_{MQ}\left(\frac{a}{M^2}, \frac{b}{M^2}, \frac{c}{M^2}\right) \approx L(a, b, c) - \log M^2 \text{ for } M^2 \ll |a|, |b|, |c|$$



## Properties of the *Effective Scale*

$$Q_{\text{eff}}^2(a, b, c) = Q_{\text{eff}}^2(-a, -b, -c)$$

$$Q_{\text{eff}}^2(\lambda a, \lambda b, \lambda c) = |\lambda| Q_{\text{eff}}^2(a, b, c)$$

$$Q_{\text{eff}}^2(a, a, a) = |a|$$

$$Q_{\text{eff}}^2(a, -a, -a) \approx 5.54 |a|$$

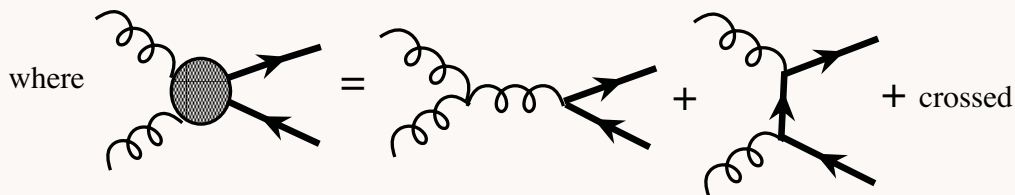
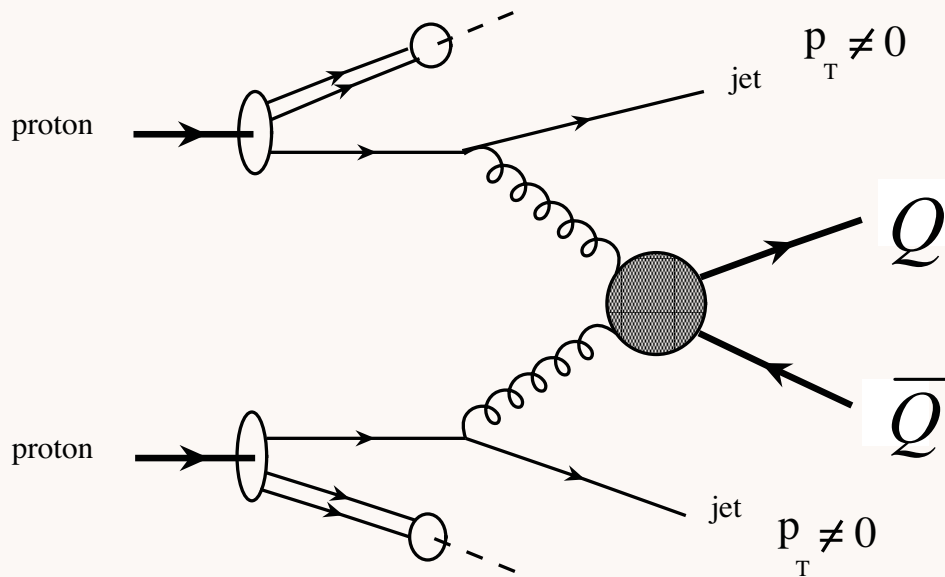
$$Q_{\text{eff}}^2(a, a, c) \approx 3.08 |c| \quad \text{for } |a| \gg |c|$$

$$Q_{\text{eff}}^2(a, -a, c) \approx 22.8 |c| \quad \text{for } |a| \gg |c|$$

$$Q_{\text{eff}}^2(a, b, c) \approx 22.8 \frac{|bc|}{|a|} \quad \text{for } |a| \gg |b|, |c|$$

*Surprising dependence on Invariants*

# Heavy Quark Hadro-production



- Preliminary calculation using (massless) results for tree level form factor
- Very low effective scale  
➔ much larger cross section than  $\overline{MS}$  with scale  $\mu_R = M_{Q\bar{Q}}$  or  $M_Q$
- Future : repeat analysis using the full mass-dependent results and include all form factors

**Expect that this approach accounts for most of the one-loop corrections**

# Elimination of Renormalization Scale Ambiguity

- **Multi-scale analytic** renormalization based on **physical, gauge-invariant** Green's functions
- **Optimal** improvement of perturbation theory with **no scale-ambiguity** since physical kinematic invariants are the arguments of the (multi-scale) couplings

# *Relate Observables to Each Other*

- Eliminate intermediate scheme
- No scale ambiguity
- Transitive!
- Commensurate Scale Relations
- Example: Generalized Crewther Relation

# *Geometric Series in Conformal QCD*

## *Generalized Crewther Relation*

Lu, Kataev, Gabadadze, Sjb

# Eliminate $\overline{MS}$ , Find Amazing Simplification

**BNL, January 8, 2008**

**Novel QCD Phenomena**

**Stan Brodsky  
SLAC**

# *Generalized Crewther Relation*

$$\left[1 + \frac{\alpha_R(s^*)}{\pi}\right] \left[1 - \frac{\alpha_{g_1}(q^2)}{\pi}\right] = 1$$

$$\sqrt{s^*} \simeq 0.52Q$$

*Conformal relation true to all orders in  
perturbation theory*

*No radiative corrections to axial anomaly*

*Nonconformal terms set relative scales (BLM)*

*Analytic matching at quark thresholds*

*No renormalization scale ambiguity!*

# *Leading Order Commensurate Scales*

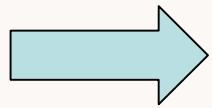
$p(Q)$

*Translation between schemes at LO*



# Analyticity and Mass Thresholds

$\overline{MS}$  does not have automatic decoupling of heavy particles



Must define a set of schemes in each desert region and match

$$\alpha_s^{(f)}(M_Q) = \alpha_s^{(f+1)}(M_Q)$$

- The coupling has **discontinuous derivative** at the matching point
- At higher orders the coupling itself becomes **discontinuous!**
- Does not distinguish between spacelike and timelike momenta

“AN ANALYTIC EXTENSION OF THE  $\overline{MS}$ -BAR RENORMALIZATION SCHEME”  
S. Brodsky, M. Gill, M. Melles, J. Rathsmann. **Phys.Rev.D58:116006,1998**

# Conformal symmetry: Template for QCD

- Initial approximation to PQCD; then correct for non-zero beta function and quark masses: *BLM*
- Commensurate scale relations: relate observables at corresponding scales: Generalized Crewther Relation
- Arguments for Infrared fixed-point for  $\alpha_s$
- Effective Charges: analytic at quark mass thresholds, finite at small momenta
- Eigensolutions of Evolution Equation of distribution amplitudes  
V. Braun et al;  
Frishman, Lepage, Sachrajda, sjb
- AdS/QCD

# *Use Physical Scheme to Characterize QCD Coupling*

- Use Observable to define QCD coupling or Pinch Scheme
- Analytic: Smooth behavior as one crosses new quark threshold
- New perspective on grand unification

Binger, Sjb

# Unification in Physical Schemes

“PHYSICAL RENORMALIZATION SCHEMES AND GRAND UNIFICATION”  
M.B. and Stanley J. Brodsky. *Phys.Rev.D69:095007,2004*

$$\alpha_i(Q) = \frac{\alpha_i(Q_0)}{1 + \hat{\Pi}_i(Q) - \hat{\Pi}_i(Q_0)} \quad i=1,2,3$$

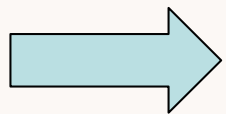
$$\hat{\Pi}_i(Q) = \frac{\alpha_i}{4\pi} \sum_p \beta_i^{(p)} \left( L_{s(p)}(Q^2 / m_p^2) + \dots \right)$$

“log-like” function:

$$\eta_p = 8/3, 5/3, 40/21$$

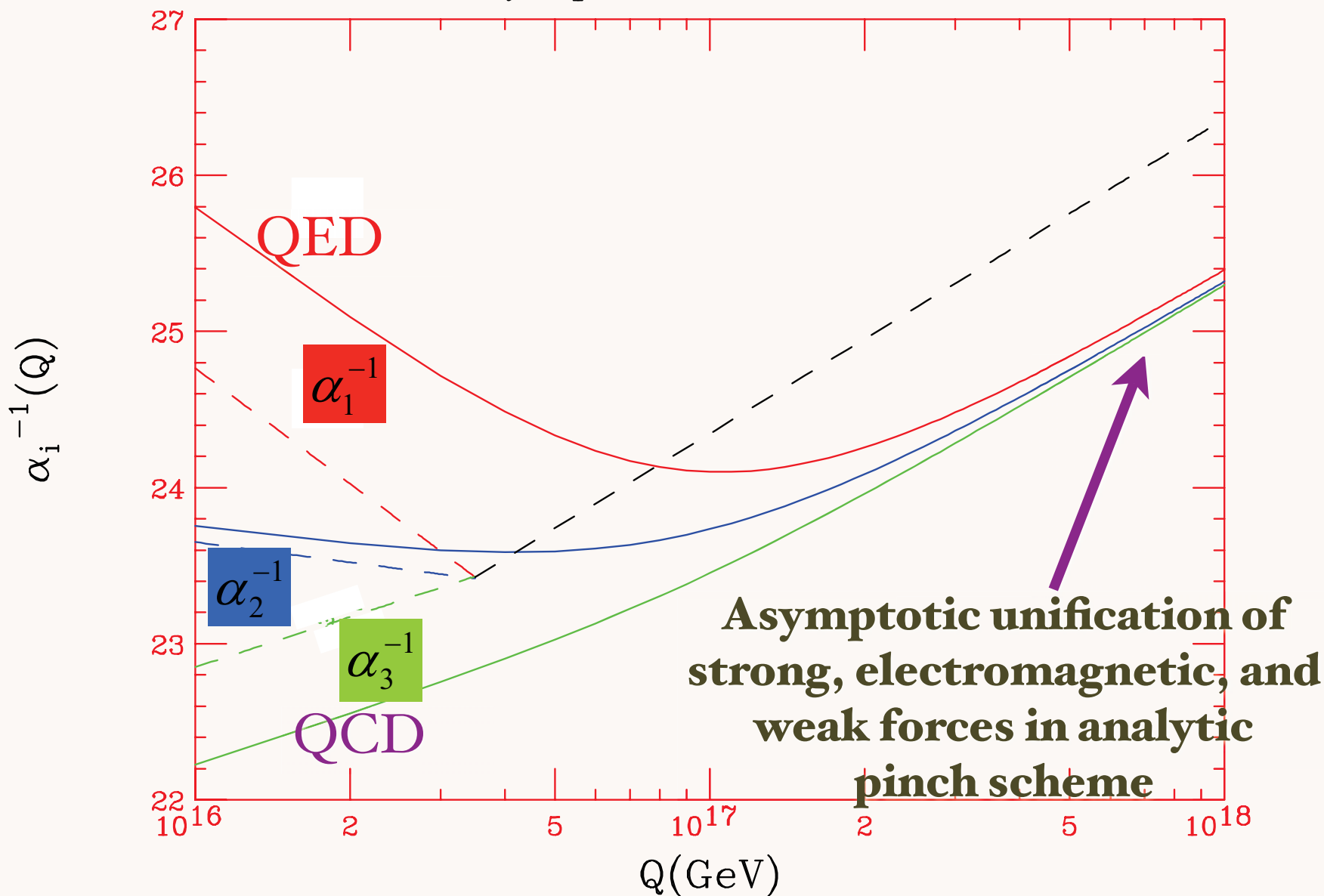
$$L_{s(p)} \approx \log(e^{\eta_p} + Q^2 / m_p^2)$$

For spin  $s(p) = 0, 1/2, \text{ and } 1$



Elegant and natural formalism for all threshold effects

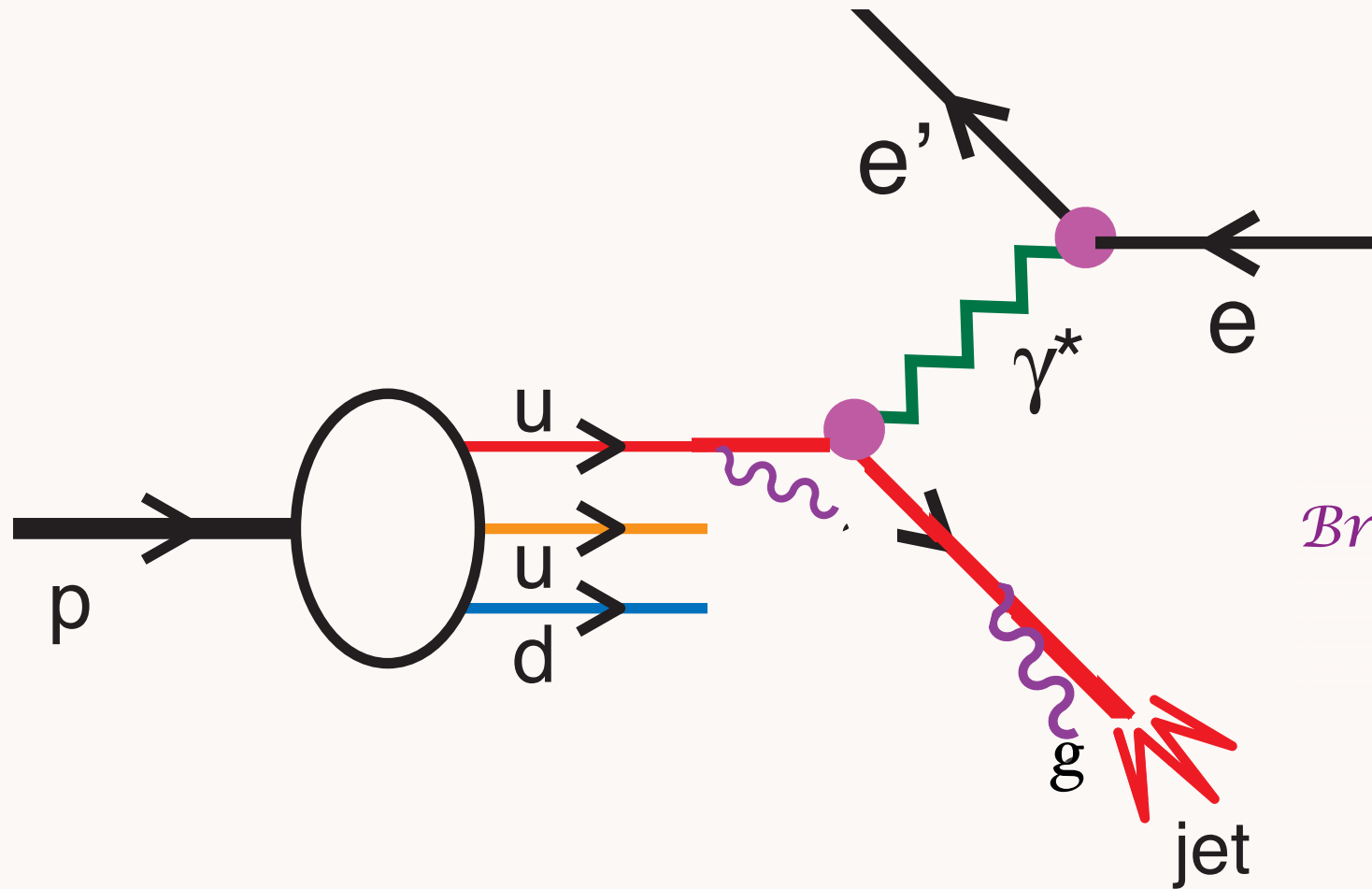
### Asymptotic Unification



# Challenging Conventional Wisdom

- **Renormalization scale is arbitrary**
- • **Initial and final-state interactions are power suppressed in a hard QCD reaction**
- **Heavy quark distributions derive exclusively from gluon splitting**
- **Nuclear parton distributions are universal**
- **Hadroproduction at large transverse momentum derives exclusively from 2 to 2 scattering subprocesses**

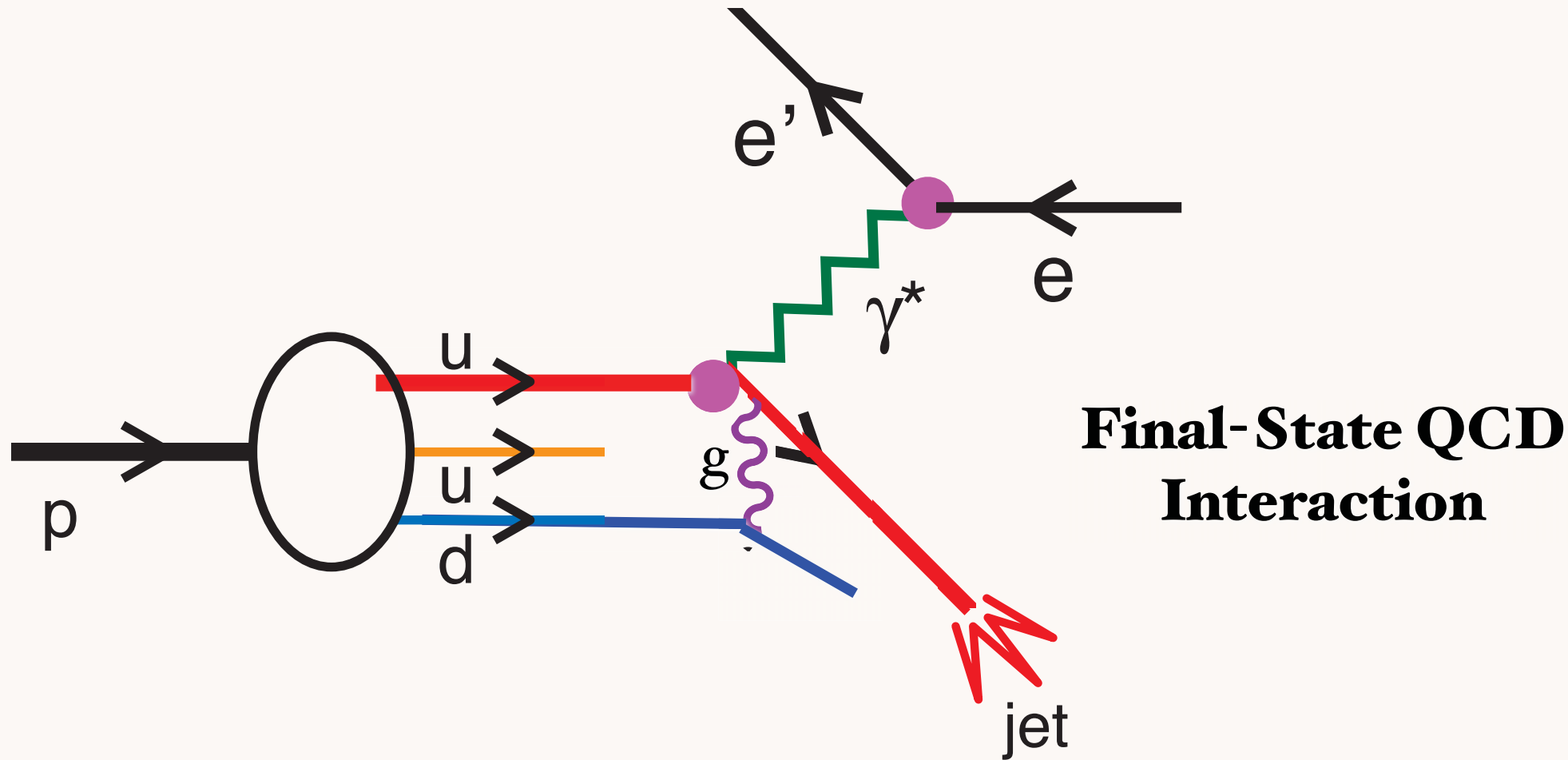
# Deep Inelastic Electron-Proton Scattering



*Gluonic  
Bremsstrahlung*

**DGLAP Evolution**

# Deep Inelastic Electron-Proton Scattering



*Conventional wisdom:  
Final-state interactions of struck quark can be neglected*



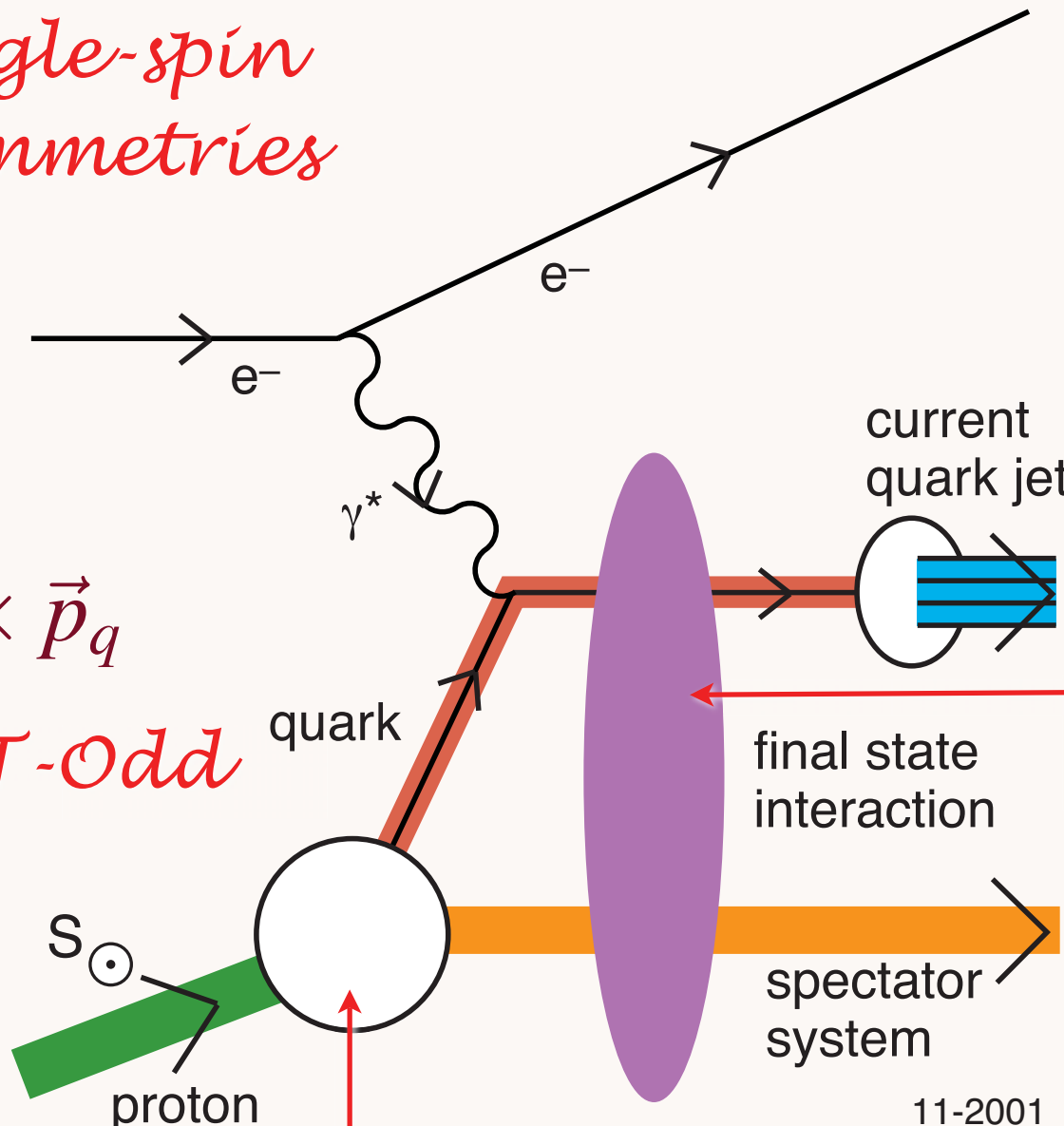
# Physics of Rescattering

- Diffractive DIS: New Insights into Final State Interactions in QCD
- Origin of Hard Pomeron
- Structure Functions not Probability Distributions!
- T-odd SSAs, Shadowing, Antishadowing
- Diffractive dijets/ trijets, doubly diffractive Higgs
- Novel Effects: Color Transparency, Color Opaqueness, Intrinsic Charm, Odderon

*Single-spin asymmetries*

# Leading Twist Sivers Effect

$i \vec{S}_p \cdot \vec{q} \times \vec{p}_q$   
*Pseudo-T-Odd*



*QCD S- and P-Coulomb Phases*

*Light-Front Wavefunction  
S and P-Waves*

11-2001  
8624A06

D. S. Hwang,  
I. A. Schmidt,  
sjb

BNL, January 8, 2008

**Novel QCD Phenomena**

Stan Brodsky  
SLAC

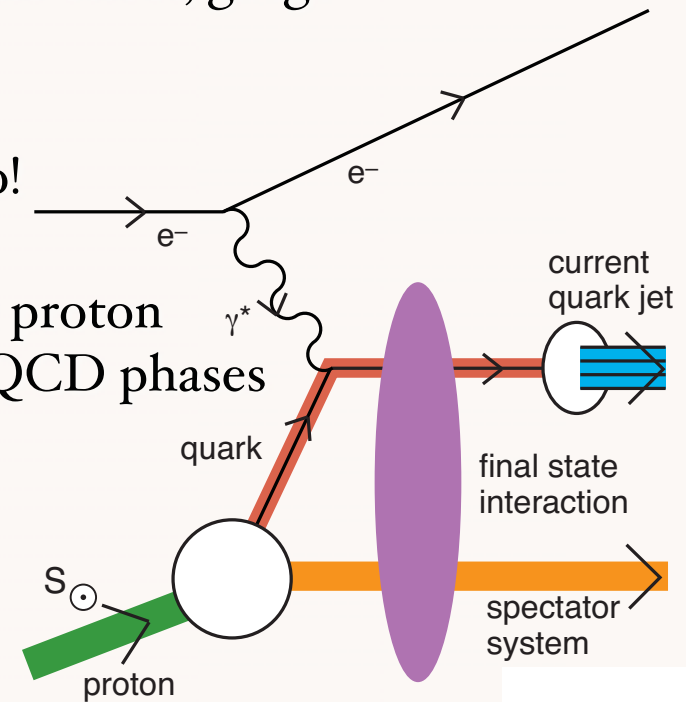
# *Final-State Interactions Produce T-Odd (Sivers Effect) $\mathbf{i} \vec{S} \cdot \vec{p}_{jet} \times \vec{q}$*

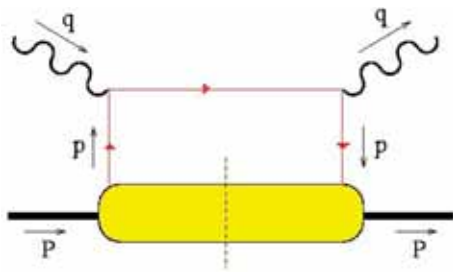
- Bjorken Scaling!
- Arises from Interference of Final-State Coulomb Phases in S and P waves
- Relate to the quark contribution to the target proton anomalous magnetic moment

Hwang, Schmidt. sjb;  
Burkardt

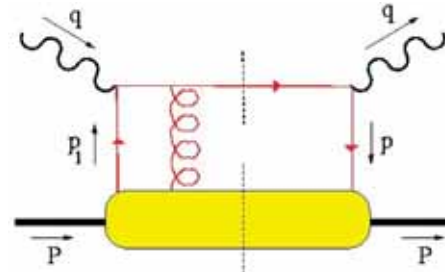
# Final-State Interactions Produce Pseudo-T-Odd (Sivers Effect)

- Leading-Twist Bjorken Scaling!
- Requires nonzero orbital angular momentum of quark!  $\mathbf{i} \vec{S} \cdot \vec{p}_{jet} \times \vec{q}$
- Arises from the interference of Final-State QCD Coulomb phases in S- and P- waves; Wilson line effect; gauge independent
- Unexpected QCD Effect -- thought to be zero!
- Relate to the quark contribution to the target proton anomalous magnetic moment and final-state QCD phases
- QCD Coulomb phase at soft scale
- Measure in jet trigger or leading hadron
- Sum of Sivers Functions for all quarks and gluons vanishes. (Zero gravito-anomalous magnetic moment:  $B(o)= o$ )

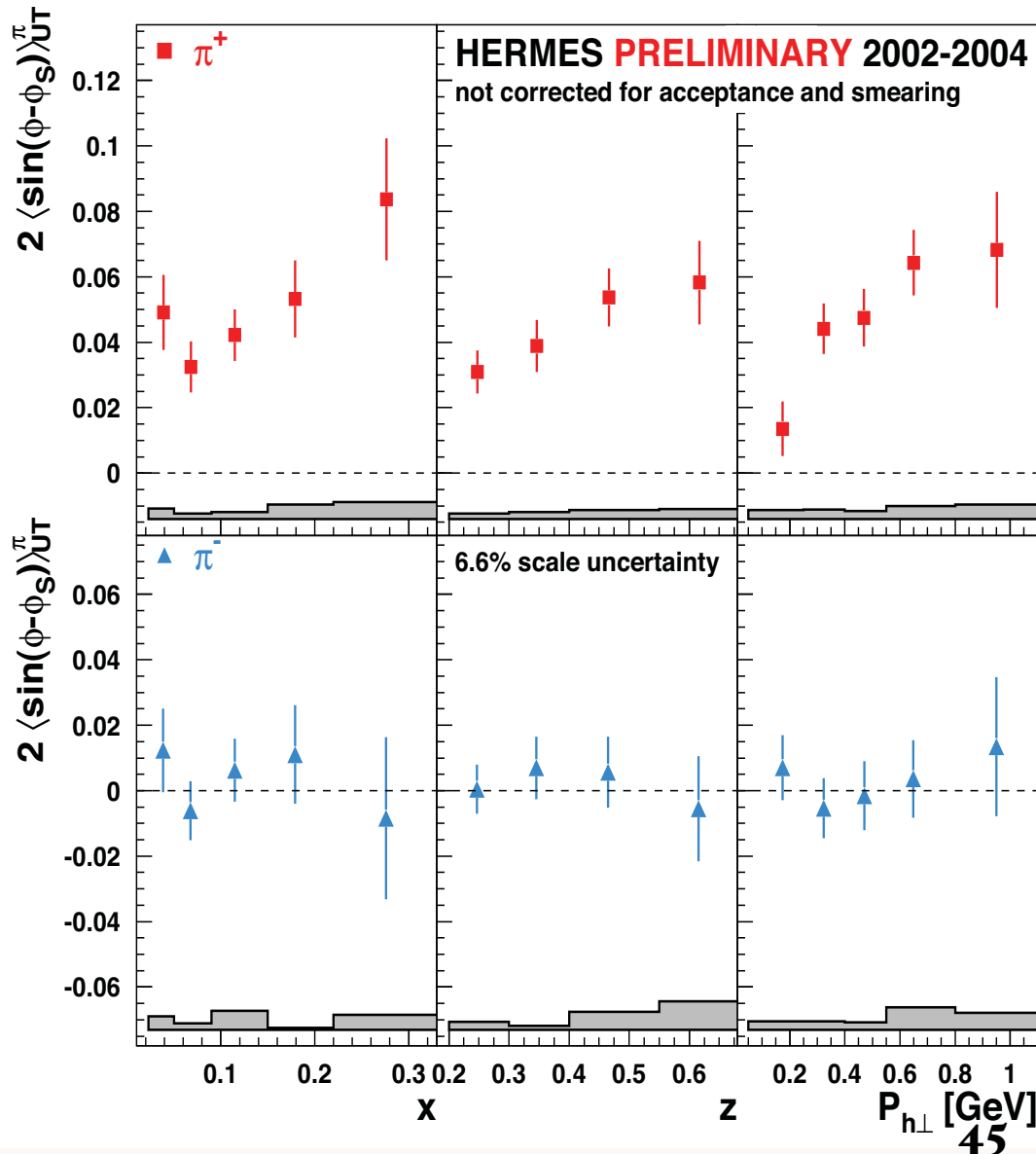




can interfere  
with



and produce  
a T-odd effect!  
(also need  $L_z \neq 0$ )



- First evidence for non-zero Sivers function!
- $\Rightarrow$  presence of non-zero quark orbital angular momentum!
- **Positive** for  $\pi^+$  ...  
Consistent with zero for  $\pi^-$  ...

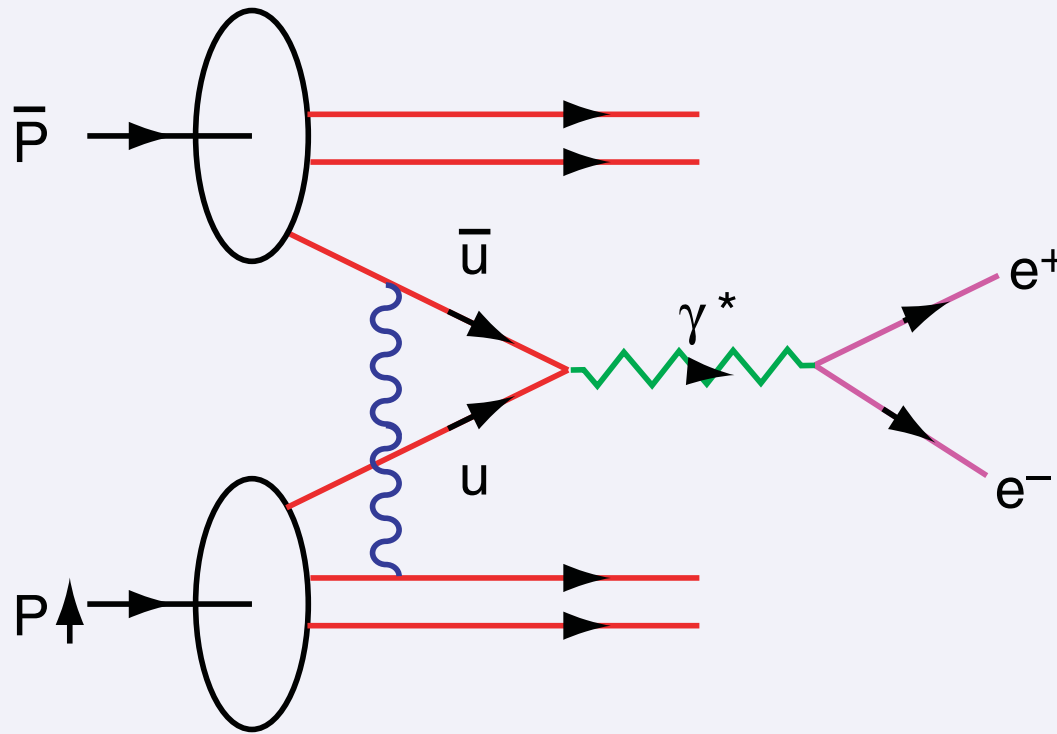
**Gamberg: Hermes data compatible with BHS model**

**Schmidt, Lu: Hermes charge pattern follow quark contributions to anomalous moment**

Tomena

Stan Brodsky  
SLAC

# Predict Opposite Sign SSA in DY !



Collins;  
Hwang, Schmidt.  
sjb

Single Spin Asymmetry In the Drell Yan Process

$$\vec{S}_p \cdot \vec{p} \times \vec{q}_{\gamma^*}$$

Quarks Interact in the Initial State

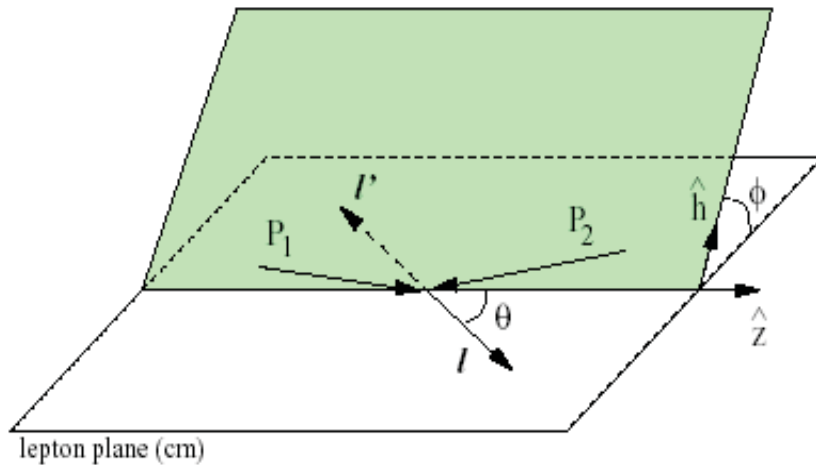
Interference of Coulomb Phases for  $S$  and  $P$  states

Produce Single Spin Asymmetry [Siver's Effect] Proportional to the Proton Anomalous Moment and  $\alpha_s$ .

Opposite Sign to DIS! No Factorization

# Drell-Yan angular distribution

## *Unpolarized DY*



Lam – Tung SR :  $1 - \lambda = 2\nu$

NLO pQCD :  $\lambda \approx 1 \quad \mu \approx 0 \quad \nu \approx 0$

experiment :  $\nu \approx 0.3$

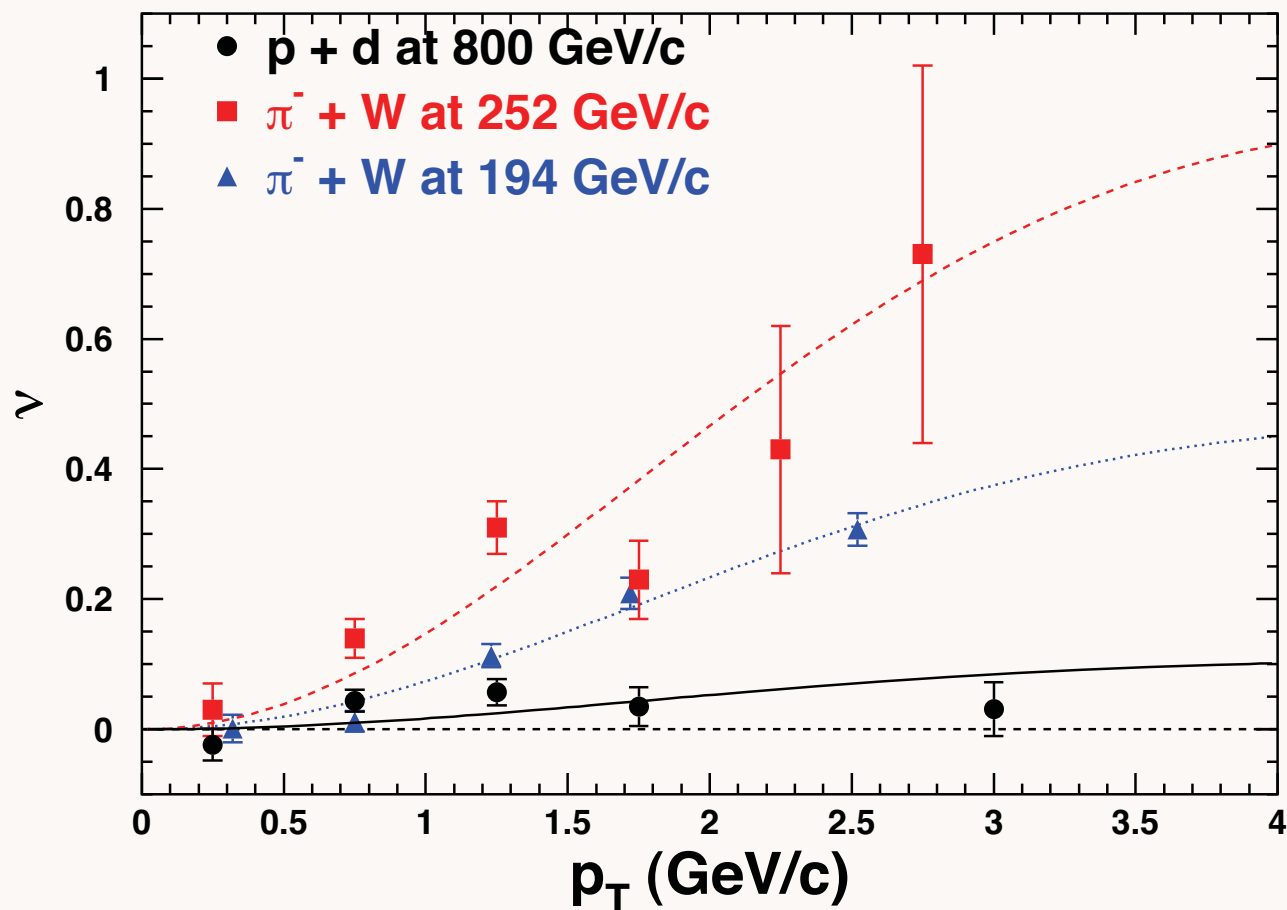
$$\frac{1}{\sigma} \frac{d\sigma}{d\Omega} = \frac{3}{4\pi} \frac{1}{\lambda + 3} \left( 1 + \lambda \cos^2 \theta + \mu \sin 2\theta \cos \phi + \frac{\nu}{2} \sin^2 \theta \cos 2\phi \right)$$

- Experimentally, a violation of the Lam-Tung sum rule is observed by sizeable  $\cos 2\phi$  moments
- Several model explanations
  - higher twist
  - spin correlation due to non-trivial QCD vacuum
  - Non-zero Boer Mulders function

**B. Seitz**

# Measurement of Angular Distributions of Drell-Yan Dimuons in $p + d$ Interaction at 800 GeV/c

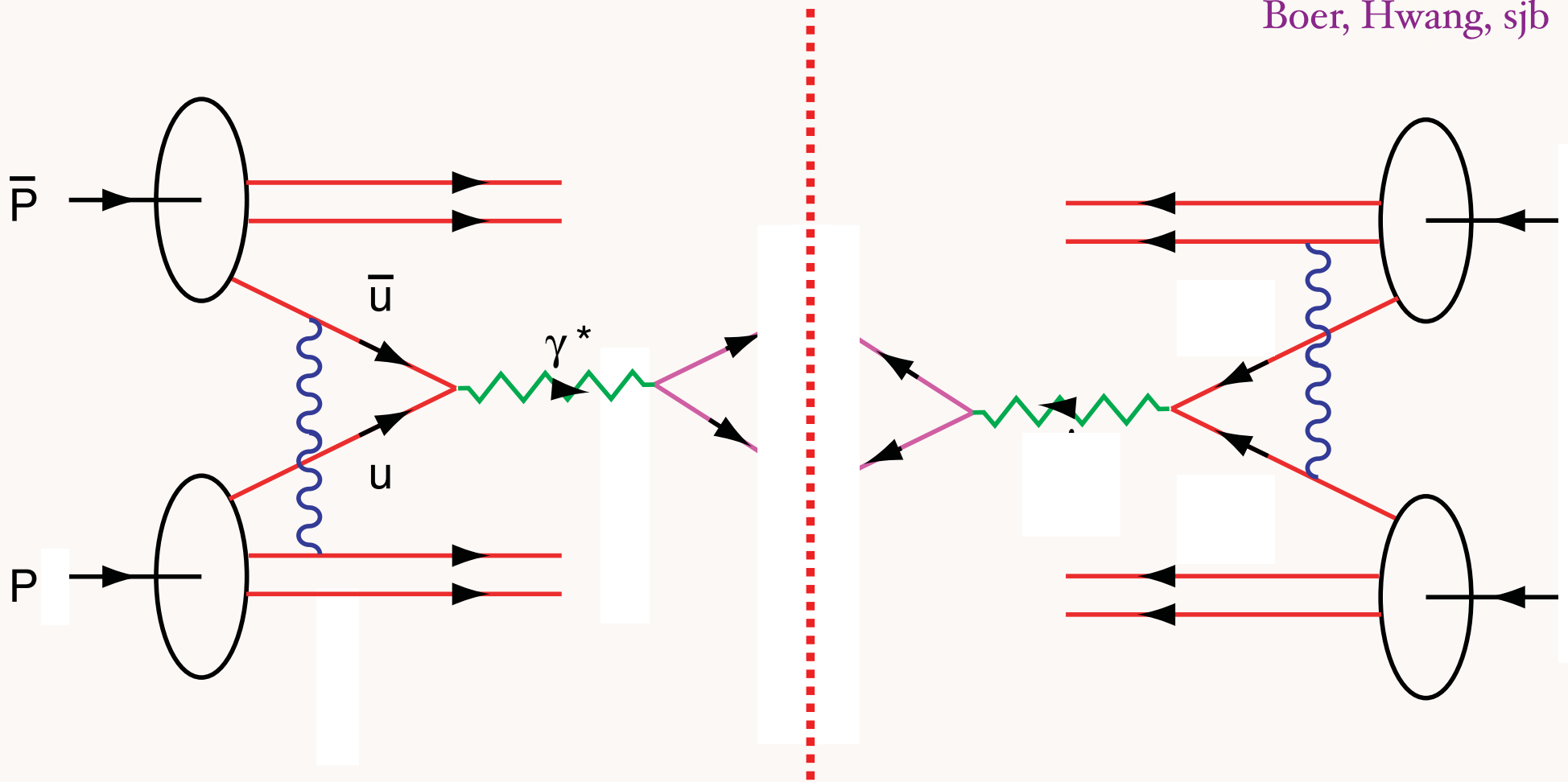
(FNAL E866/NuSea Collaboration)



Huge Effect in  
 $\pi W \rightarrow \mu^+ \mu^- X$   
Negligible Effect  
 $pd \rightarrow \mu^+ \mu^- X$

Parameter  $\nu$  vs.  $p_T$  in the Collins-Soper frame for three Drell-Yan measurements. Fits to the data using Eq. 3 and  $M_C = 2.4 \text{ GeV}/c^2$  are also shown.





**$DY \cos 2\phi$  correlation at leading twist from double ISI**

*Product of Boer - Mulders Functions*

$$h_1^\perp(x_1, \mathbf{p}_\perp^2) \times \bar{h}_1^\perp(x_2, \mathbf{k}_\perp^2)$$

$$f_1 = \text{[Diagram: Yellow circle with a blue dot in the center.]}$$

*Unpolarized Distribution*

$$g_{1L} = \text{[Diagram: Yellow circle with a blue dot on the left and a right-pointing arrow.]} - \text{[Diagram: Yellow circle with a blue dot on the right and a left-pointing arrow.]}$$

*Bj Sum Rule*

$$h_{1T} = \text{[Diagram: Yellow circle with a blue dot at the bottom and an upward-pointing arrow.]} - \text{[Diagram: Yellow circle with a blue dot at the top and a downward-pointing arrow.]}$$

*Transversity*

$$f_{1T}^\perp = \text{[Diagram: Yellow circle with a blue dot in the center and an upward-pointing arrow.]} - \text{[Diagram: Yellow circle with a blue dot in the center and a downward-pointing arrow.]}$$

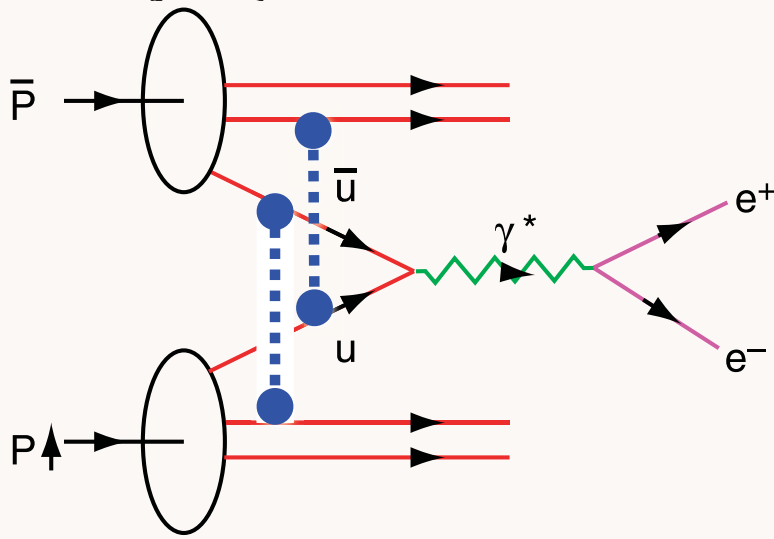
*Sivers Function*

$$h_1^\perp = \text{[Diagram: Yellow circle with a blue dot in the center and a downward-pointing arrow.]} - \text{[Diagram: Yellow circle with a blue dot in the center and an upward-pointing arrow.]}$$

*Boer-Mulders Function*

*T-Odd:  
Require ISI or FSI*

# DY cos 2φ correlation at leading twist from double ISI



*Product of Boer -  
Mulders  
Functions*

$$h_1^\perp(x_1, \mathbf{p}_\perp^2) \times \bar{h}_1^\perp(x_2, \mathbf{k}_\perp^2)$$

$$F \equiv \mathcal{F}[(2\hat{h} \cdot \mathbf{p}_\perp \hat{h} \cdot \mathbf{k}_\perp - \mathbf{p}_\perp \cdot \mathbf{k}_\perp) h_1^\perp \bar{h}_1^\perp]$$

$$= \int d^2\mathbf{p}_\perp d^2\mathbf{k}_\perp \delta^2(\mathbf{p}_\perp + \mathbf{k}_\perp - \mathbf{q}_\perp) (2\hat{h} \cdot \mathbf{p}_\perp \hat{h} \cdot \mathbf{k}_\perp - \mathbf{p}_\perp \cdot \mathbf{k}_\perp) \times h_1^\perp(\Delta, \mathbf{p}_\perp^2) \bar{h}_1^\perp(\bar{\Delta}, \mathbf{k}_\perp^2),$$

(40)

$$\nu = \frac{2}{M_1 M_2} \frac{\sum_{a, \bar{a}} e_a^2 F_a}{\sum_{a, \bar{a}} e_a^2 G_a}$$

$$G \equiv \mathcal{F}[f_1 \bar{f}_1]$$

$$= \int d^2\mathbf{p}_\perp d^2\mathbf{k}_\perp \delta^2(\mathbf{p}_\perp + \mathbf{k}_\perp - \mathbf{q}_\perp) f_1(\Delta, \mathbf{p}_\perp^2) \bar{f}_1(\bar{\Delta}, \mathbf{k}_\perp^2),$$

**Boer, Hwang, sjb**

# Double Initial-State Interactions

generate anomalous  $\cos 2\phi$

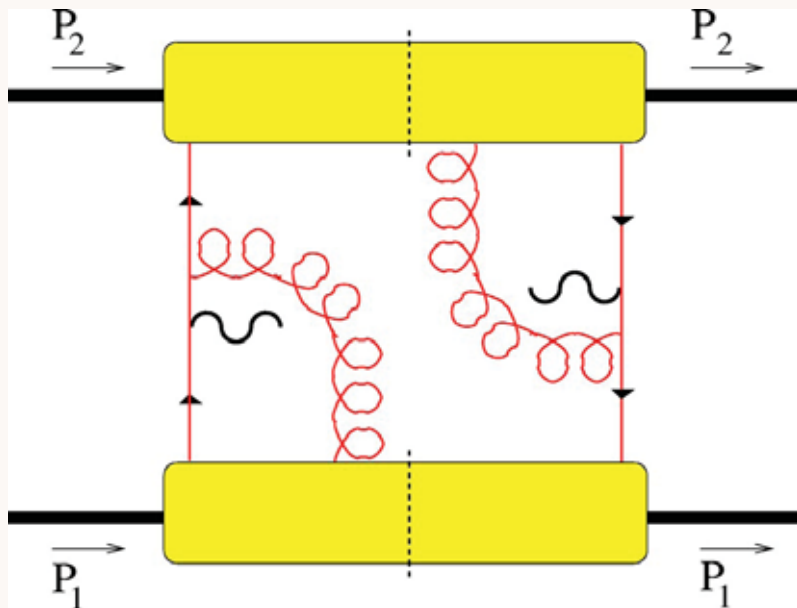
Boer, Hwang, sjb

## Drell-Yan planar correlations

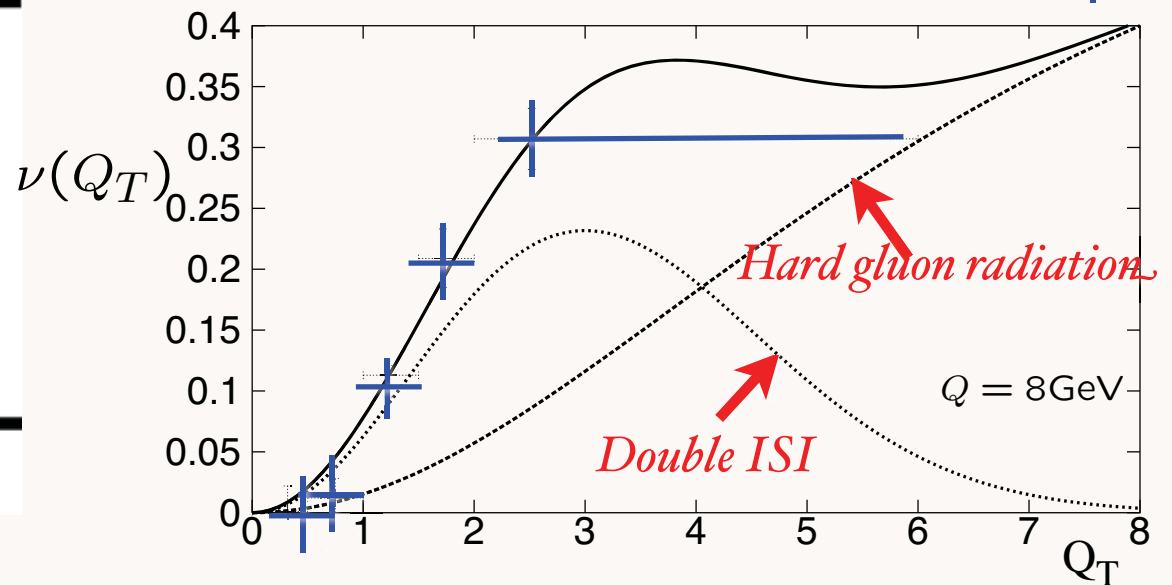
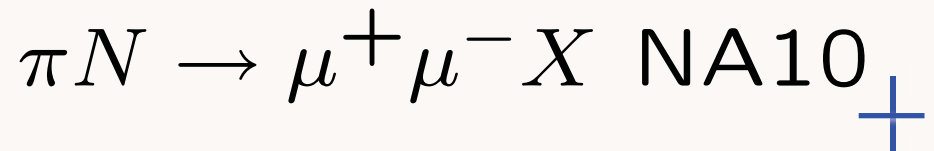
$$\frac{1}{\sigma} \frac{d\sigma}{d\Omega} \propto \left( 1 + \lambda \cos^2 \theta + \mu \sin 2\theta \cos \phi + \frac{\nu}{2} \sin^2 \theta \cos 2\phi \right)$$

PQCD Factorization (Lam Tung):  $1 - \lambda - 2\nu = 0$

$$\frac{\nu}{2} \propto h_1^\perp(\pi) h_1^\perp(N)$$



**Violates Lam-Tung relation!**



Model: Boer,

Stan Brodsky  
SLAC

# Anomalous effect from Double ISI in Massive Lepton Production

Boer, Hwang, sjb

$\cos 2\phi$  correlation

- Leading Twist, valence quark dominated
- Violates Lam-Tung Relation!
- Not obtained from standard PQCD subprocess analysis
- Normalized to the square of the single spin asymmetry in semi-inclusive DIS
- No polarization required
- Challenge to standard picture of PQCD Factorization

