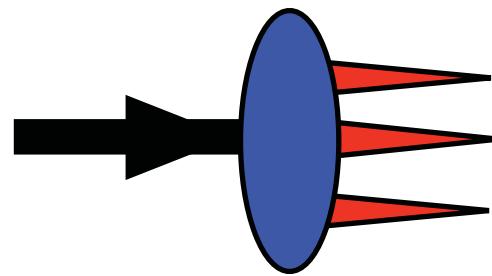
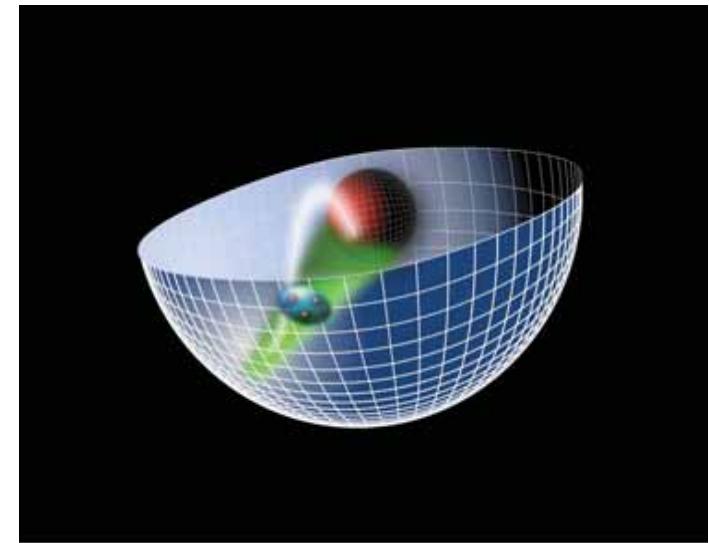


# *QCD at the Light-Front*



$$\Psi_n(x_i, \vec{k}_{\perp i}, \lambda_i)$$



LC 2010  
university of valencia

**June 17, 2010**



**Stan Brodsky**



*& CP3 -Origins*

# Light Cone 2010

Relativistic Hadronic and Particle Physics

Valencia, Spain  
June, 14-18, 2010

## Local Organizing Committee

### *Chairpersons*

- Joannis Papavassiliou (Universidad de Valencia-IFIC, Spain)
- Vicente Vento (Universidad de Valencia-IFIC, Spain)

### *Scientific Secretaries*

- Arlene Cristina Aguilar (Universidade Federal ABC, Brazil)
- Aurore Courtoy (INFN Sezione di Pavia, Italy)
- Jorge Portolés (IFIC, Spain)



# I•L•C•A•C, Inc.

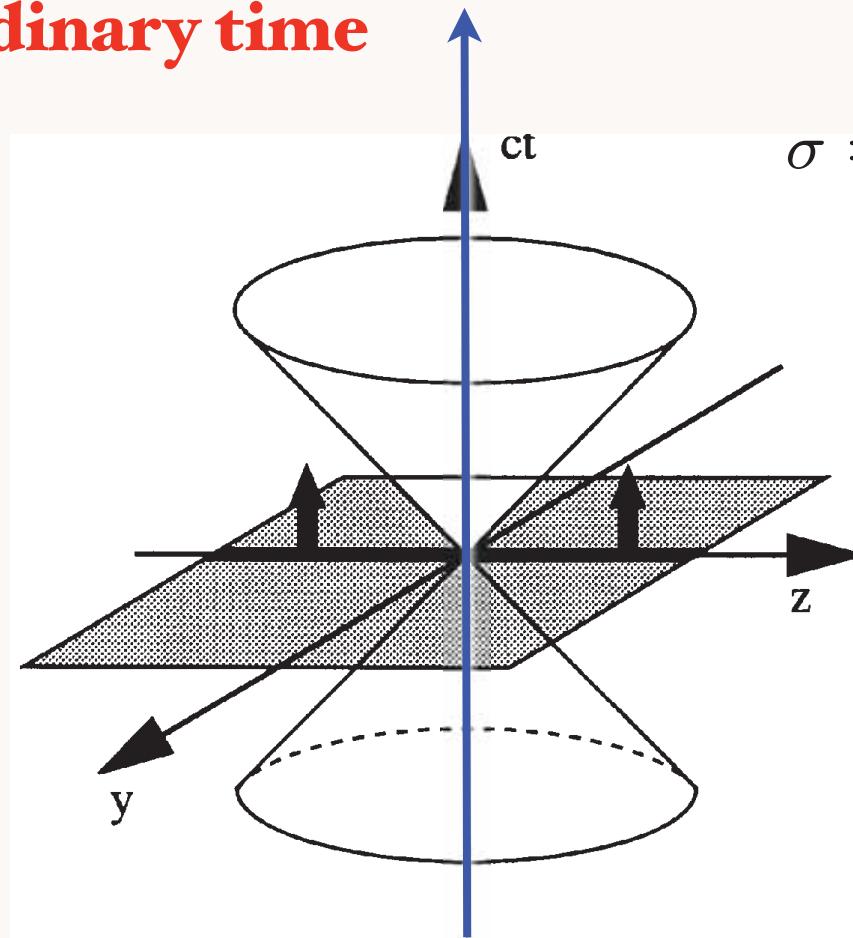
## The International Light Cone Advisory Committee, Inc.

### Previous Meetings:

<u>Place</u>	<u>Organizer</u>	<u>Number of Participants</u>
<a href="#"><u>Light Cone 2009</u></a>	Frederico, Bakker ( <a href="#">Pictures</a> )	
<a href="#"><u>Light Cone 2008</u></a>	Mathiot, Bakker & Diehl: Mulhouse Pictures <a href="#">1</a> , <a href="#">2</a>	58
<a href="#"><u>Amsterdam 2004</u></a>	Bakker, Boer & Mulders	49
<a href="#"><u>Durham 2003</u></a>	Stirling, Dalley & Wilkinson	54
<a href="#"><u>Los Alamos 2002</u></a>	Johnson, Kisslinger, Burkardt & Pate	about 50
Trento2001	Bassetto, Griguolo, Nardelli & Vian	77
<a href="#"><u>Heidelberg2000</u></a>	Pauli, Werner & Hollenberg	57
<a href="#"><u>Adelaide99</u></a>	Hollenberg, McKellar & Williams	55
<a href="#"><u>StPetersburg98</u></a>	Lipatov	70
<a href="#"><u>LesHouches97</u></a>	Grange	about 80
Ames96	Vary	75
Regensburg95	Werner	about 70
Seattle94	Miller	about 80
Zürich93	Wyler	about 60
Dallas92	McCartor	about 70
<a href="#"><u>Heidelberg91</u></a>	Pauli	about 50

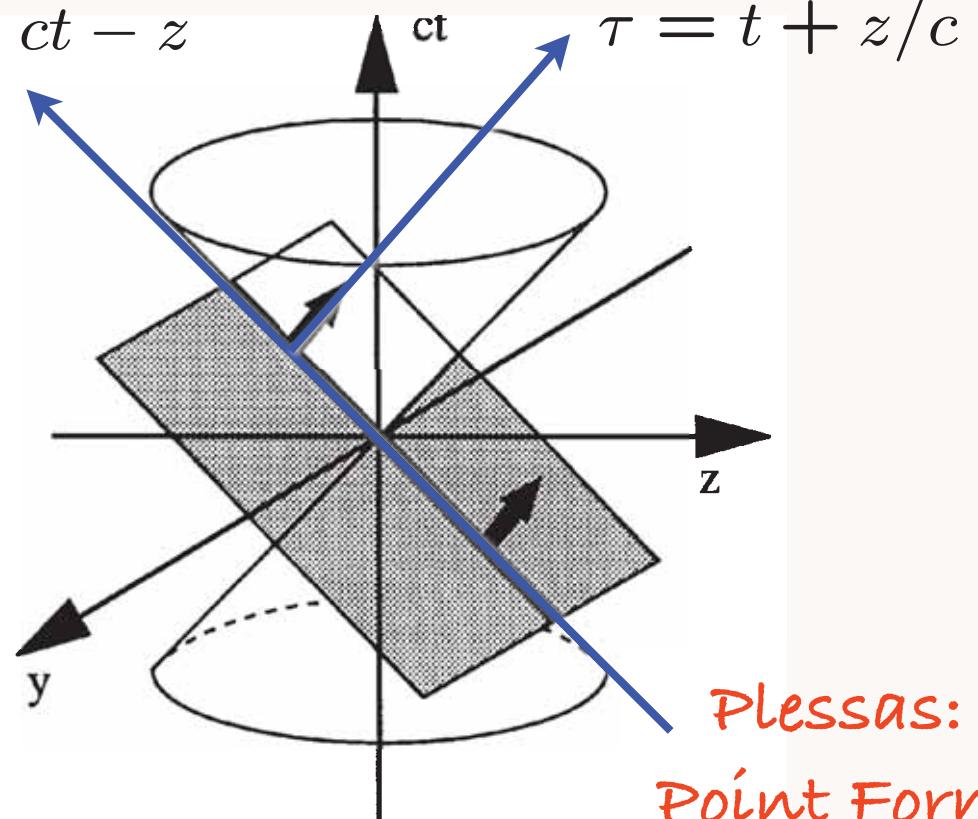
# Dirac's Amazing Idea: The Front Form

Evolve in  
ordinary time



Instant Form

Evolve in  
light-front time!



Front Form

Each element of  
flash photograph  
illuminated  
at same Light Front  
time

$$\tau = t + z/c$$

Evolve in LF time

$$P^- = i \frac{d}{d\tau}$$

**Causal, Trivial Vacuum**

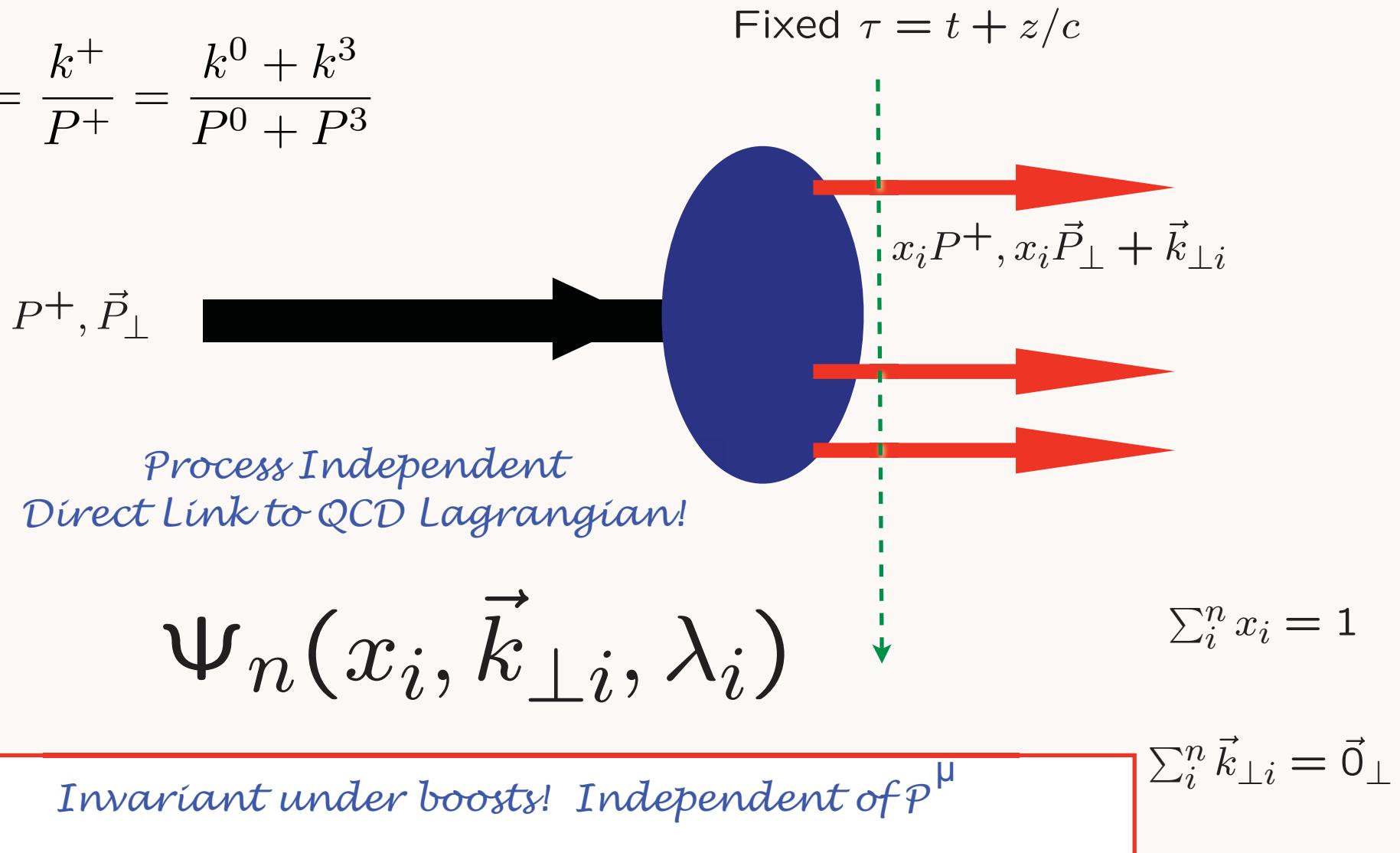
Laser Physics is  
Light-Front Physics

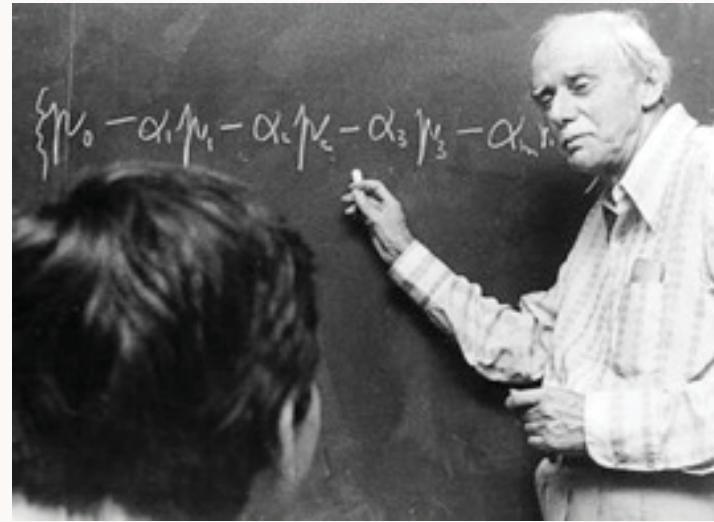
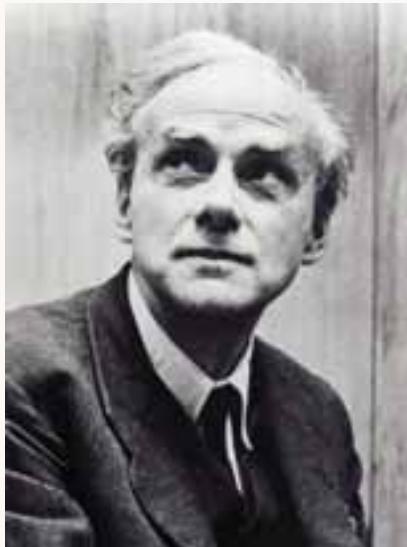


T  
e.  
x  
t

# Light-Front Wavefunctions: rigorous representation of composite systems in quantum field theory

$$x = \frac{k^+}{P^+} = \frac{k^0 + k^3}{P^0 + P^3}$$





*"Working with a front is a process that is unfamiliar to physicists.  
But still I feel that the mathematical simplification that it introduces is all-important.*

*I consider the method to be promising and have recently been making an extensive study of it.*

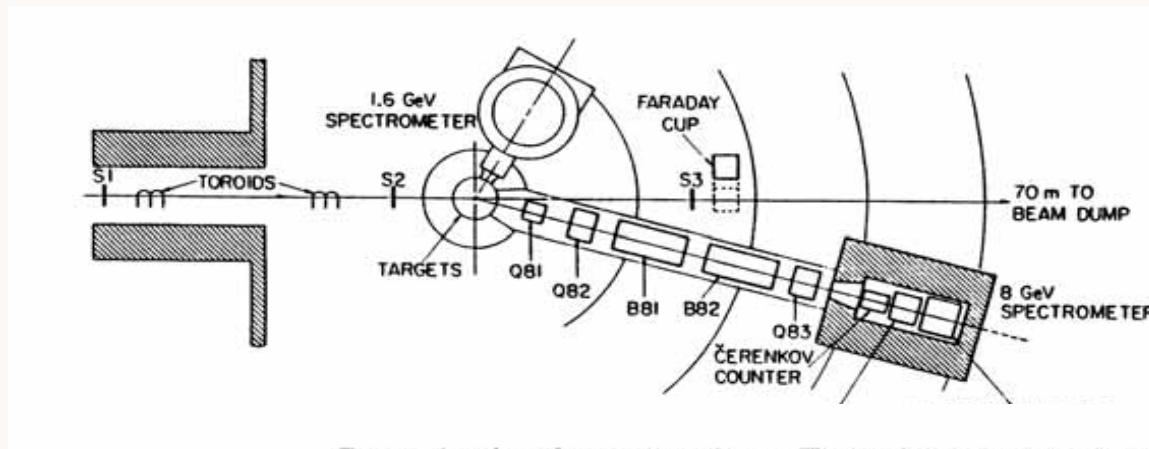
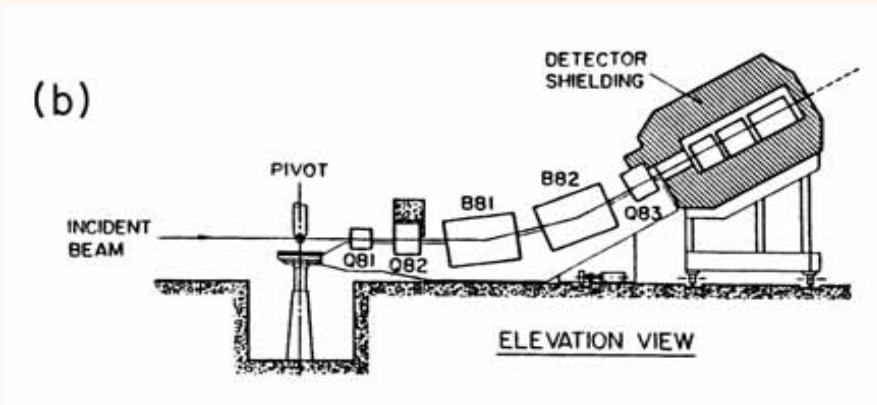
*It offers new opportunities, while the familiar instant form seems to be played out" - P.A.M. Dirac (1977)*

# 1967 SLAC Experiment:

Scatter 20 GeV/c Electrons on protons  
in a Hydrogen Target

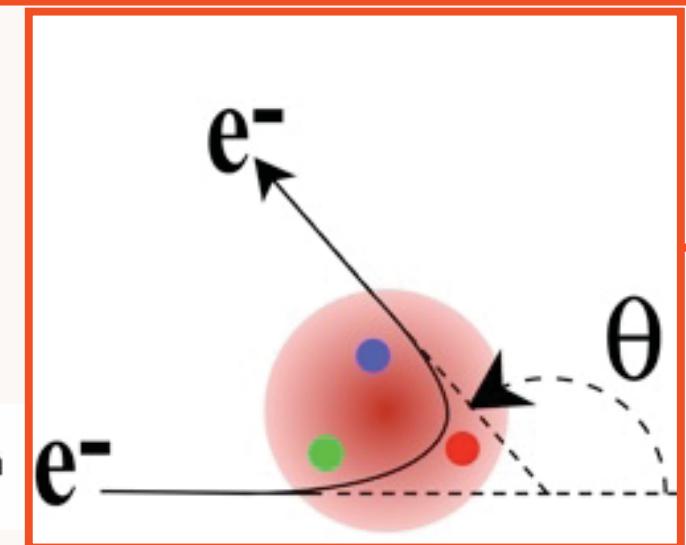
Discovery of the Quark Structure of Matter

$$ep \rightarrow e' X$$



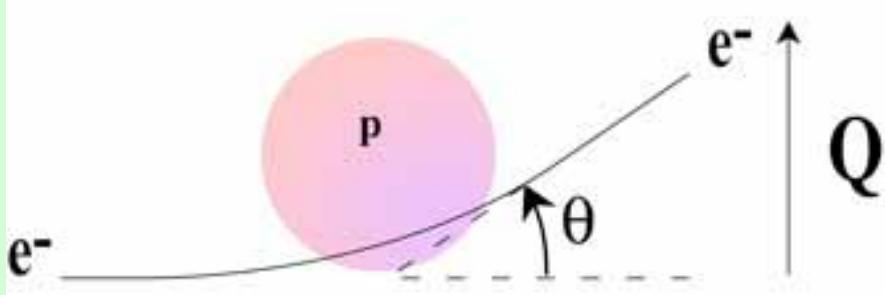
Deep inelastic scattering: Experiments on the proton  
and the observation of scaling\*

**Discovery of quarks!**



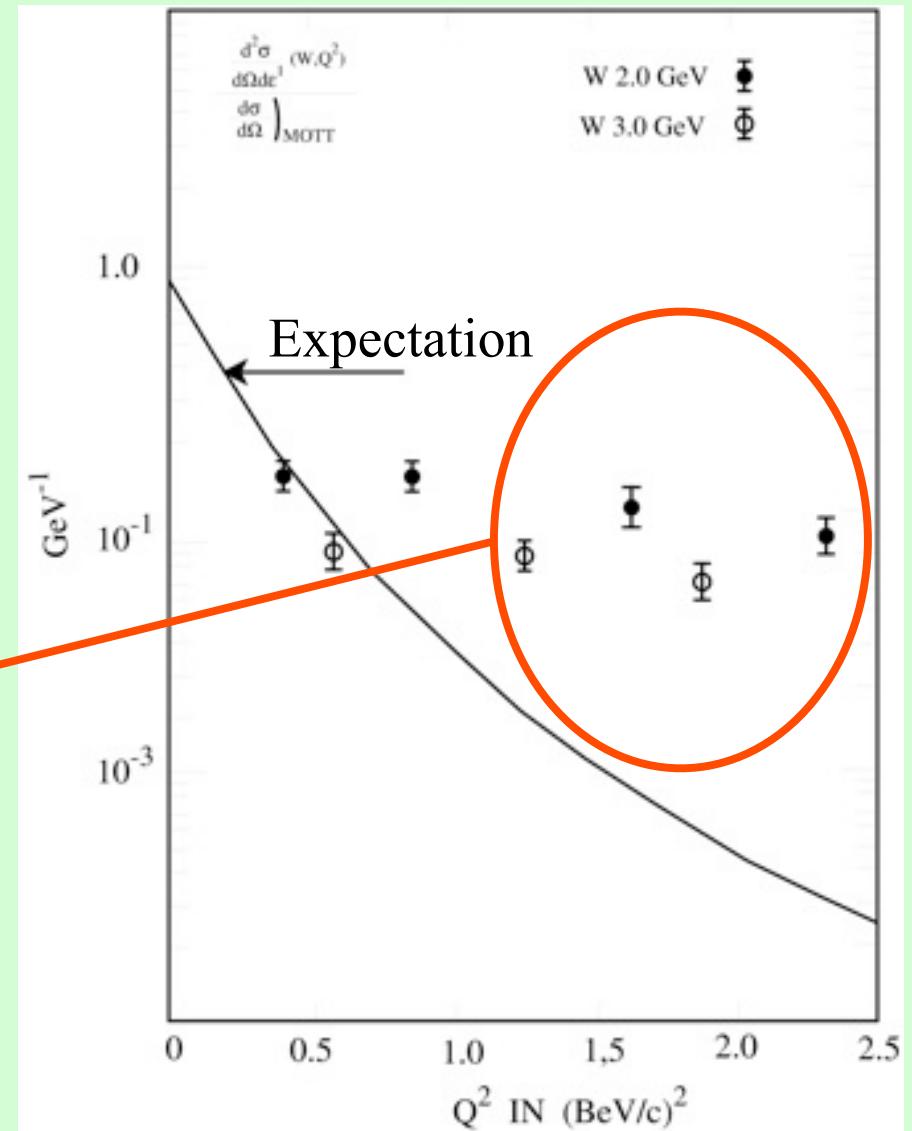
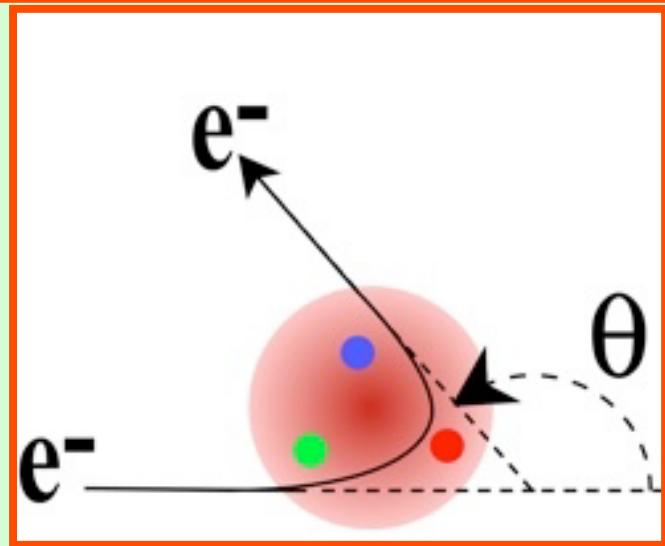
Friedman, Kendall, Taylor: Nobel Prize

# Deep inelastic electron-proton scattering

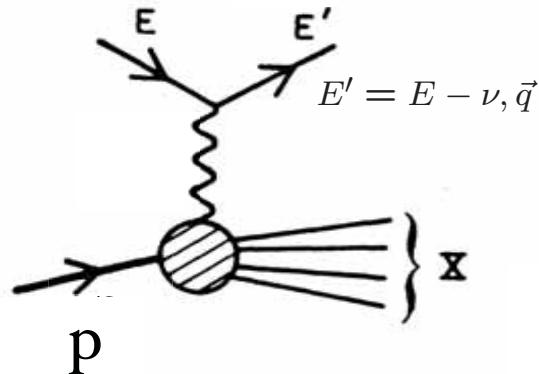


- Rutherford scattering using *very* high-energy electrons striking protons

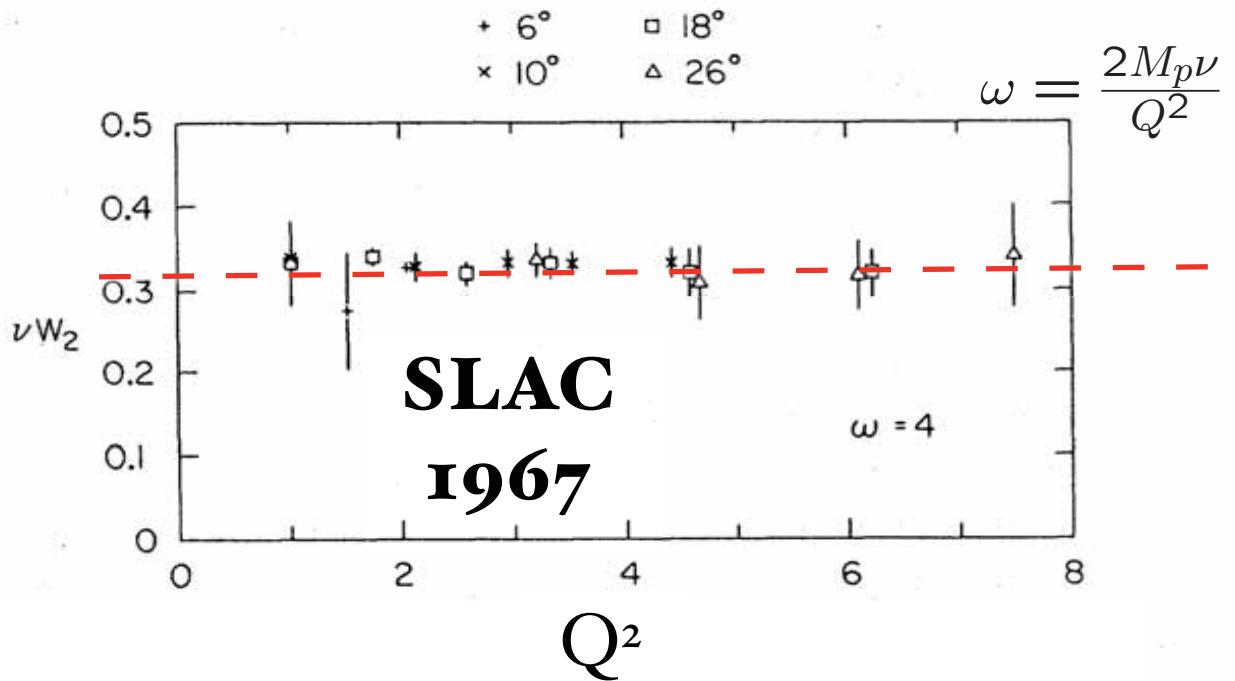
Discovery of quarks!



$$ep \rightarrow e' X$$



$$Q^2 = \vec{q}^2 - \nu^2$$



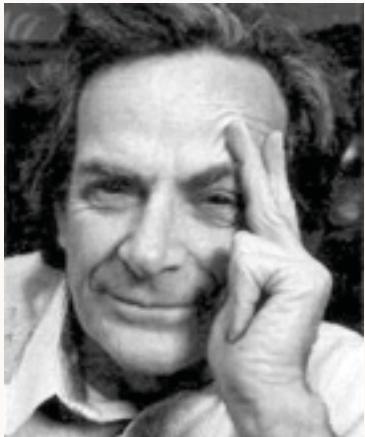
No intrinsic length scale!

Measure rate as a function of energy loss  $\nu$  and momentum transfer  $Q$

$$x_{bj} = \frac{1}{\omega_{bj}} = \frac{Q^2}{2q \cdot p}$$

Discovery of Bjorken Scaling  
Electron scatters on point-like quarks!

# Quarks in the Proton



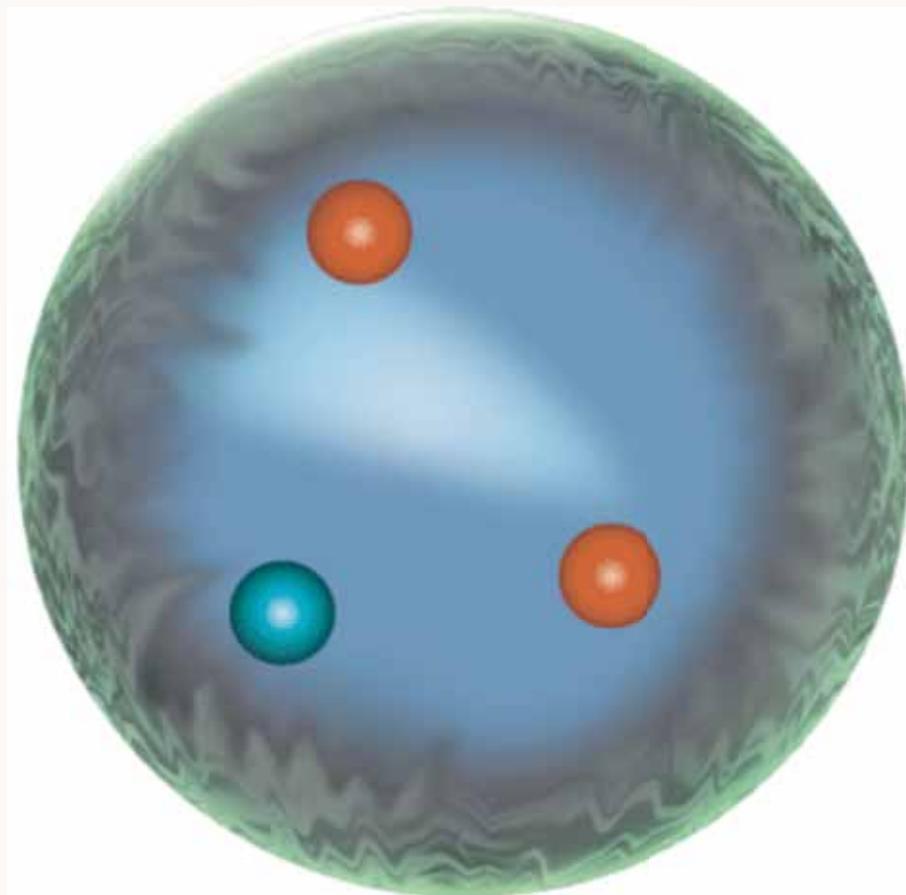
Feynman & Bjorken:  
“Parton” model



Bjorken: Scaling

**Valencia LC2010**  
**June 17, 2010**

$$\mathbf{p} = (\text{u u d})$$

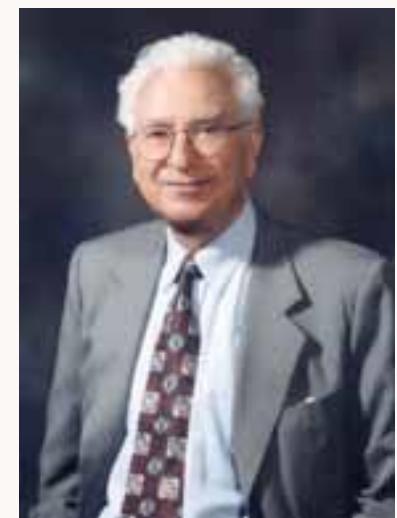


$$1 fm \\ 10^{-15} m = 10^{-13} cm$$

**QCD at the Light-Front**



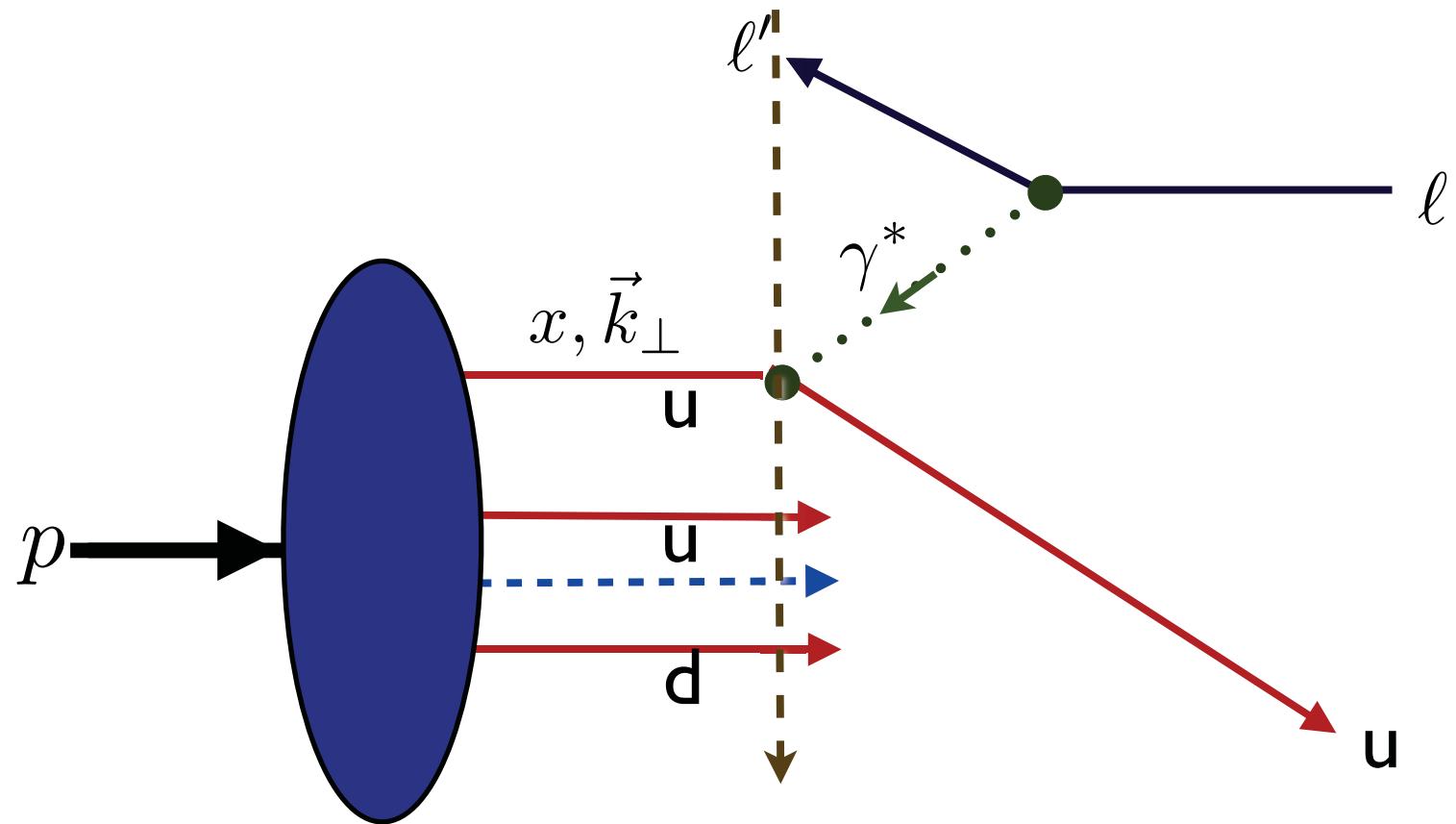
Zweig: “Aces, Deuces,  
Treys”



Gell Mann: “Three Quarks for  
Mr. Mark”

**Stan Brodsky, SLAC & CP3**

Fixed  $\tau = t + z/c$

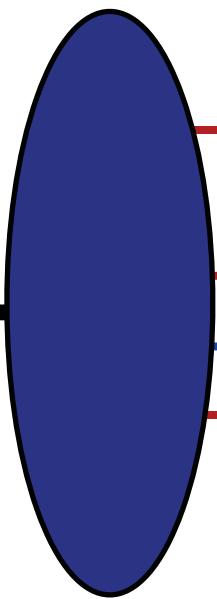


$$x = \frac{k^+}{p^+} = \frac{k^0 + k^z}{p^0 + p^z} \simeq x_{bj} = \frac{Q^2}{2p \cdot q}$$

Fixed  $\tau = t + z/c$

$$x = \frac{k^+}{P^+}$$

$$p$$



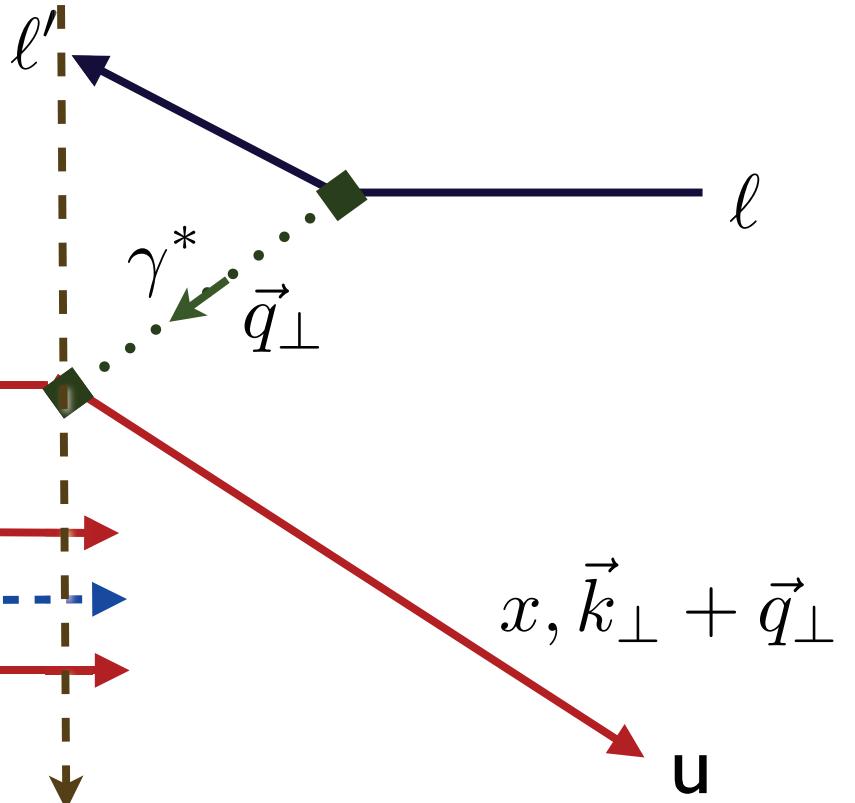
$$x, \vec{k}_\perp$$

**u**

**u**

**g**

**d**



$$p^\mu = (p^+, p^-, \vec{p}_\perp) = (P^+, \frac{M^2}{P^+}, 0_\perp)$$

$$Q^2 = \vec{q}_\perp^2$$

$$q^\mu = (q^+, q^-, \vec{q}_\perp) = (0, \frac{2q \cdot p}{P^+}, \vec{q}_\perp)$$

P-conservation

$$2q \cdot p + M^2 = \frac{(\vec{k}_\perp + \vec{q}_\perp)^2 + m^2}{x} + \frac{\vec{k}_\perp^2 + M_s^2}{1-x}$$

$$x = \frac{Q^2}{2q \cdot p} = x_{bj}$$

plus mass,  
transverse momentum  
and final-state interaction corrections

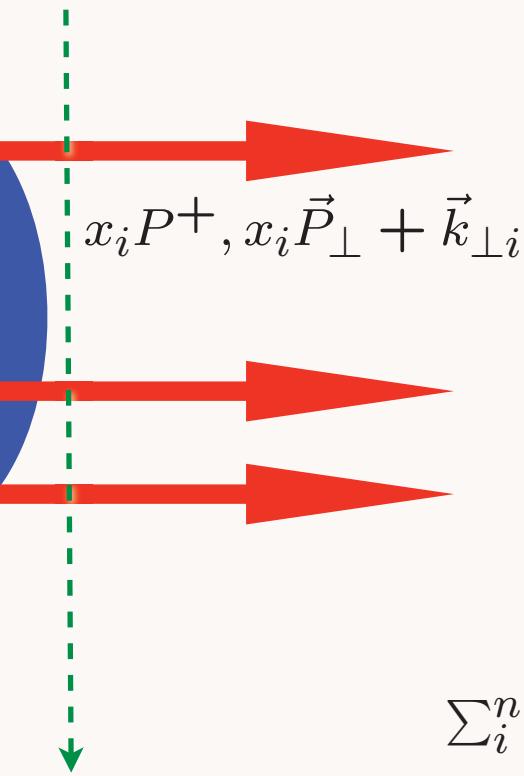
# Light-Front Wavefunctions: rigorous representation of composite systems in quantum field theory

$$x = \frac{k^+}{P^+} = \frac{k^0 + k^3}{P^0 + P^3}$$

$$P^+, \vec{P}_\perp$$

$$\Psi_n(x_i, \vec{k}_{\perp i}, \lambda_i)$$

$$\text{Fixed } \tau = t + z/c$$



$$\sum_i^n x_i = 1$$

Structure functions and other distributions  
computed from the square of the LFWFs

Goal: Predict all features from first principles

$$\sum_i^n \vec{k}_{\perp i} = \vec{0}_\perp$$

# QCD Lagrangian

## Generalization of QED

The diagram illustrates the QCD Lagrangian  $\mathcal{L}_{\text{QCD}}$  enclosed in a red box. The components are labeled as follows:

- gluon dynamics:**  $-\frac{1}{4g^2} \text{Tr}(G^{\mu\nu} G_{\mu\nu})$
- quark kinetic energy + quark-gluon dynamics:**  $\sum_{f=1}^{nf} i \bar{\psi}_f D_\mu \gamma^\mu \psi_f$
- mass term:**  $\sum_{f=1}^{nf} m_f \bar{\psi}_f \psi_f$

Annotations with arrows point to specific terms:

- An arrow from "QCD color charge" points to the term  $-\frac{1}{4g^2}$ .
- An arrow from "field strength tensor" points to  $G^{\mu\nu}$ .
- An arrow from "covariant derivative" points to  $D_\mu$ .
- An arrow from "quark field" points to  $\bar{\psi}_f \psi_f$ .
- An arrow from "gluon dynamics" points to the entire first term.
- An arrow from "quark kinetic energy + quark-gluon dynamics" points to the second term.
- An arrow from "mass term" points to the third term.

Yang Mills Gauge Principle:  
Color Rotation and Phase  
Invariance at Every Point of  
Space and Time

Scale-Invariant Coupling  
Renormalizable  
Nearly-Conformal  
Asymptotic Freedom  
Color Confinement

# QED Lagrangian

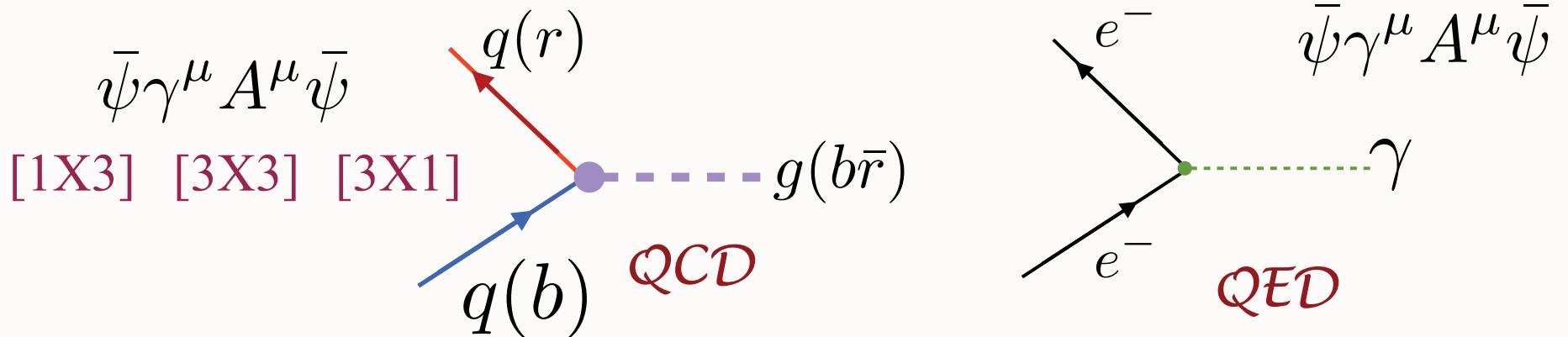
$$\mathcal{L}_{QED} = -\frac{1}{4}Tr(F^{\mu\nu}F_{\mu\nu}) + \sum_{\ell=1}^{n_\ell} i\bar{\Psi}_\ell D_\mu \gamma^\mu \Psi_\ell + \sum_{\ell=1}^{n_\ell} m_\ell \bar{\Psi}_\ell \Psi_\ell$$

$$iD^\mu = i\partial^\mu - eA^\mu \quad F^{\mu\nu} = \partial^\mu A^\nu - \partial^\nu A^\mu$$

Yang Mills Gauge Principle:  
Phase Invariance at Every  
Point of Space and Time

Scale-Invariant Coupling  
Renormalizable  
Nearly-Conformal  
Landau Pole

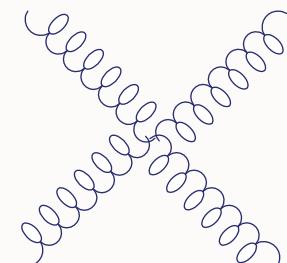
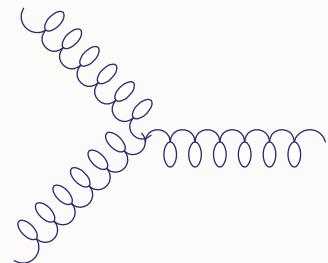
# Fundamental Couplings of QED and QCD



$$\mathcal{L}_{QCD} = -\frac{1}{4} Tr(G^{\mu\nu}G_{\mu\nu}) + \sum_{f=1}^{n_f} i\bar{\Psi}_f D_\mu \gamma^\mu \Psi_f + \sum_{f=1}^{n_f} m_f \bar{\Psi}_f \Psi_f$$

$$G^{\mu\nu} = \partial^\mu A^\nu - \partial^\nu A^\mu - g[A^\mu, A^\nu]$$

Gluon vertices



$$G^{\mu\nu} G_{\mu\nu}$$

gluon self couplings

# Angular Momentum on the Light-Front

$$J^z = \sum_{i=1}^n s_i^z + \sum_{j=1}^{n-1} l_j^z.$$

*LC gauge*

Conserved  
LF Fock state by Fock State

**Gluon orbital angular momentum defined in physical lc gauge**

$$l_j^z = -i \left( k_j^1 \frac{\partial}{\partial k_j^2} - k_j^2 \frac{\partial}{\partial k_j^1} \right)$$

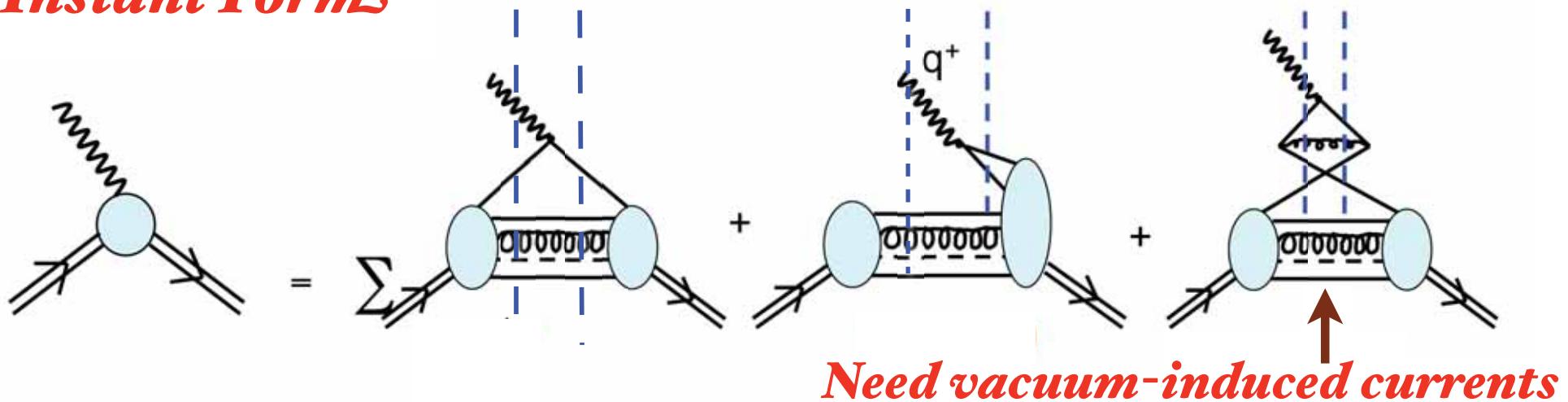
n-1 orbital angular momenta

*Orbital Angular Momentum is a property of LFWFS*

Nonzero Anomalous Moment  $\rightarrow$   
Nonzero quark orbital angular momentum!

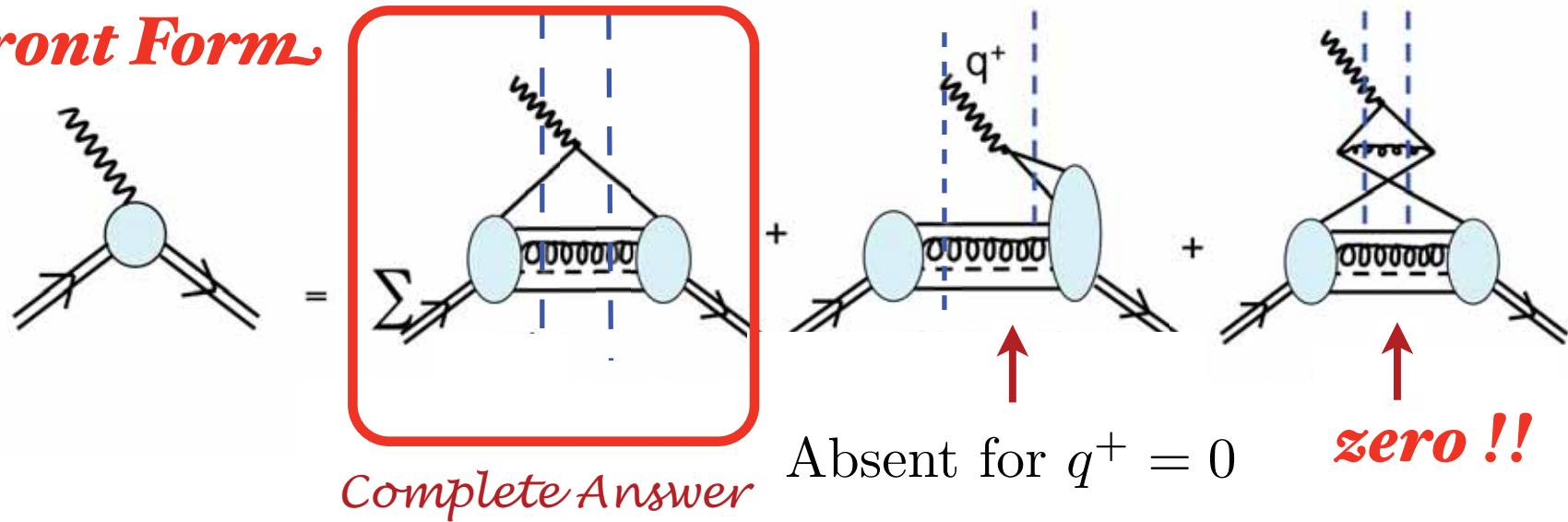
## Calculation of Form Factors in Equal-Time Theory

### Instant Form



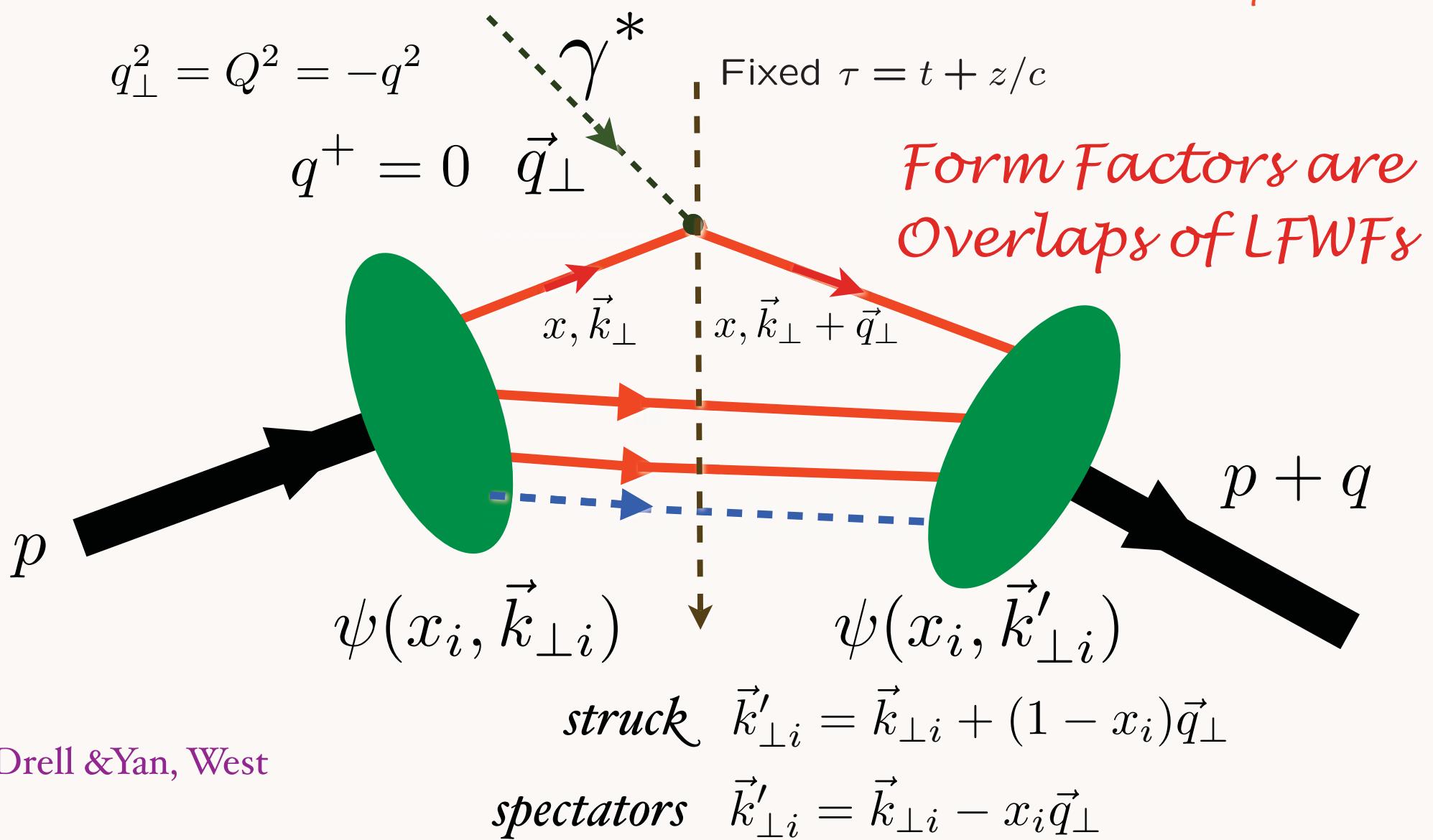
## Calculation of Form Factors in Light-Front Theory

### Front Form



$$\langle p + q | j^+(0) | p \rangle = 2p^+ F(q^2)$$

Interaction  
picture

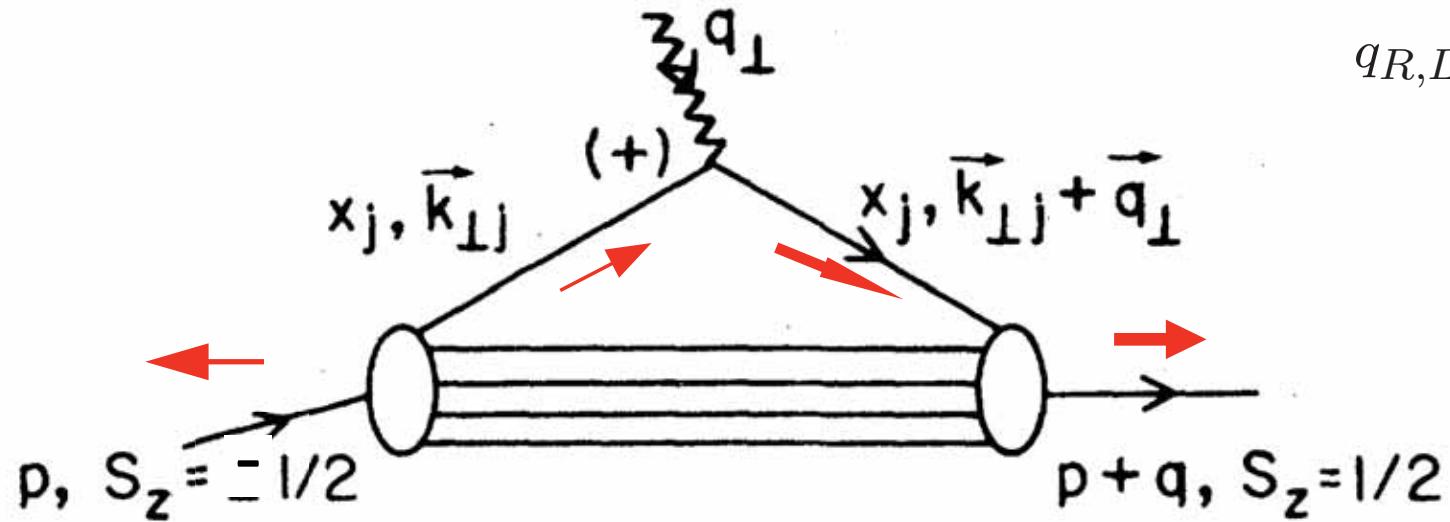


Drell & Yan, West

$$\frac{F_2(q^2)}{2M} = \sum_a \int [dx][d^2\mathbf{k}_\perp] \sum_j e_j \frac{1}{2} \times \text{Drell, sjb}$$

$$\left[ -\frac{1}{q^L} \psi_a^{\uparrow*}(x_i, \mathbf{k}'_{\perp i}, \lambda_i) \psi_a^{\downarrow}(x_i, \mathbf{k}_{\perp i}, \lambda_i) + \frac{1}{q^R} \psi_a^{\downarrow*}(x_i, \mathbf{k}'_{\perp i}, \lambda_i) \psi_a^{\uparrow}(x_i, \mathbf{k}_{\perp i}, \lambda_i) \right]$$

$$\mathbf{k}'_{\perp i} = \mathbf{k}_{\perp i} - x_i \mathbf{q}_{\perp} \quad \mathbf{k}'_{\perp j} = \mathbf{k}_{\perp j} + (1 - x_j) \mathbf{q}_{\perp}$$

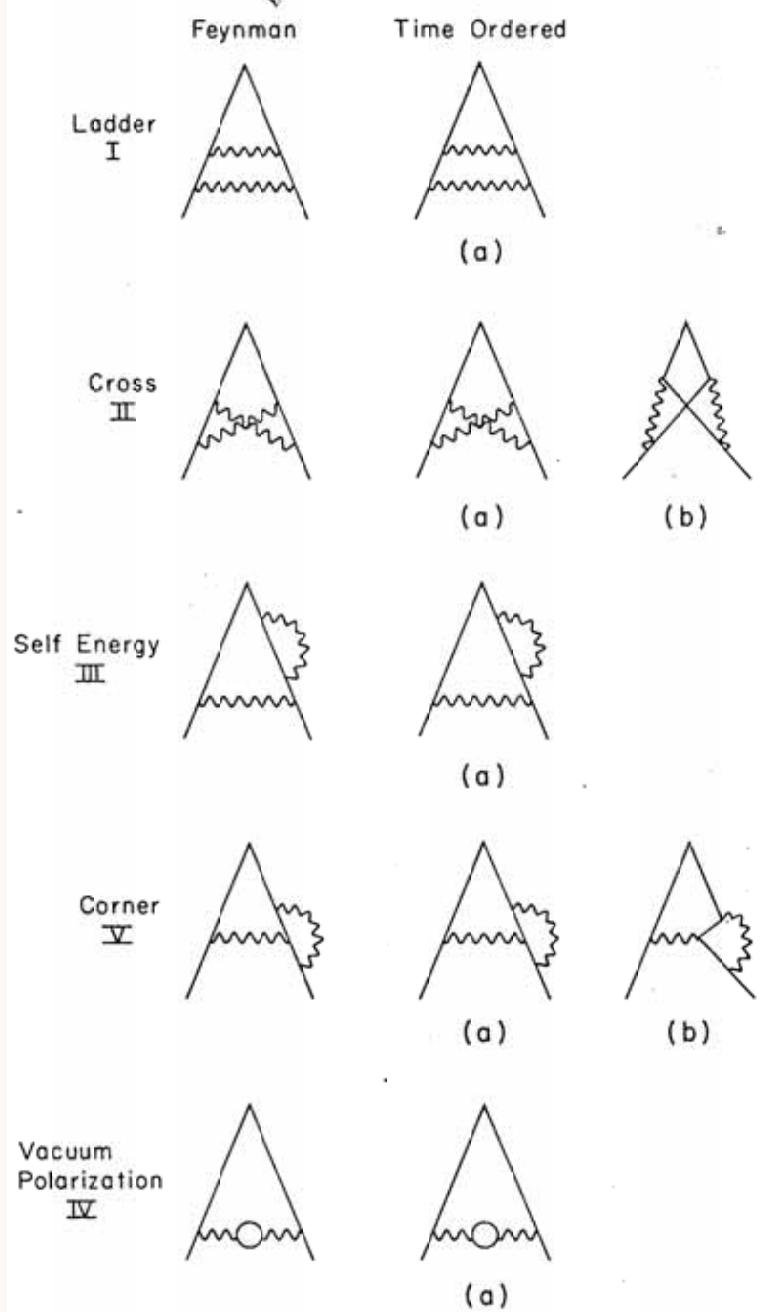


Must have  $\Delta \ell_z = \pm 1$  to have nonzero  $F_2(q^2)$

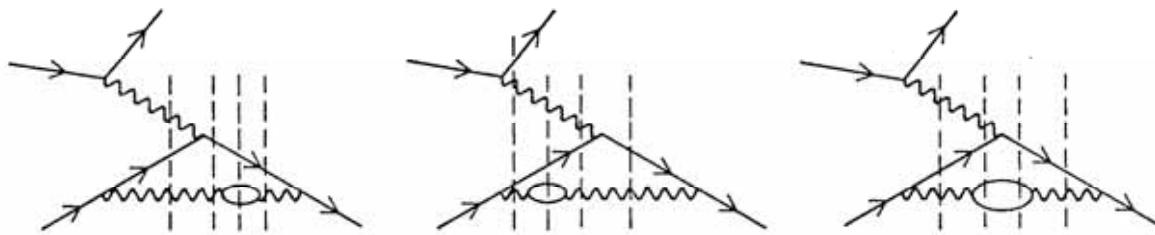
Nonzero Proton Anomalous Moment  $\rightarrow$   
Nonzero orbital quark angular momentum

# QED $g-2$ in LFPth

Roskies, Suaya, and sjb

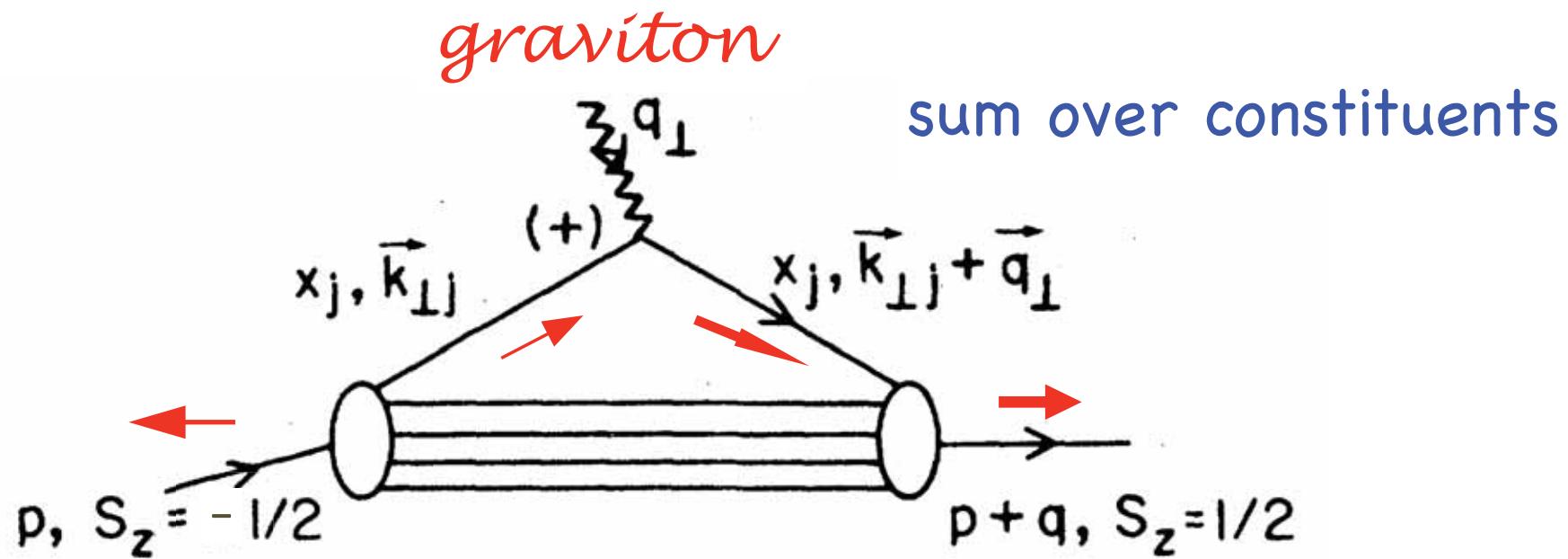


Alternate denominator renormalization



# Anomalous gravitomagnetic moment $B(0)$

Terayev, Okun, et al:  $B(0)$  Must vanish because of Equivalence Theorem



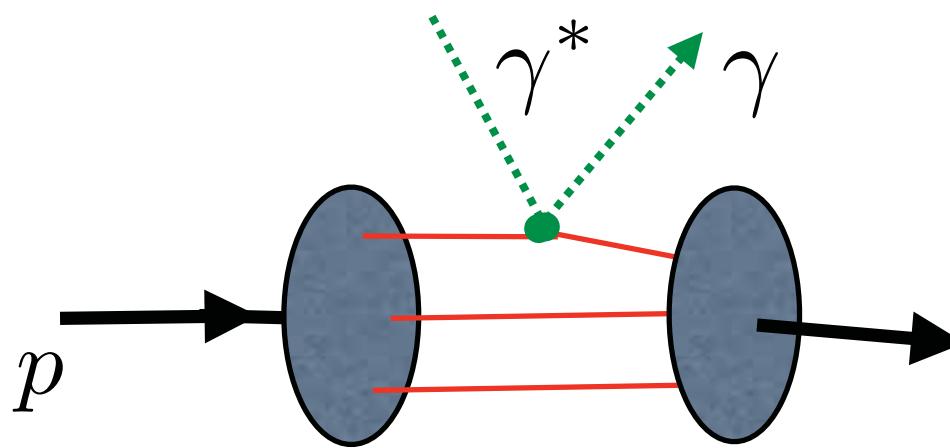
Hwang, Schmidt, sjb;  
Holstein et al

$$B(0) = 0$$

Each Fock State

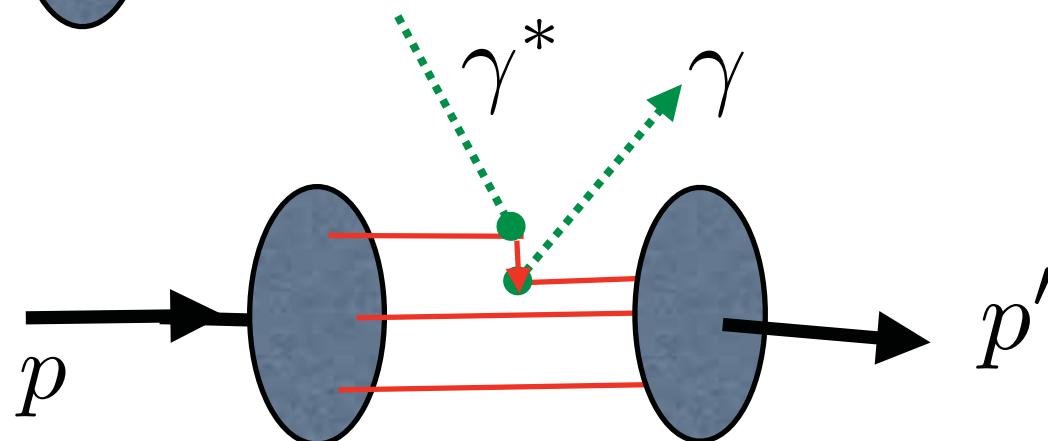
# *J=0 Fixed Pole Contribution to DVCS*

- $J=0$  fixed pole -- direct test of QCD locality -- from seagull or instantaneous contribution to Feynman propagator



Szczepaniak, Llanes-Estrada, sjb

Close, Gunion, sjb

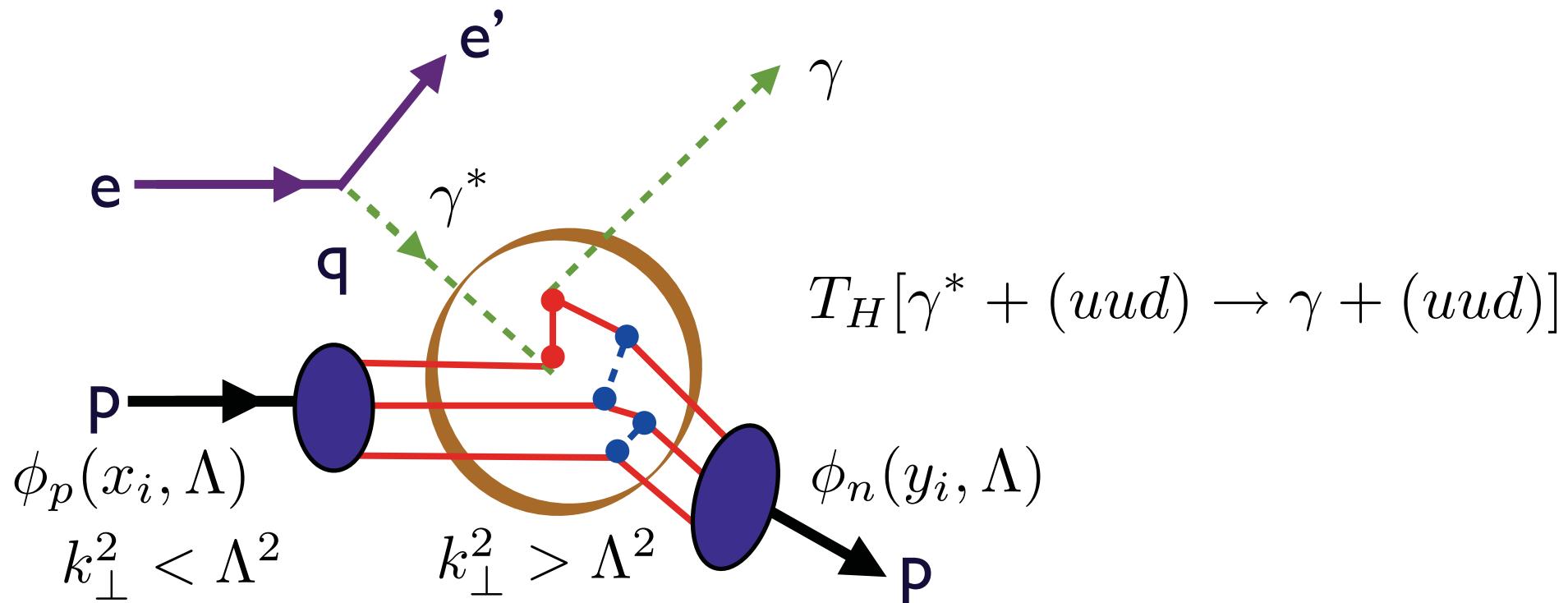


Real amplitude, independent of  $Q^2$  at fixed  $t$

*QCD Factorization*  
*DVCS in hard-scattering domain*

$$ep \rightarrow e' \gamma p$$

Lepage, sjb



$$T = \int_0^1 dx \int_0^1 dy \int_0^1 dz \phi_p(x, \Lambda) T_H(x, y, z; Q^2, s, t; \Lambda) \phi_n(y, \Lambda) \phi_\pi^+(z, \Lambda)$$

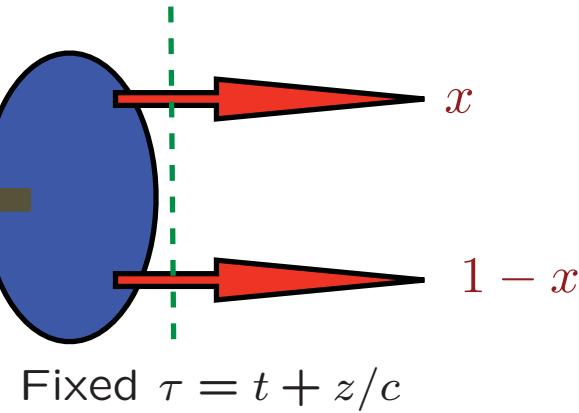
**Universal distribution amplitudes.**  
**Renormalization Group Invariance:**  
**Renormalization scale is unambiguous -- BLM**

$J=0$  Fixed pole from instantaneous gluon

# Hadron Distribution Amplitudes

$$\phi_M(x, Q) = \int^Q d^2 \vec{k} \psi_{q\bar{q}}(x, \vec{k}_\perp)$$

$$\sum_i x_i = 1$$

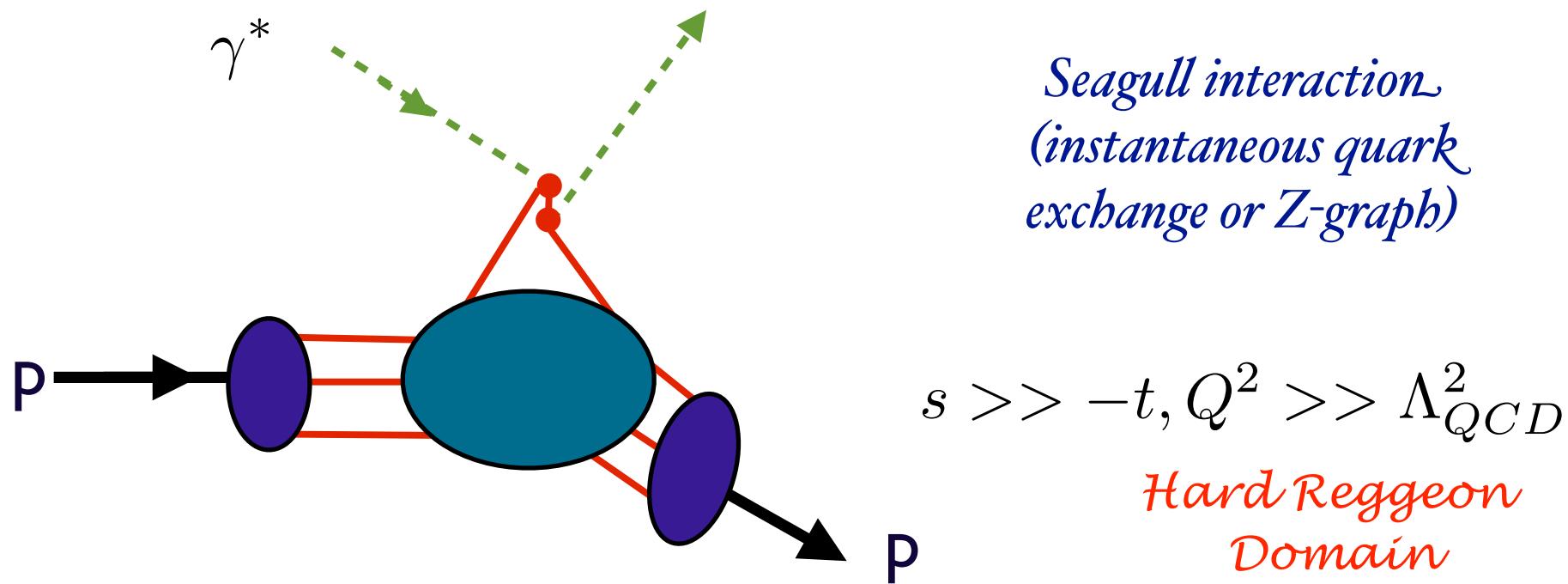


$$k_\perp^2 < Q^2$$

- Fundamental gauge invariant non-perturbative input to hard exclusive processes, heavy hadron decays. Defined for Mesons, Baryons *Lepage, sjb*
- Evolution Equations from PQCD, OPE *Efremov, Radyushkin*, *Sachrajda, Frishman Lepage, sjb*
- Conformal Invariance *Braun, Gardi*
- Compute from valence light-front wavefunction in light-cone gauge

# Deeply Virtual Compton Scattering

$$\gamma^* p \rightarrow \gamma p$$



$$T(\gamma^*(q)p \rightarrow \gamma(k) + p) \sim \epsilon \cdot \epsilon' \sum_R s_R^\alpha(t) \beta_R(t)$$

$$\alpha_R(t) \rightarrow 0$$

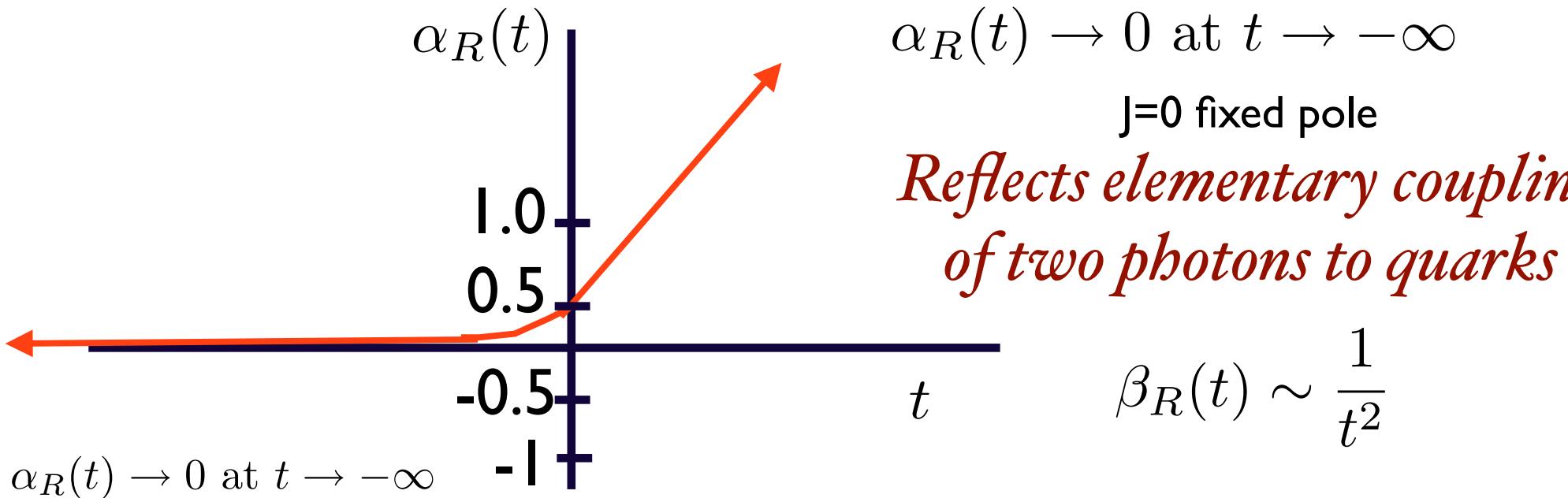
*Reflects elementary coupling of two photons to quarks*

$$\beta_R(t) \sim \frac{1}{t^2}$$

$$\frac{d\sigma}{dt} \sim \frac{1}{s^2} \frac{1}{t^4} \sim \frac{1}{s^6} \text{ at fixed } \frac{Q^2}{s}, \frac{t}{s}$$

# Regge domain

$$T(\gamma^* p \rightarrow \pi^+ n) \sim \epsilon \cdot p_i \sum_R s_R^\alpha(t) \beta_R(t) \quad s \gg -t, Q^2$$



$$\frac{d\sigma}{dt} (\gamma^* p \rightarrow \gamma p) \rightarrow \frac{1}{s^2} \beta_R^2(t) \sim \frac{1}{s^2 t^4} \sim \frac{1}{s^6} \text{ at fixed } \frac{t}{s}, \frac{Q^2}{s}$$

Fundamental test of QCD

# *J=0 Fixed pole in real and virtual Compton scattering*

Damashek, Gilman  
Close, Gunion, sjb  
Llanes-Estrada,  
Szczepaniak, sjb

Effective two-photon contact term

Seagull for scalar quarks

Real phase

$$M = s^0 \sum e_q^2 F_q(t)$$

Independent of  $Q^2$  at fixed  $t$

$\langle 1/x \rangle$  Moment: Related to Feynman-Hellman Theorem

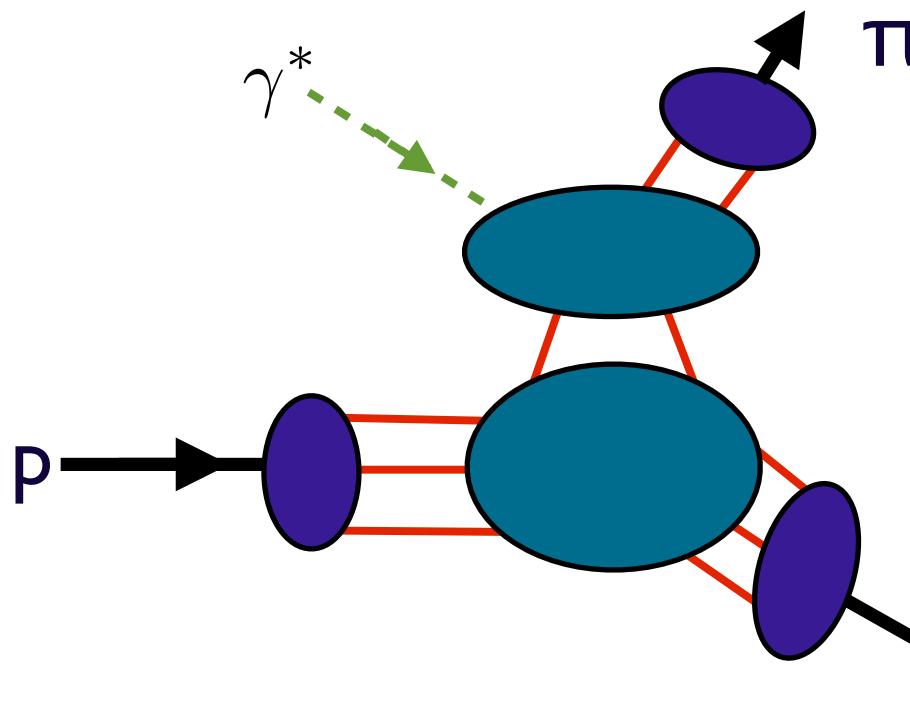
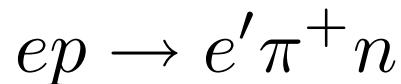
Fundamental test of local gauge theory

No ambiguity in D-term

$Q^2$ -independent contribution to Real DVCS amplitude

$$s^2 \frac{d\sigma}{dt} (\gamma^* p \rightarrow \gamma p) = F^2(t)$$

# Exclusive Electroproduction



*Hard Reggeon Domain*

$$s \gg -t, Q^2 \gg \Lambda_{QCD}^2$$

$$T(\gamma^* p \rightarrow \pi^+ n) \sim \epsilon \cdot p_i \sum_R s_R^\alpha(t) \beta_R(t)$$

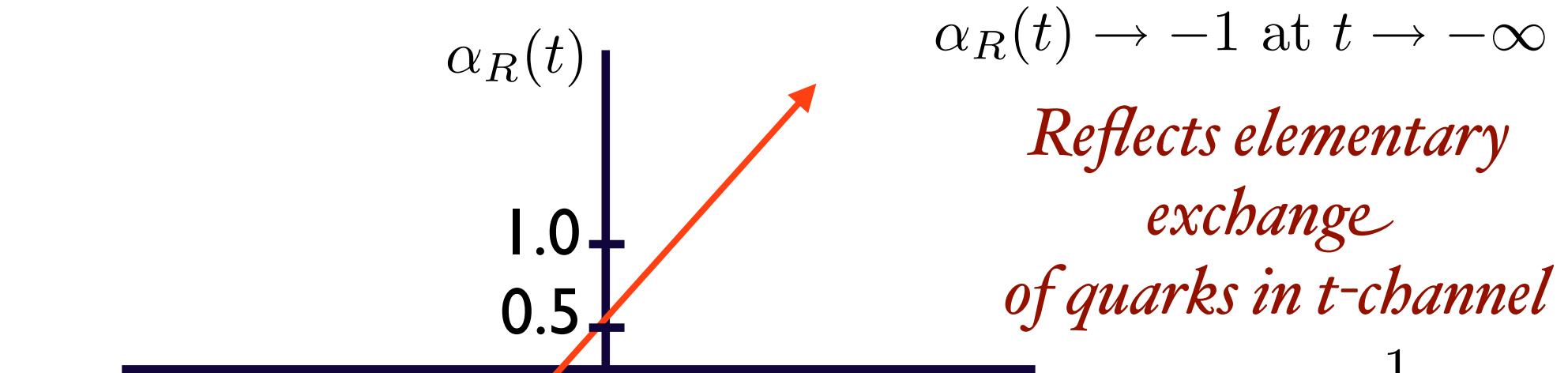
$\alpha_R(t) \rightarrow -1$     *Reflects elementary exchange of quarks in t-channel*

$$\beta_R(t) \sim \frac{1}{t^2}$$

$$\frac{d\sigma}{dt} \sim \frac{1}{s^7} \text{ at fixed } \frac{Q^2}{s}, \frac{t}{s}$$

# Regge domain

$$T(\gamma^* p \rightarrow \pi^+ n) \sim \epsilon \cdot p_i \sum_R s_R^\alpha(t) \beta_R(t) \quad s \gg -t, Q^2$$



*Reflects elementary exchange of quarks in t-channel*

$$\beta_R(t) \sim \frac{1}{t^2}$$

$$\frac{d\sigma}{dt}(\gamma^* p \rightarrow \pi^+ n) \rightarrow \frac{1}{s^3} \beta_R^2(t)$$

$$\frac{d\sigma}{dt} \sim \frac{1}{s^3} \frac{1}{t^4} \sim \frac{1}{s^7} \text{ at fixed } \frac{Q^2}{s}, \frac{t}{s}$$

*Fundamental test of QCD*

$$|p, S_z\rangle = \sum_{n=3} \Psi_n(x_i, \vec{k}_{\perp i}, \lambda_i) |n; \vec{k}_{\perp i}, \lambda_i\rangle$$

*sum over states with n=3, 4, ... constituents*

The Light Front Fock State Wavefunctions

$$\Psi_n(x_i, \vec{k}_{\perp i}, \lambda_i)$$

are boost invariant; they are independent of the hadron's energy and momentum  $P^\mu$ .

The light-cone momentum fraction

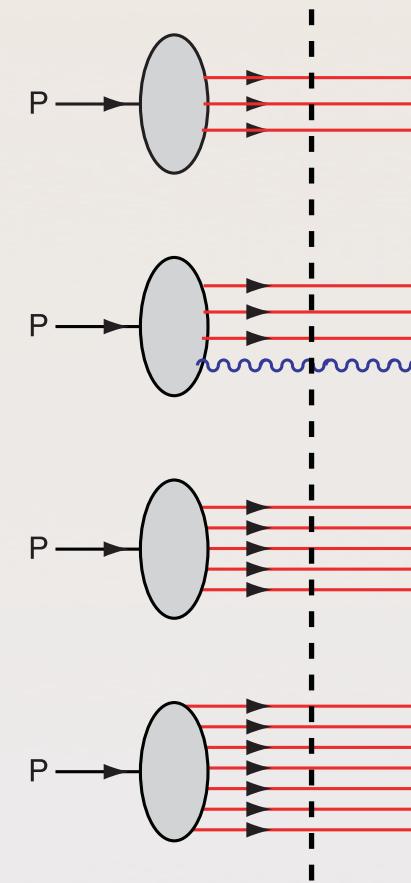
$$x_i = \frac{k_i^+}{p^+} = \frac{k_i^0 + k_i^z}{P^0 + P^z}$$

are boost invariant.

$$\sum_i^n k_i^+ = P^+, \quad \sum_i^n x_i = 1, \quad \sum_i^n \vec{k}_i^\perp = \vec{0}^\perp.$$

*Intrinsic heavy quarks  
 $c(x), b(x)$  at high  $x$  !*

$$\bar{s}(x) \neq s(x) \\ \bar{u}(x) \neq \bar{d}(x)$$



*Fixed LF time*

Mueller: gluon Fock states → BFKL Pomeron *Hidden Color*

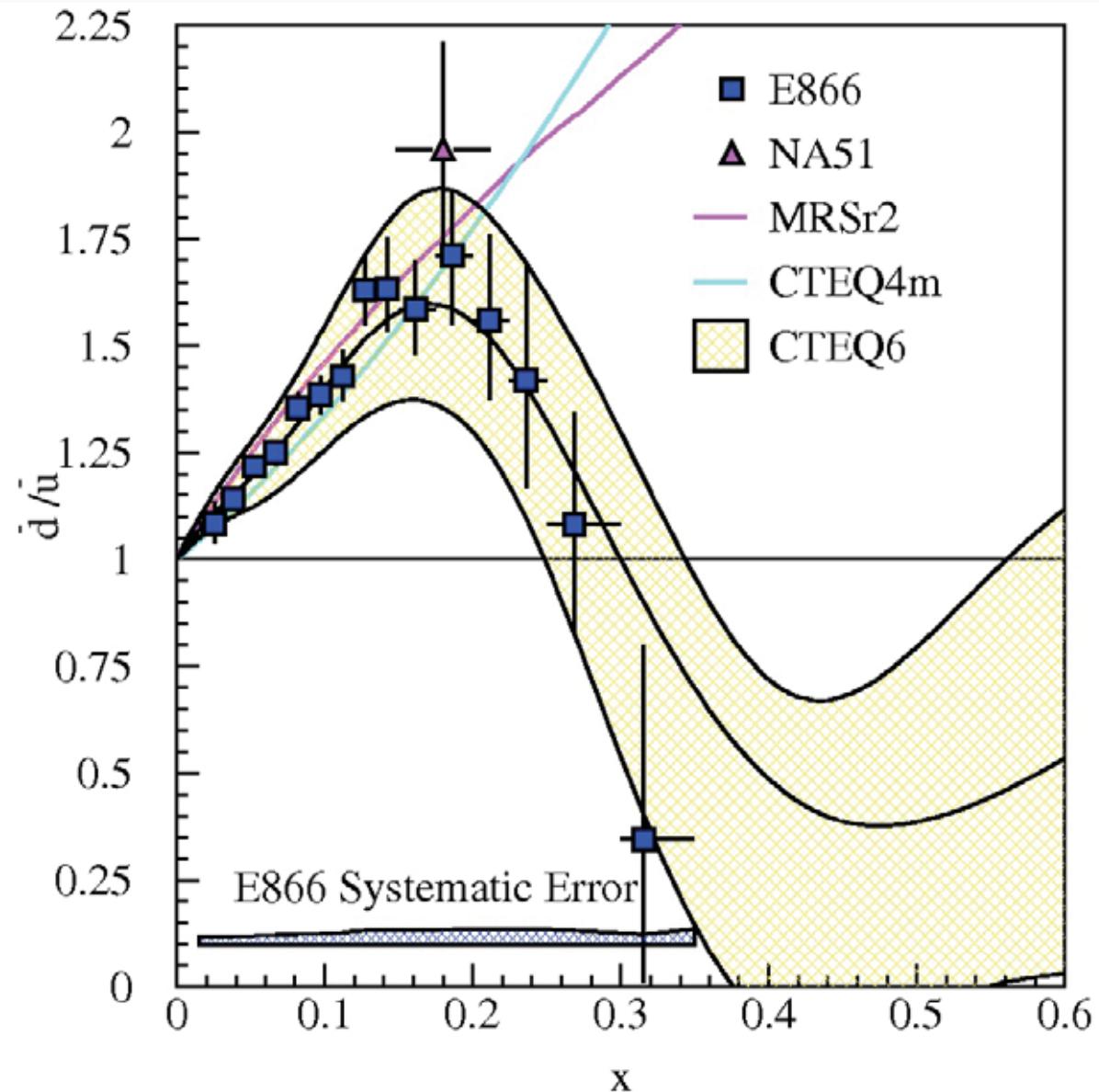
■ E866/NuSea (Drell-Yan)

$$\bar{d}(x) \neq \bar{u}(x)$$

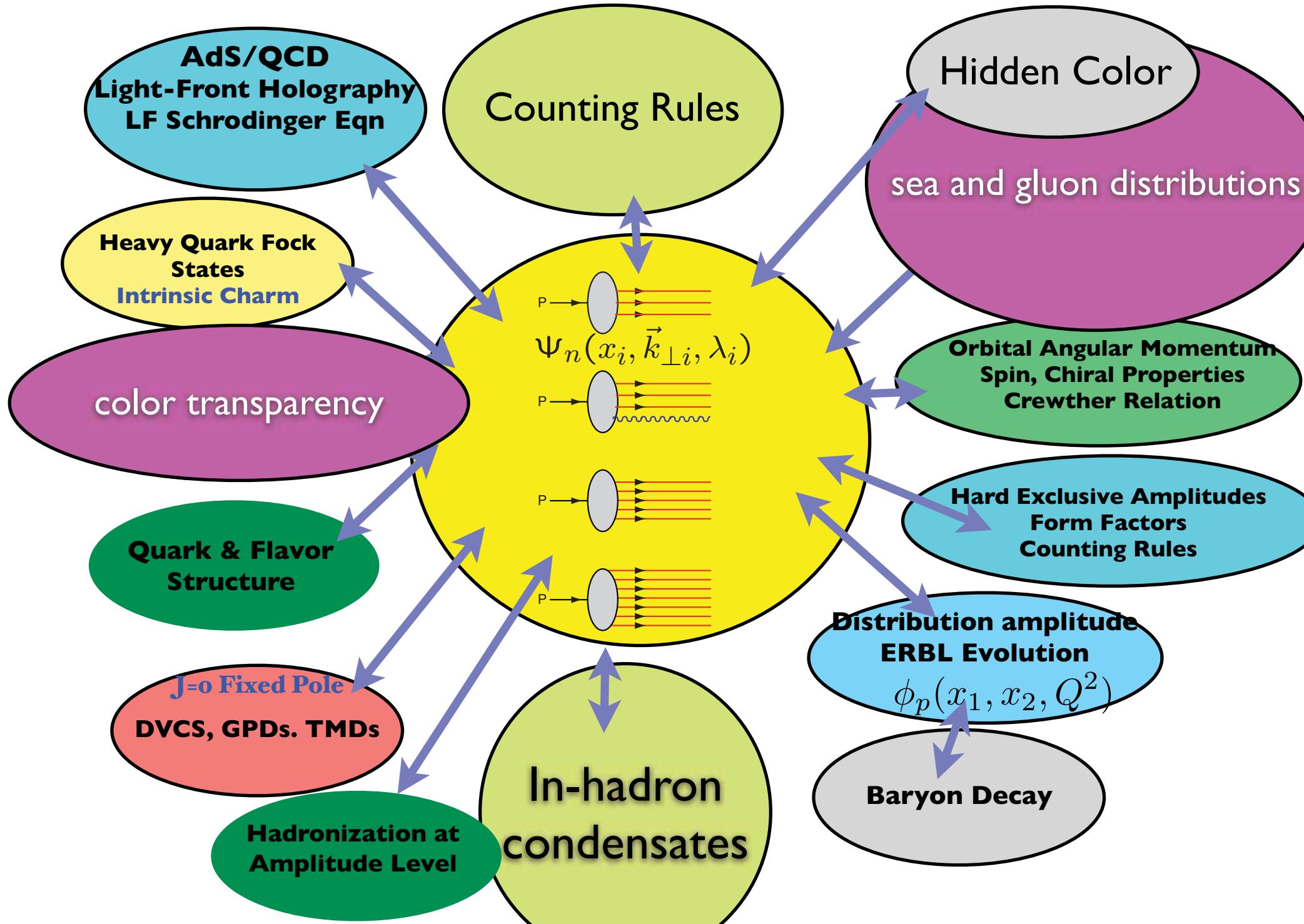
$$s(x) \neq \bar{s}(x)$$

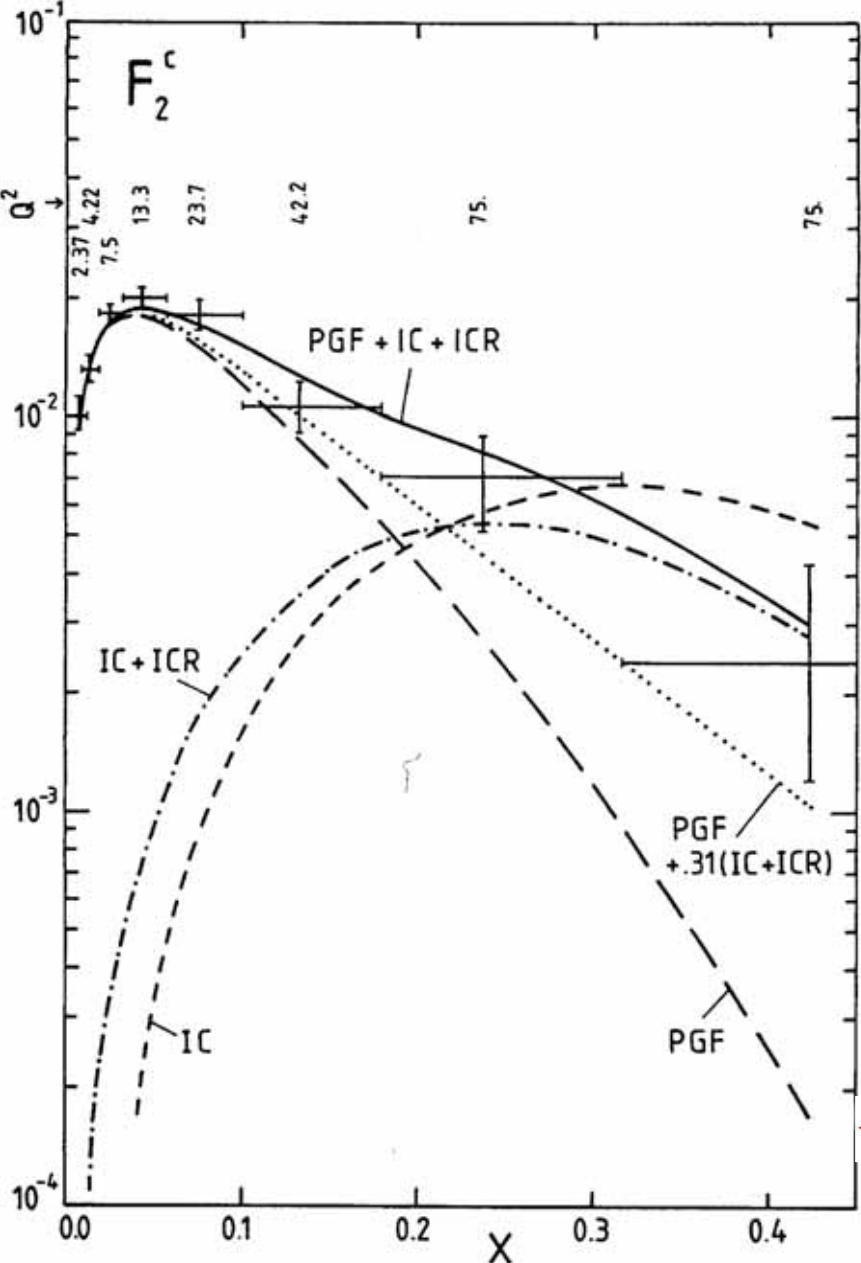
*Intrinsic glue, sea,  
heavy quarks*

$$\bar{d}(x)/\bar{u}(x) \text{ for } 0.015 \leq x \leq 0.35$$



# *QCD and the LF Hadron Wavefunctions*

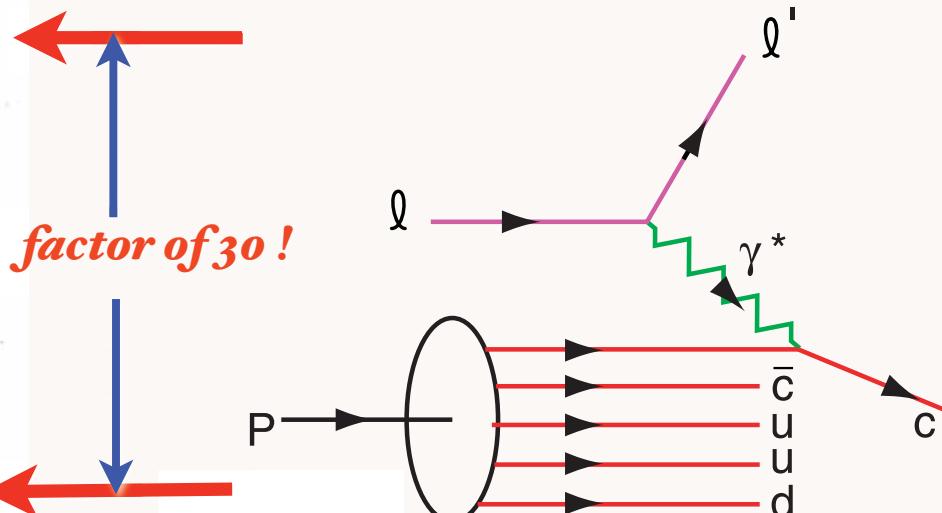




## Measurement of Charm Structure Function

J. J. Aubert et al. [European Muon Collaboration], “Production Of Charmed Particles In 250-Gev Mu+ - Iron Interactions,” Nucl. Phys. B 213, 31 (1983).

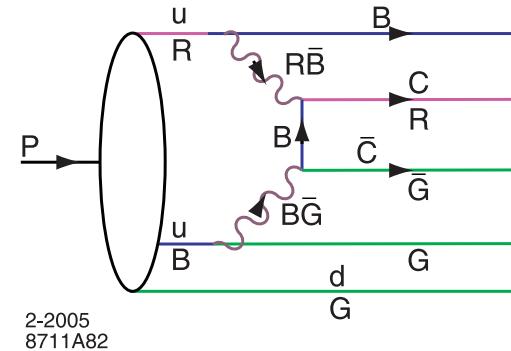
First Evidence for Intrinsic Charm  
*Never been checked!*



**DGLAP / Photon-Gluon Fusion: factor of 30 too small**

# Intrinsic Heavy-Quark Fock States

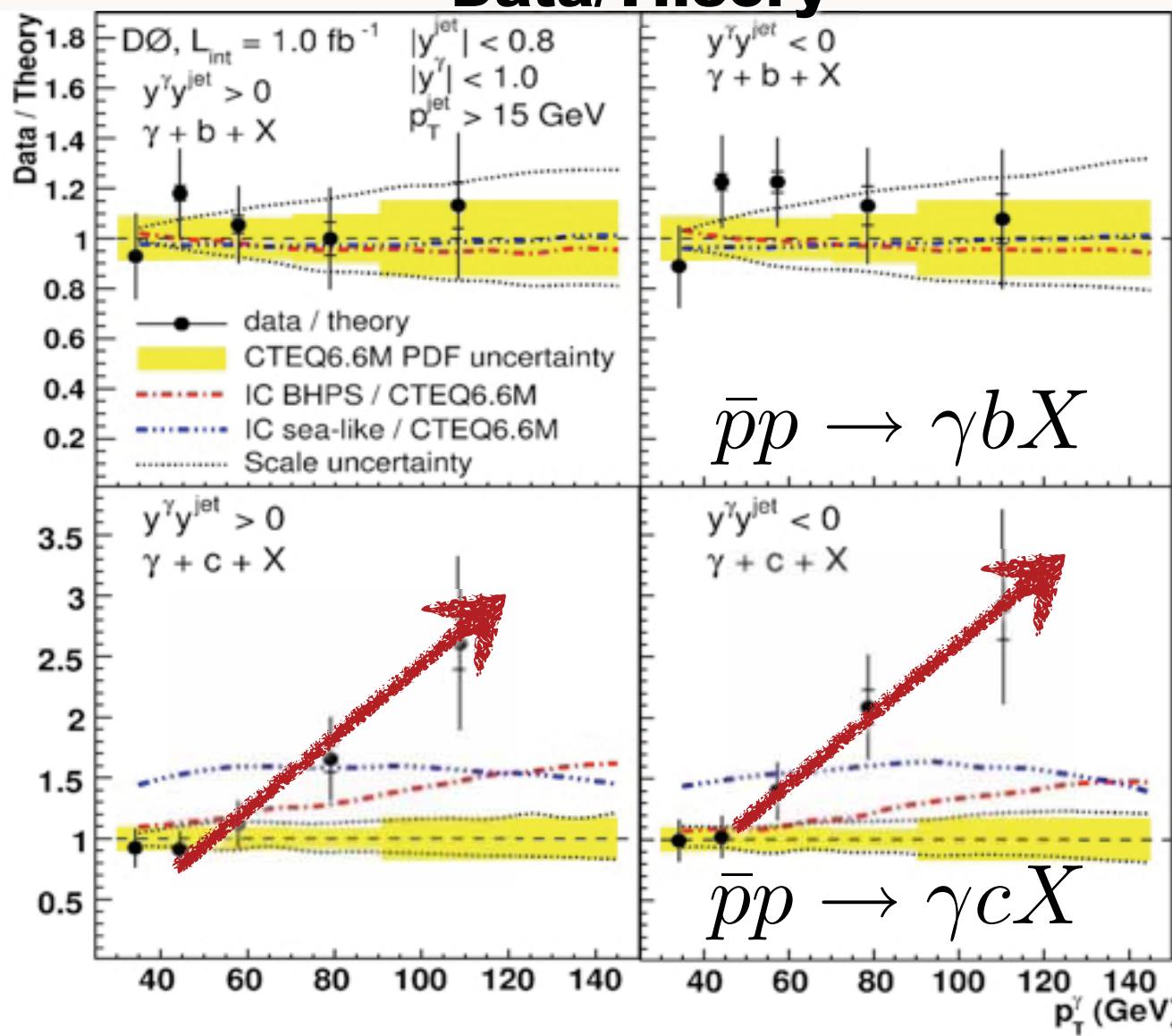
- Rigorous prediction of QCD, OPE
- Color-Octet Color-Octet Fock State!
- Probability  $P_{Q\bar{Q}} \propto \frac{1}{M_Q^2}$      $P_{Q\bar{Q}Q\bar{Q}} \sim \alpha_s^2 P_{Q\bar{Q}}$      $P_{c\bar{c}/p} \simeq 1\%$
- Large Effect at high  $x$
- Greatly increases kinematics of colliders such as Higgs production  
(Kopeliovich, Schmidt, Soffer, sjb)
- Severely underestimated in conventional parameterizations of heavy quark distributions (Pumplin, Tung)
- Many empirical tests



M. Polyakov et al.  
OPE

Measurement of  $\gamma + b + X$  and  $\gamma + c + X$  Production Cross Sections  
in  $p\bar{p}$  Collisions at  $\sqrt{s} = 1.96$  TeV

## Data/Theory



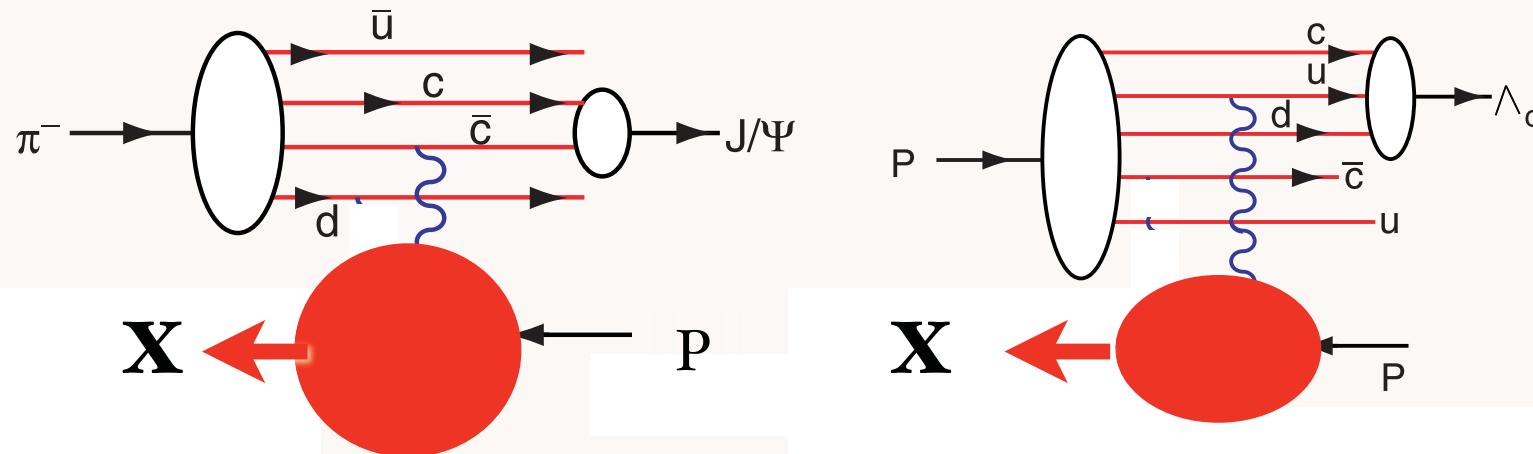
$$\frac{\Delta\sigma(\bar{p}p \rightarrow \gamma c X)}{\Delta\sigma(\bar{p}p \rightarrow \gamma b X)}$$

Ratio  
insensitive to  
gluon PDF,  
scales

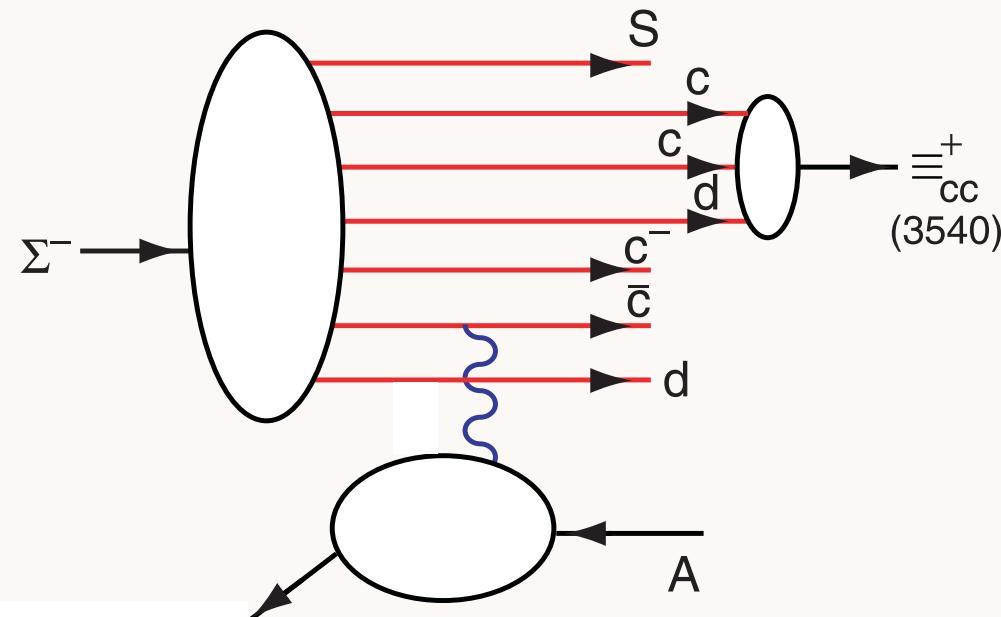
Signal for  
significant IC  
at  $x > 0.1$

- EMC data:  $c(x, Q^2) > 30 \times$  DGLAP  
 $Q^2 = 75 \text{ GeV}^2, x = 0.42$
- High  $x_F$   $pp \rightarrow J/\psi X$
- High  $x_F$   $pp \rightarrow J/\psi J/\psi X$
- High  $x_F$   $pp \rightarrow \Lambda_c X$  ISR
- High  $x_F$   $pp \rightarrow \Lambda_b X$  ISR
- High  $x_F$   $pp \rightarrow \Xi(ccd)X$  (SELEX)

# Leading Hadron Production from Intrinsic Charm



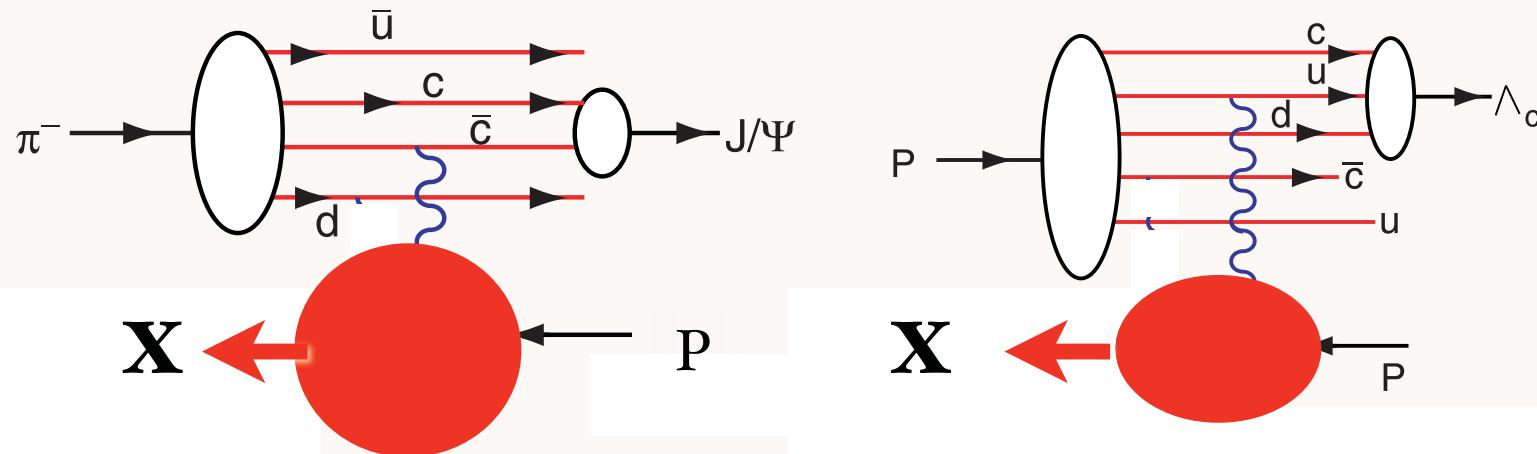
Coalescence of Comoving Charm and Valence Quarks  
Produce  $J/\psi$ ,  $\Lambda_c$  and other Charm Hadrons at High  $x_F$



## Production of a Double-Charm Baryon

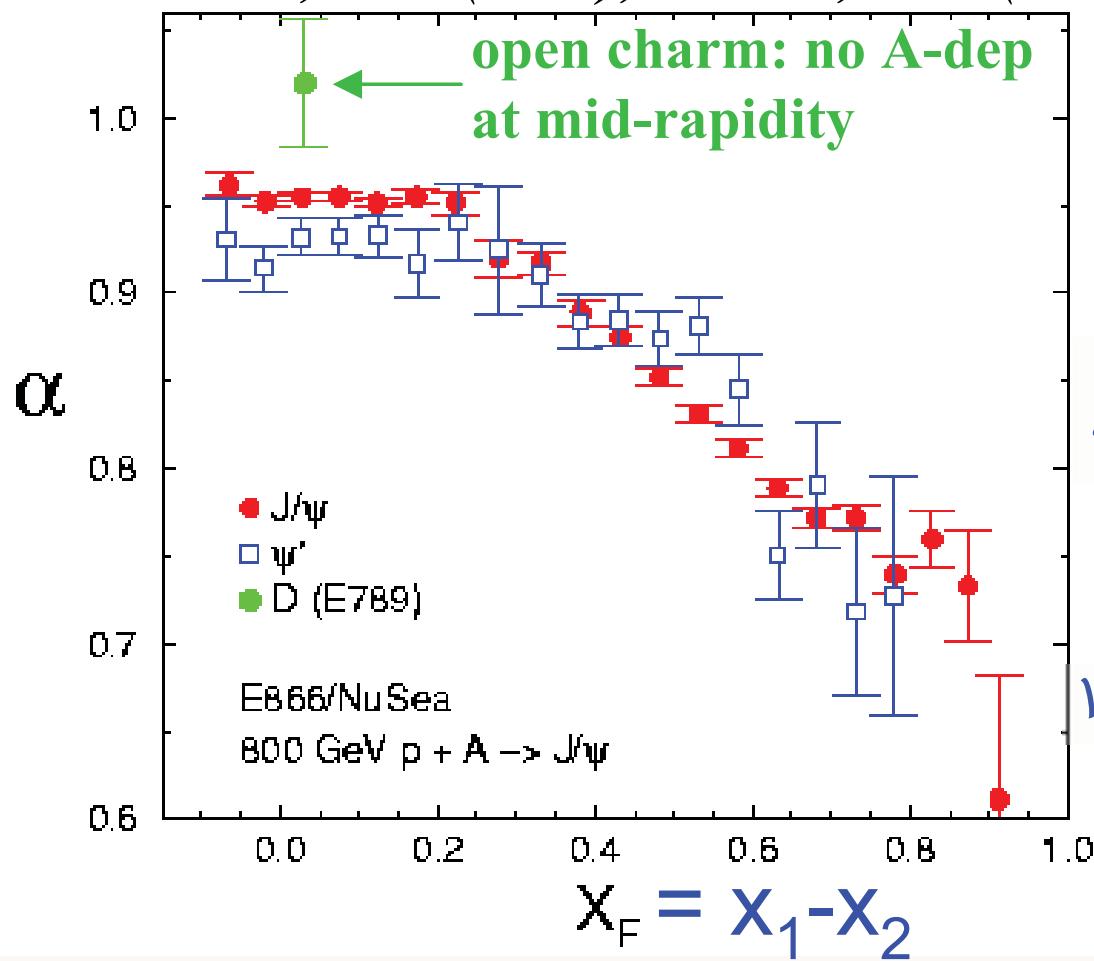
**SELEX high  $x_F$**        $\langle x_F \rangle = 0.33$

# Leading Hadron Production from Intrinsic Charm



Coalescence of Comoving Charm and Valence Quarks  
Produce  $J/\Psi$ ,  $\Lambda_c$  and other Charm Hadrons at High  $x_F$

800 GeV p-A (FNAL)  $\sigma_A = \sigma_p * A^\alpha$   
*PRL 84, 3256 (2000); PRL 72, 2542 (1994)*



$$\frac{d\sigma}{dx_F}(pA \rightarrow J/\psi X)$$

Remarkably Strong Nuclear Dependence for Fast Charmonium

Violation of PQCD Factorization!

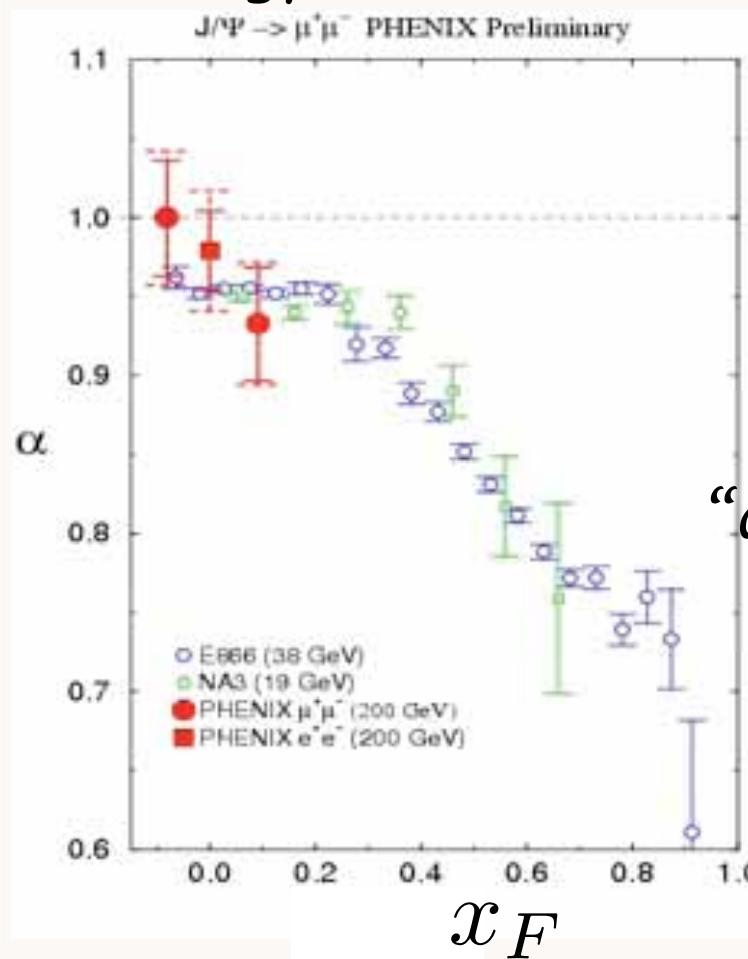
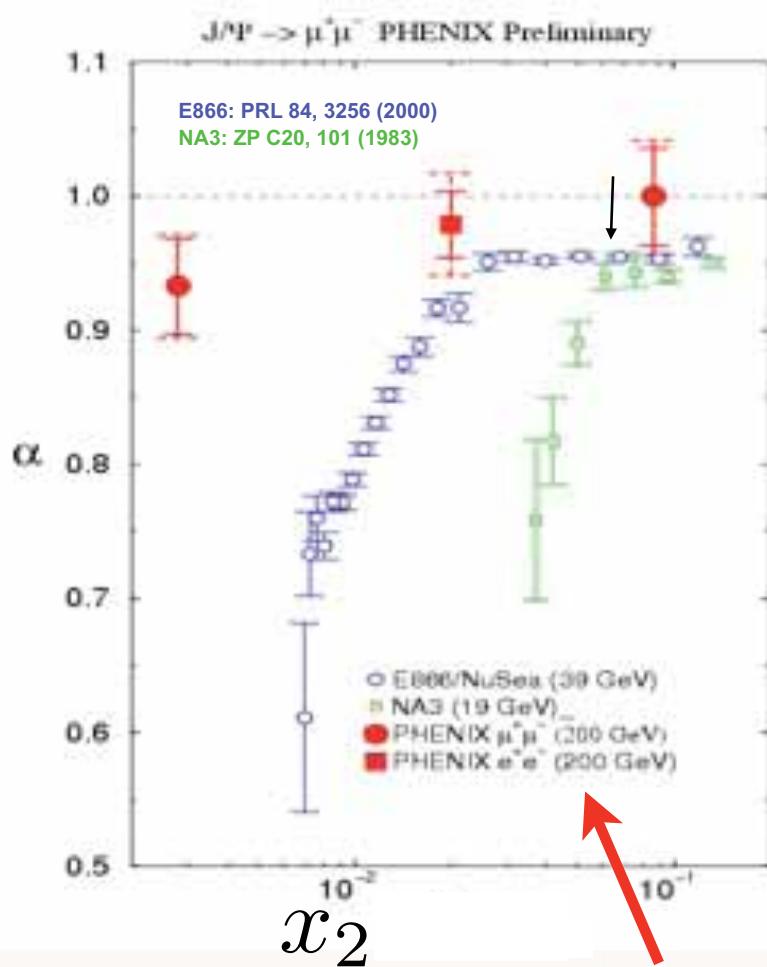
Violation of factorization in charm hadroproduction.

[P. Hoyer, M. Vanttilen \(Helsinki U.\)](#), [U. Sukhatme \(Illinois U., Chicago\)](#). HU-TFT-90-14, May 1990. 7pp.  
Published in Phys.Lett.B246:217-220,1990

# J/ψ nuclear dependence vrs rapidity, xAu, xF

M.Leitch

## PHENIX compared to lower energy measurements



Huge  
“absorption”  
effect

Klein,Vogt, PRL 91:142301,2003  
Kopeliovich, NP A696:669,2001

Violates PQCD  
factorization!

$$\frac{d\sigma}{dx_F}(pA \rightarrow J/\psi X)$$

Hoyer, Sukhatme, Vanttilinen

QCD at the Light-Front

Valencia LC2010

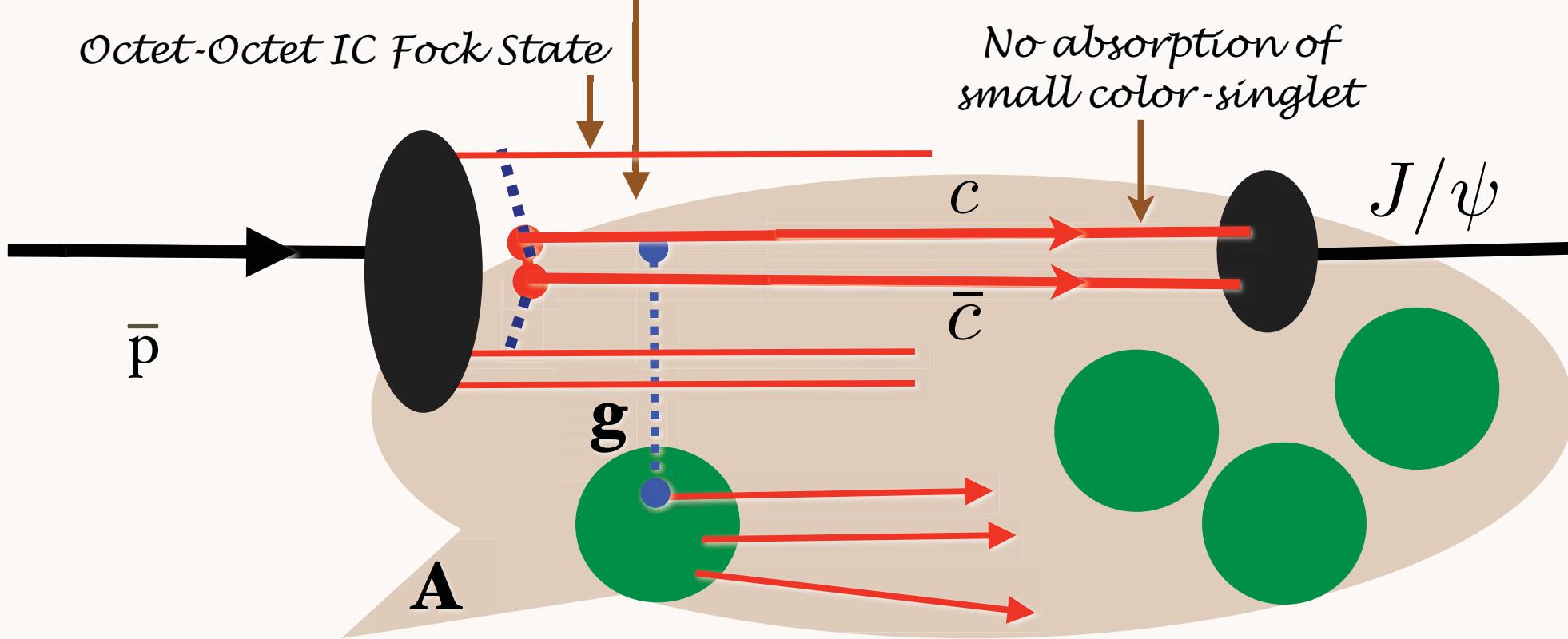
June 17, 2010

Stan Brodsky, SLAC & CP3

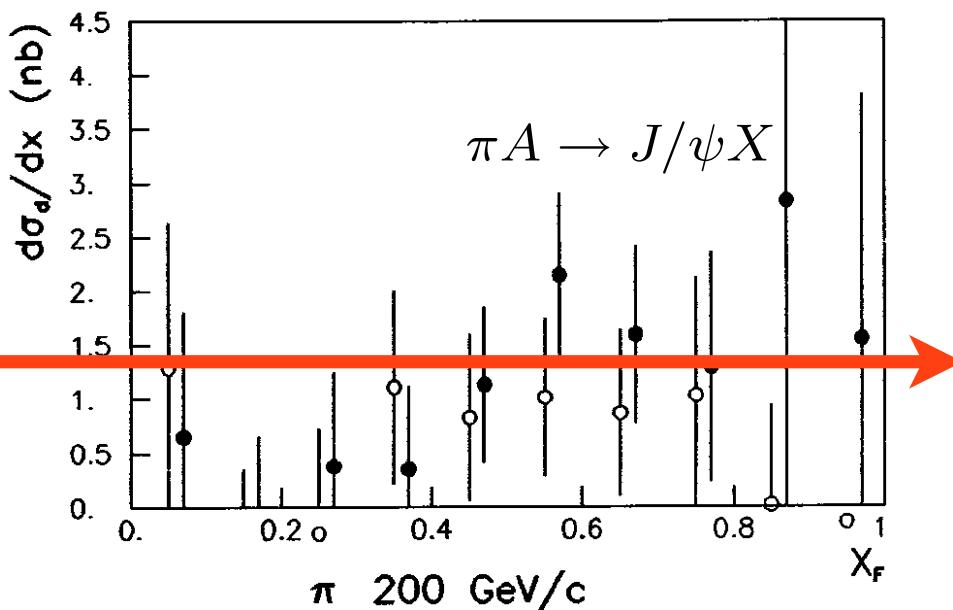
# Color-Opaque IC Fock state interacts on nuclear front surface

Kopeliovich, Schmidt,  
Soffer, sjb

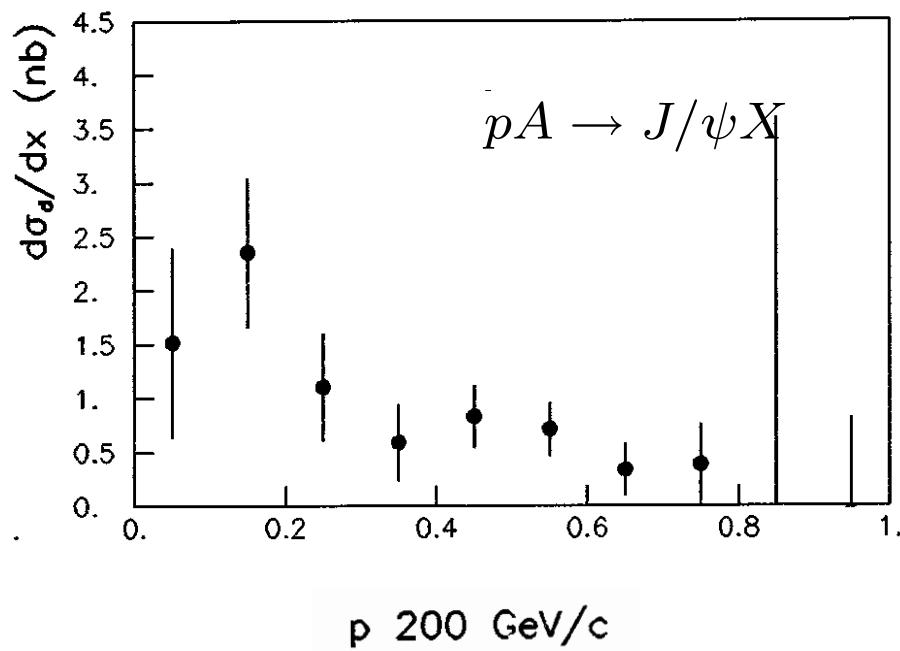
Scattering on front-face nucleon produces color-singlet  $c\bar{c}$  pair



$$\frac{d\sigma}{dx_F}(pA \rightarrow J/\psi X) = A^{2/3} \times \frac{d\sigma}{dx_F}(pN \rightarrow J/\psi X)$$



J. Badier et al, NA3



$$\frac{d\sigma}{dx_F}(pA \rightarrow J/\psi X) = A^1 \frac{d\sigma_1}{dx_F} + A^{2/3} \frac{d\sigma_{2/3}}{dx_F}$$

**Excess beyond conventional PQCD  
subprocesses**

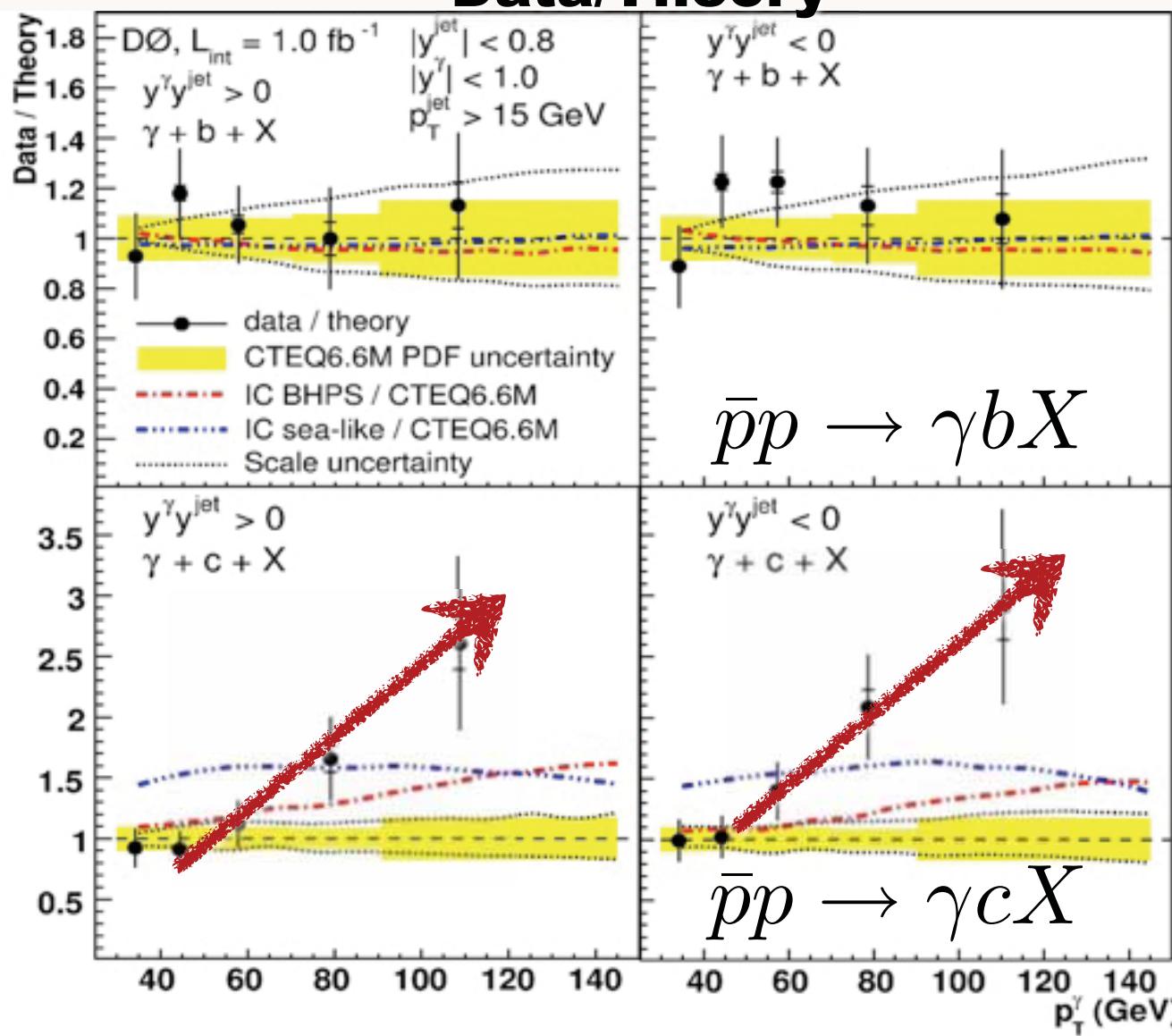
- IC Explains Anomalous  $\alpha(x_F)$  not  $\alpha(x_2)$   
dependence of  $pA \rightarrow J/\psi X$   
(Mueller, Gunion, Tang, SJB)
- Color Octet IC Explains  $A^{2/3}$  behavior at  
high  $x_F$  (NA3, Fermilab) Color Opaqueness  
(Kopeliovitch, Schmidt, Soffer, SJB)
- IC Explains  $J/\psi \rightarrow \rho\pi$  puzzle  
(Karliner, SJB)
- IC leads to new effects in  $B$  decay  
(Gardner, SJB)

## Higgs production at $x_F = 0.8$ !

Goldhaber, Kopeliovich,  
Schmidt, Soffer, sjb

Measurement of  $\gamma + b + X$  and  $\gamma + c + X$  Production Cross Sections  
in  $p\bar{p}$  Collisions at  $\sqrt{s} = 1.96$  TeV

## Data/Theory

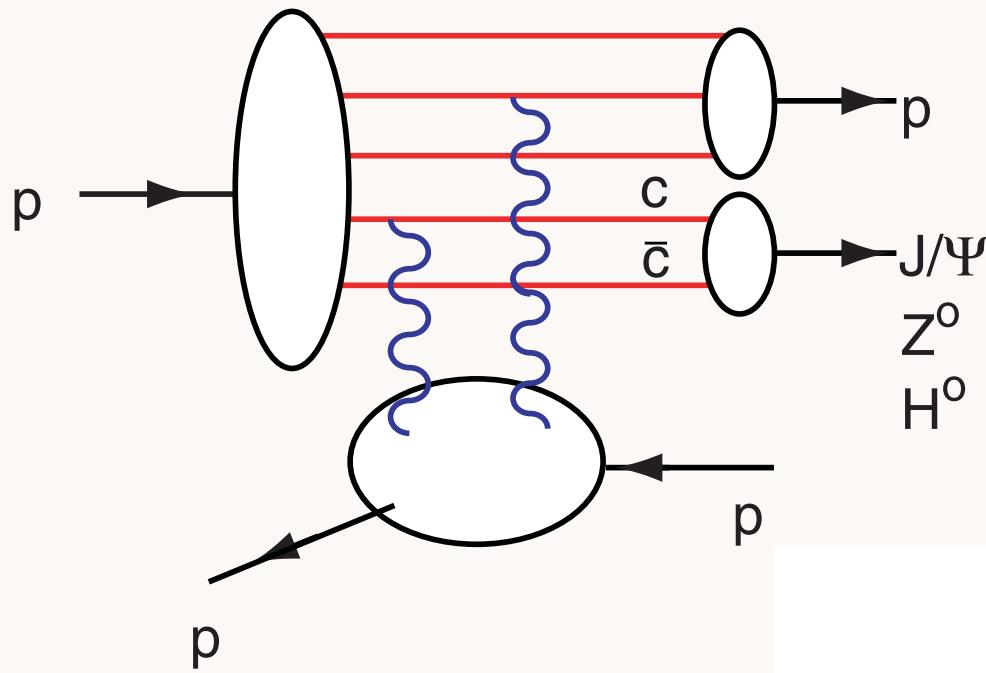


$$\frac{\Delta\sigma(\bar{p}p \rightarrow \gamma cX)}{\Delta\sigma(\bar{p}p \rightarrow \gamma bX)}$$

**Ratio  
insensitive to  
gluon PDF,  
scales**

**Signal for  
significant IC  
at  $x > 0.1$**

# Intrinsic Charm Mechanism for Exclusive Diffraction Production



$$p \ p \rightarrow J/\psi \ p \ p$$

$$x_{J/\psi} = x_c + x_{\bar{c}}$$

*Inclusive and Diffractive High- $x_F$  Higgs Production!*

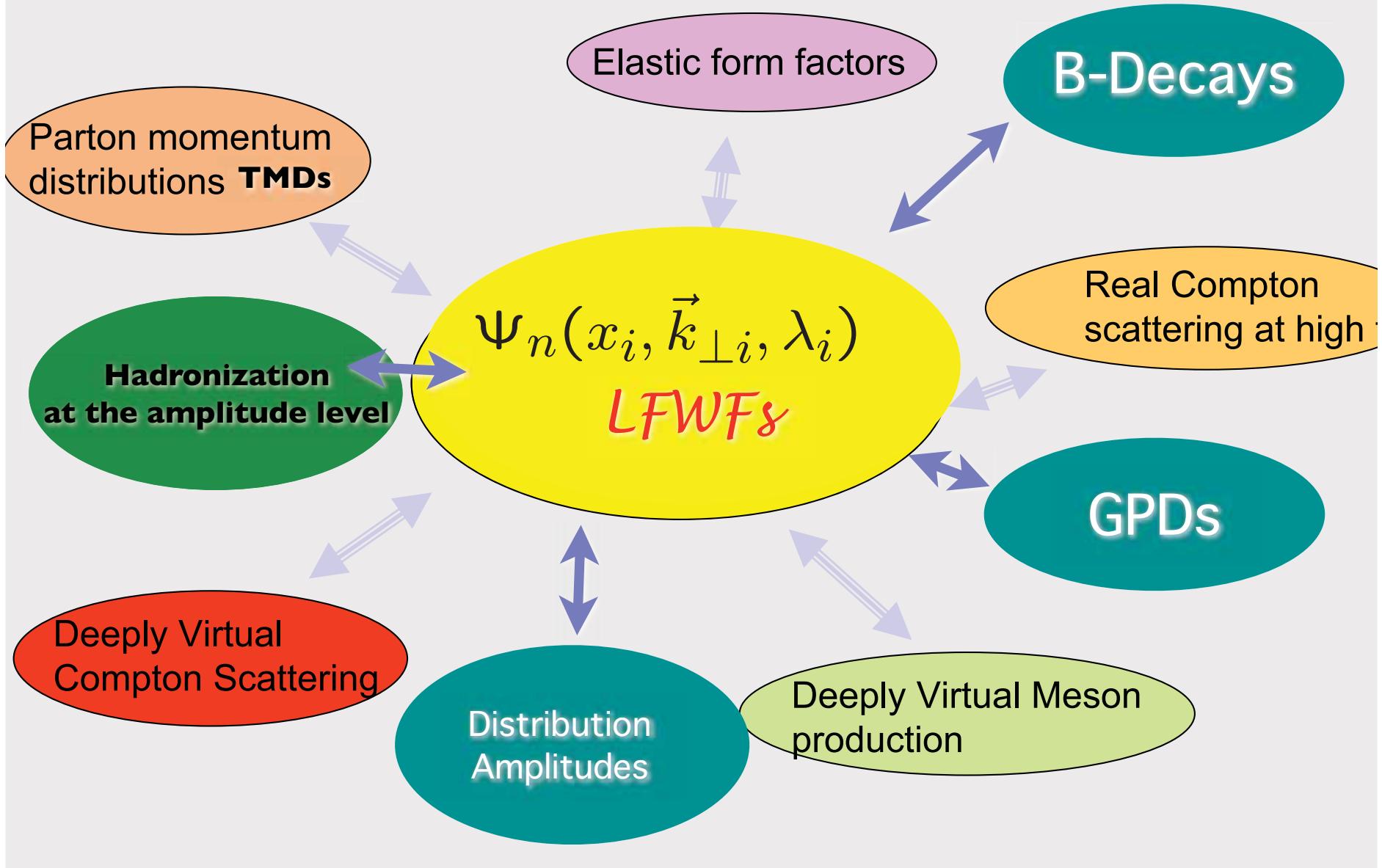
Kopeliovich, Schmidt,  
Soffer, sjb

Intrinsic  $c\bar{c}$  pair formed in color octet  $8_C$  in proton wavefunction      Large Color Dipole

Collision produces color-singlet  $J/\psi$  through  
color exchange

RHIC Experiment

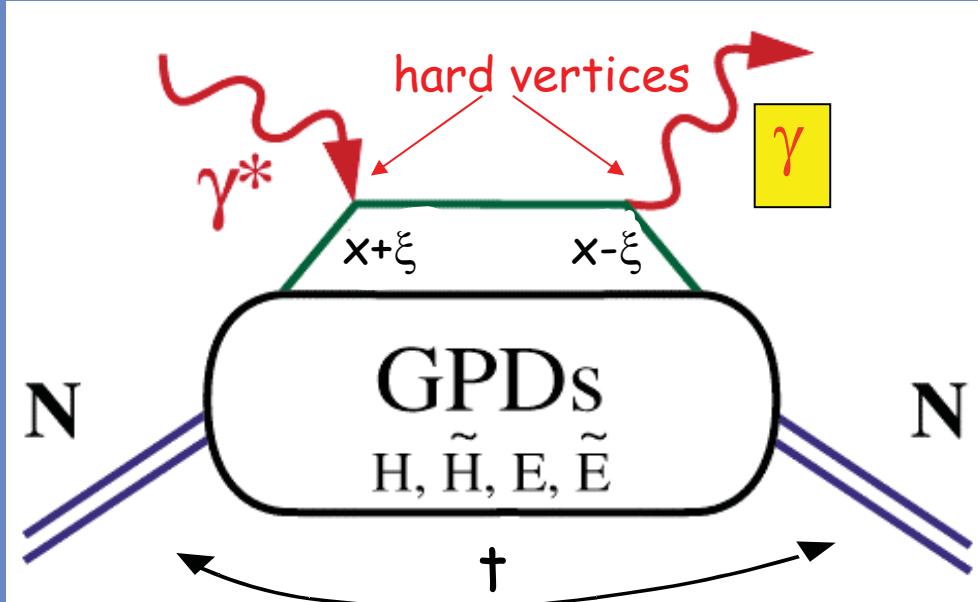
# A Unified Description of Hadron Structure



# GPDs & Deeply Virtual Exclusive Processes

## - New Insight into Nucleon Structure

### Deeply Virtual Compton Scattering (DVCS)



$x$  - quark momentum fraction

$\xi$  - longitudinal momentum transfer

$\sqrt{-\hat{\tau}}$  - Fourier conjugate to transverse impact parameter

$H(x, \xi, \hat{\tau}), E(x, \xi, \hat{\tau}), \dots$

"Generalized Parton Distributions"

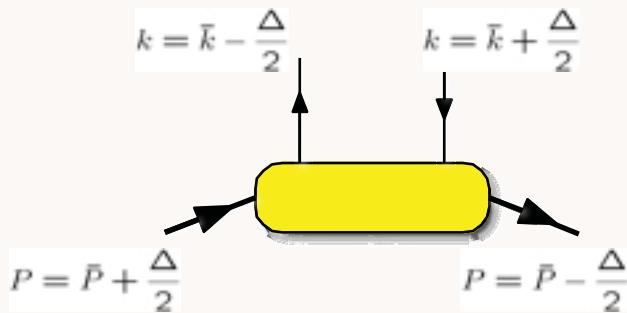
Timelike DVCS: **Mukhurjee, Afanasev, Carlson, sjb**

# Light-Front Wave Function Overlap Representation

## DVCS/GPD

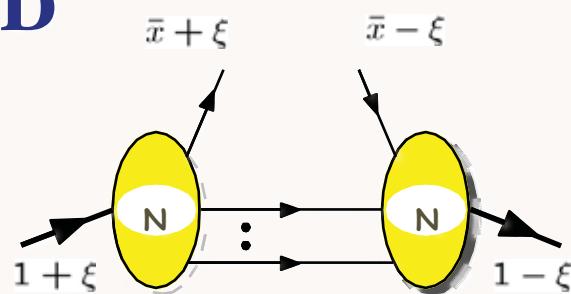
Diehl, Hwang, sjb, NPB596, 2001

See also: Diehl, Feldmann, Jakob, Kroll



$$\xi < \bar{x} < 1$$

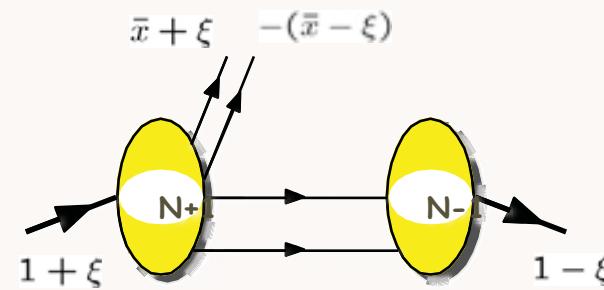
$$\sum_N$$



**DGLAP region**

$$-\xi < \bar{x} < \xi$$

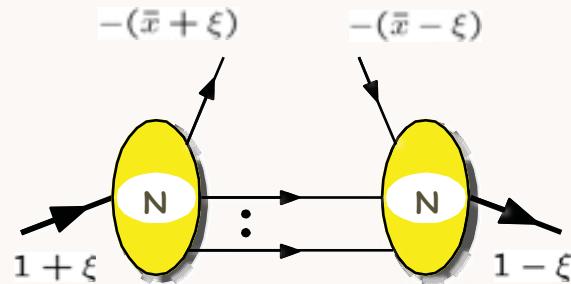
$$\sum_N$$



**ERBL region**

$$-1 < \bar{x} < -\xi$$

$$\sum_N$$



**DGLAP region**

**Bakker & JI Lorce**

# Example of LFWF representation of GPDs ( $n+I \Rightarrow n-I$ )

Diehl, Hwang, sjb

$$\begin{aligned}
& \frac{1}{\sqrt{1-\zeta}} \frac{\Delta^1 - i\Delta^2}{2M} E_{(n+1 \rightarrow n-1)}(x, \zeta, t) \\
&= (\sqrt{1-\zeta})^{3-n} \sum_{n, \lambda_i} \int \prod_{i=1}^{n+1} \frac{dx_i d^2 \vec{k}_{\perp i}}{16\pi^3} 16\pi^3 \delta \left( 1 - \sum_{j=1}^{n+1} x_j \right) \delta^{(2)} \left( \sum_{j=1}^{n+1} \vec{k}_{\perp j} \right) \\
&\quad \times 16\pi^3 \delta(x_{n+1} + x_1 - \zeta) \delta^{(2)}(\vec{k}_{\perp n+1} + \vec{k}_{\perp 1} - \vec{\Delta}_{\perp}) \\
&\quad \times \delta(x - x_1) \psi_{(n-1)}^{\uparrow *}(x'_i, \vec{k}'_{\perp i}, \lambda_i) \psi_{(n+1)}^{\downarrow}(x_i, \vec{k}_{\perp i}, \lambda_i) \delta_{\lambda_1 - \lambda_{n+1}},
\end{aligned}$$

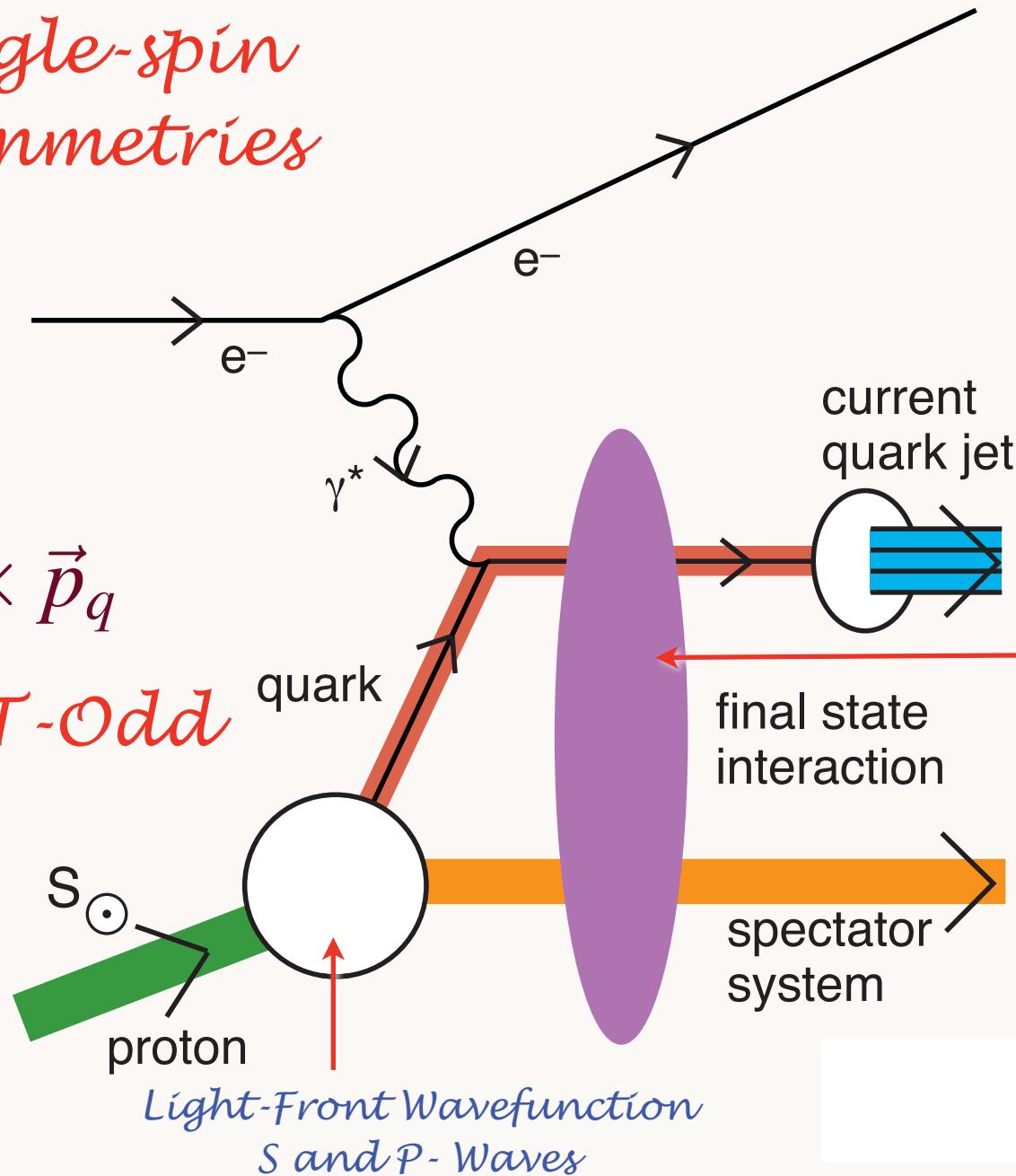
where  $i = 2, \dots, n$  label the  $n-1$  spectator partons which appear in the final-state hadron wavefunction with

$$x'_i = \frac{x_i}{1-\zeta}, \quad \vec{k}'_{\perp i} = \vec{k}_{\perp i} + \frac{x_i}{1-\zeta} \vec{\Delta}_{\perp}.$$

# Single-spin asymmetries

$$i \vec{S}_p \cdot \vec{q} \times \vec{p}_q$$

Pseudo-T-Odd



# Leading Twist Sivers Effect

Hwang, Schmidt,  
sjb

Collins, Burkardt,  
Ji, Yuan

*QCD S- and P-Coulomb Phases  
--Wilson Line*

Leading-Twist Rescattering Violates pQCD Factorization!

Sign reversal in DY!

Valencia LC2010

June 17, 2010

QCD at the Light-Front

Stan Brodsky, SLAC & CP3

# Final State Interactions Produce T-Odd (Sivers Effect)

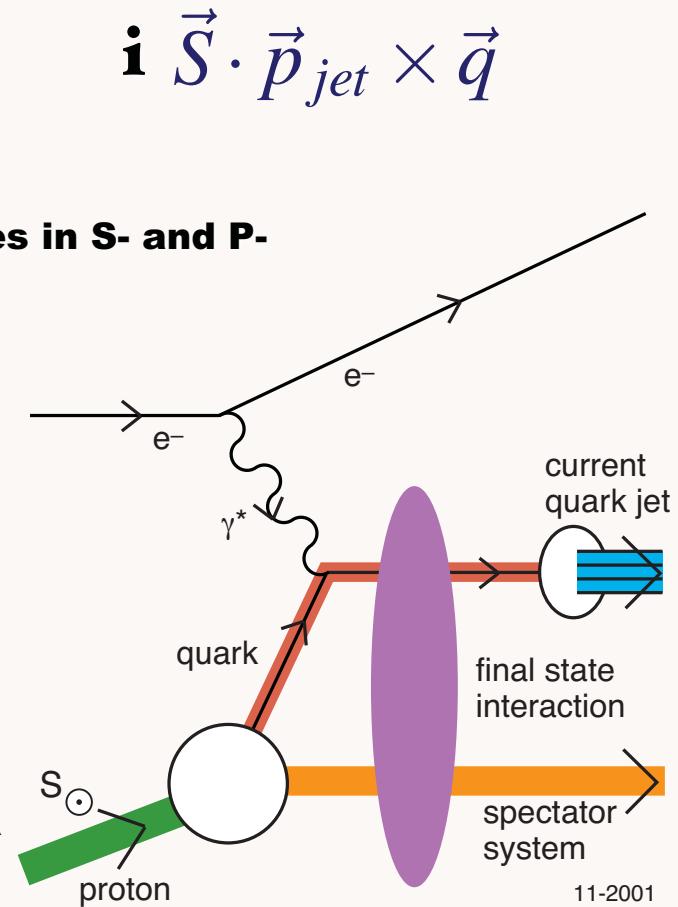
- Bjorken Scaling!
- Arises from Interference of Final-State Coulomb Phases in S and P waves
- Relate to the quark contribution to the target proton anomalous magnetic moment
- Sum of Sivers Functions for all quarks and gluons vanishes. (Zero anomalous gavitomagnetic moment)  
$$\vec{S} \cdot \vec{p}_{jet} \times \vec{q}$$

Hwang, Schmidt.  
sjb; Burkardt

# Final-State Interactions Produce Pseudo T-Odd (Sivers Effect)

Hwang, Schmidt, sjb  
Collins

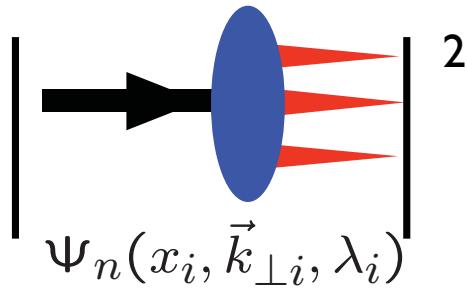
- **Leading-Twist Bjorken Scaling!**
- **Requires nonzero orbital angular momentum of quark**
- **Arises from the interference of Final-State QCD Coulomb phases in S- and P-waves;**
- **Wilson line effect -- Ic gauge prescription** Stefanis
- **Relate to the quark contribution to the target proton anomalous magnetic moment and final-state QCD phases**
- **QCD phase at soft scale!**
- **New window to QCD coupling and running gluon mass in the IR**
- **QED S and P Coulomb phases infinite -- difference of phases finite!**
- **Alternate: Retarded and Advanced Gauge: Augmented LFWFs** Pasquini, Xiao, Yuan, sjb  
Mulders, Boer Qiu, Sterman



11-2001  
8624A06

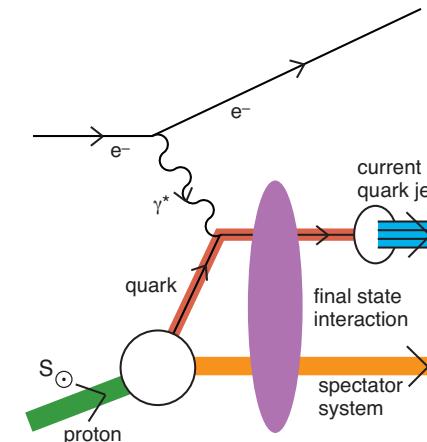
# Static

- Square of Target LFWFs
- No Wilson Line
- Probability Distributions
- Process-Independent
- T-even Observables
- No Shadowing, Anti-Shadowing
- Sum Rules: Momentum and  $J^z$
- DGLAP Evolution; mod. at large  $x$
- No Diffractive DIS



# Dynamic

- Modified by Rescattering: ISI & FSI
- Contains Wilson Line, Phases
- No Probabilistic Interpretation
- Process-Dependent - From Collision
- T-Odd (Sivers, Boer-Mulders, etc.)
- Shadowing, Anti-Shadowing, Saturation
- Sum Rules Not Proven
- DGLAP Evolution
- Hard Pomeron and Odderon Diffractive DIS



Hwang,  
Schmidt, sjb,  
Mulders, Boer  
Qiu, Sterman  
Collins, Qiu  
Pasquini, Xiao,  
Yuan, sjb

# QCD Lagrangian

The diagram illustrates the components of the QCD Lagrangian. A red box encloses the main equation, with three arrows pointing to its parts: 'gluon dynamics' points to the first term, 'quark kinetic energy + quark-gluon dynamics' points to the second term, and 'mass term' points to the third term.

$$\mathcal{L}_{QCD} = -\frac{1}{4}Tr(G^{\mu\nu}G_{\mu\nu}) + \sum_{f=1}^{n_f} i\bar{\Psi}_f D_\mu \gamma^\mu \Psi_f + \sum_{f=1}^{n_f} m_f \bar{\Psi}_f \Psi_f$$
$$iD^\mu = i\partial^\mu - gA^\mu \quad [D^\mu, D^\nu] = igG^{\mu\nu}$$

$\lim N_C \rightarrow 0$  at fixed  $\alpha = C_F \alpha_s, n_\ell = n_F/C_F$

Analytic limit of QCD: Abelian Gauge Theory

**QCD** → **QED**

P. Huet, sjb

*QED ( $N_C=0$ ): Underlies Atomic Physics, Molecular Physics, Chemistry, Electromagnetic Interactions ...*

*QCD: Underlies Hadron Physics, Nuclear Physics, Strong Interactions, Jets*

## *Theoretical Tools*

- Feynman diagrams and perturbation theory
- Bethe Salpeter Equation, Dyson-Schwinger Equations
- Lattice Gauge Theory, Hägler, Lepage
- Light-Front Methods: Discretized Light-Front Quantization, Transverse Lattice
- AdS/CFT !

*LF Quantization*

Bjorken, Kogut, Soper, Susskind

*LFWFS and Exclusive QCD:*

Lepage and SJB, Efremov, Radyushkin

*RGE and LF Hamiltonians:*

Glazek & Wilson

*DLCQ:*

Hornbostel, Pauli, & SJB

Pinsky, Hiller

*Renormalization of  $H_{LF}$*

Hiller, Chabysheva, Pauli, Pinsky, McCartor, Suaya, sjb

*Rotation Invariance, Regularization*

Karmanov, Mathiot

*Zero-Modes: Standard Model*

Srivastava, sjb

# Light-Front formalism links dynamics to spectroscopy

$$L^{QCD} \rightarrow H_{LF}^{QCD}$$

Physical gauge:  $A^+ = 0$

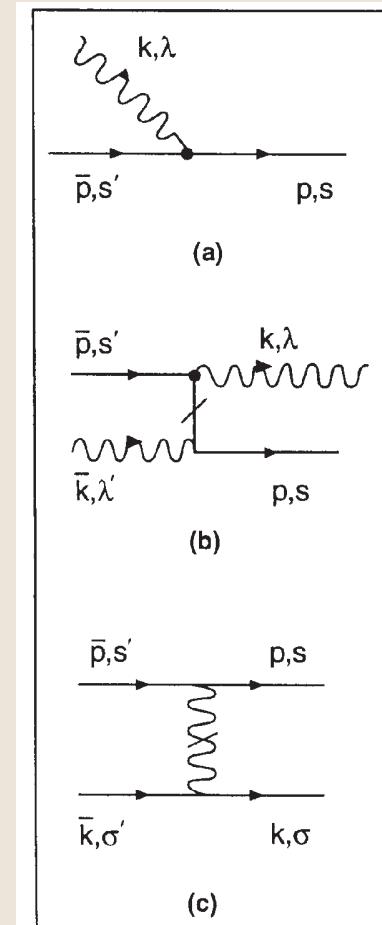
**Heisenberg Matrix  
Formulation**

$$H_{LF}^{QCD} = \sum_i \left[ \frac{m^2 + k_\perp^2}{x} \right]_i + H_{LF}^{int}$$

$H_{LF}^{int}$ : Matrix in Fock Space

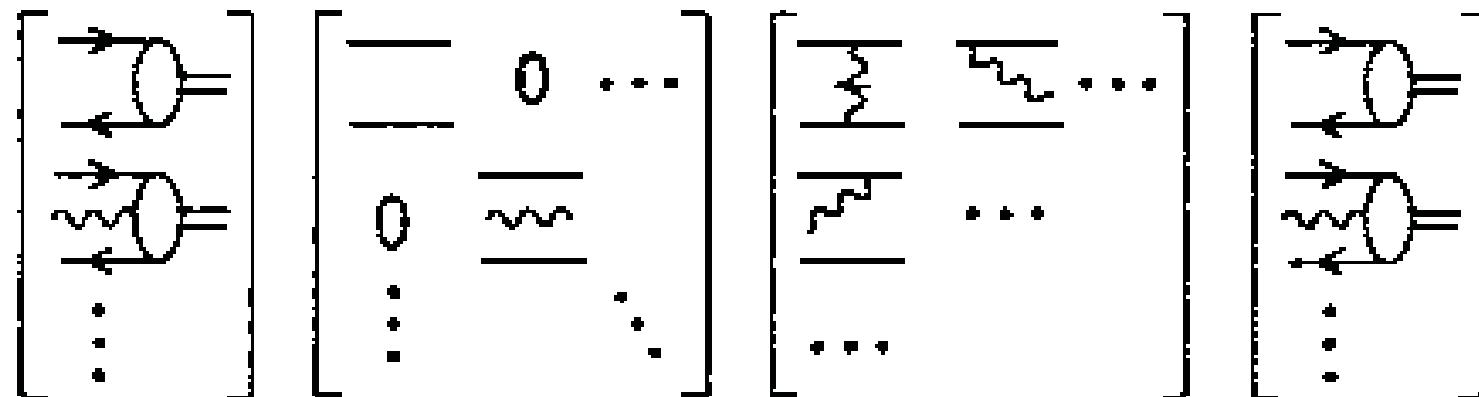
$$H_{LF}^{QCD} |\Psi_h\rangle = \mathcal{M}_h^2 |\Psi_h\rangle$$

Eigenvalues and Eigensolutions give Hadron Spectrum and Light-Front wavefunctions



# LIGHT-FRONT SCHRÖDINGER EQUATION

$$\left( M_\pi^2 - \sum_i \frac{\vec{k}_{\perp i}^2 + m_i^2}{x_i} \right) \begin{bmatrix} \psi_{q\bar{q}/\pi} \\ \psi_{q\bar{q}g/\pi} \\ \vdots \end{bmatrix} = \begin{bmatrix} \langle q\bar{q} | V | q\bar{q} \rangle & \langle q\bar{q} | V | q\bar{q}g \rangle & \cdots \\ \langle q\bar{q}g | V | q\bar{q} \rangle & \langle q\bar{q}g | V | q\bar{q}g \rangle & \cdots \\ \vdots & \vdots & \ddots \end{bmatrix} \begin{bmatrix} \psi_{q\bar{q}/\pi} \\ \psi_{q\bar{q}g/\pi} \\ \vdots \end{bmatrix}$$



$$A^+ = 0$$

**G.P. Lepage, sjb**

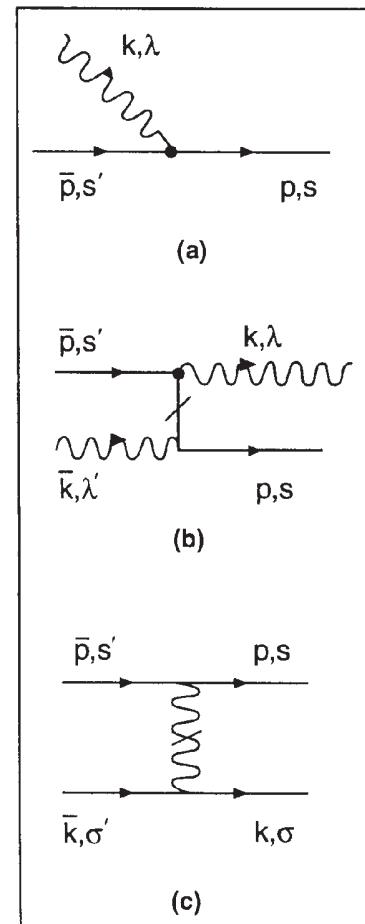
# Light-Front QCD

## Heisenberg Matrix Formulation

$$H_{LF}^{QCD} |\Psi_h\rangle = \mathcal{M}_h^2 |\Psi_h\rangle$$

H.C. Pauli & sjb

Discretized Light-Cone  
Quantization

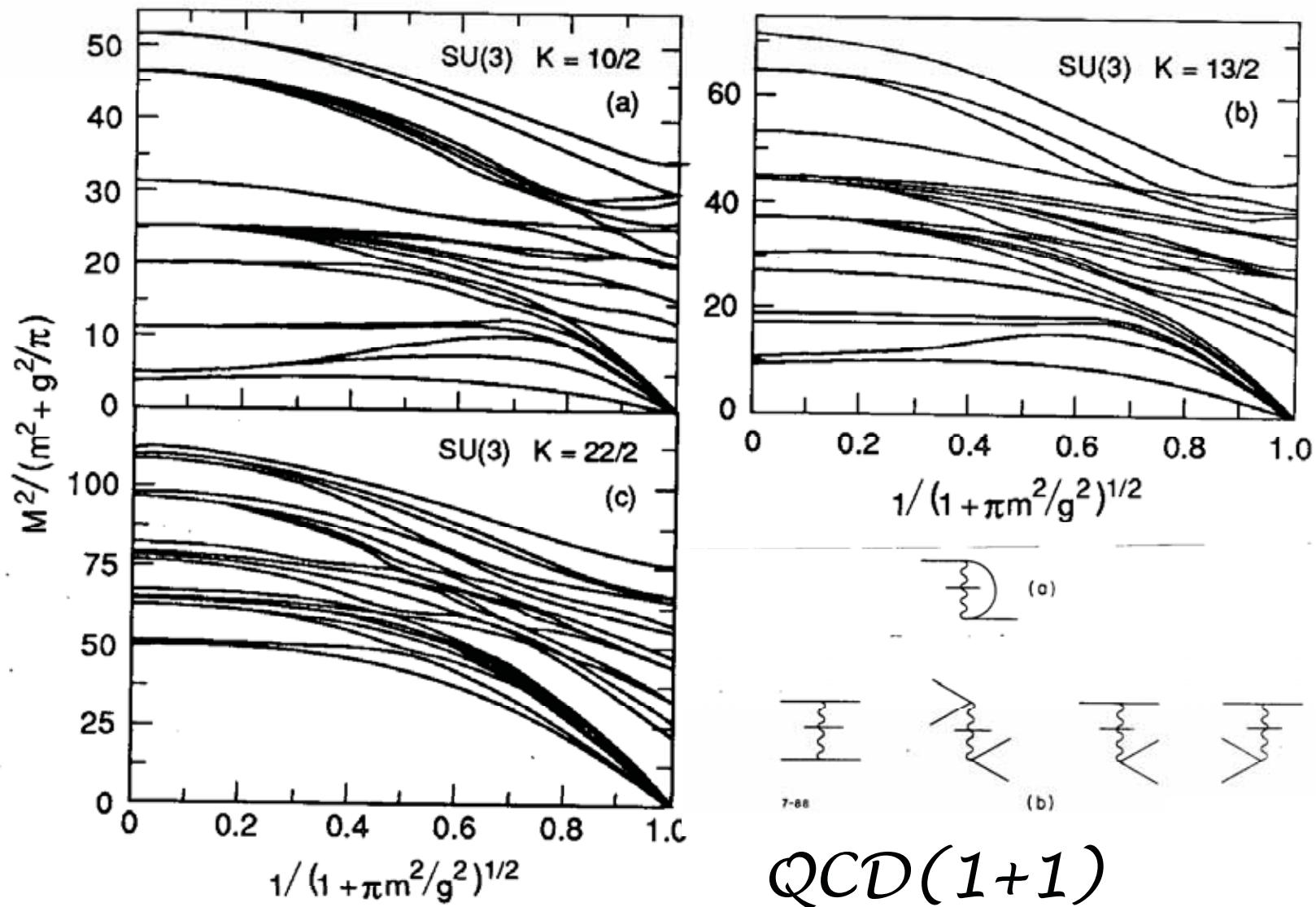


n	Sector	1 $q\bar{q}$	2 $gg$	3 $q\bar{q}g$	4 $q\bar{q}q\bar{q}$	5 $ggg$	6 $q\bar{q}gg$	7 $q\bar{q}q\bar{q}g$	8 $q\bar{q}q\bar{q}q\bar{q}$	9 $gggg$	10 $q\bar{q}ggg$	11 $q\bar{q}q\bar{q}gg$	12 $q\bar{q}q\bar{q}q\bar{q}g$	13 $q\bar{q}q\bar{q}q\bar{q}q\bar{q}$
1	$q\bar{q}$					.		.	.	.	.	.	.	.
2	$gg$				.			.	.		.	.	.	.
3	$q\bar{q}g$								.			.	.	.
4	$q\bar{q}q\bar{q}$		.			.				.	.		.	.
5	$ggg$	.			.			.	.		.	.	.	.
6	$q\bar{q}gg$							.	.			.	.	.
7	$q\bar{q}q\bar{q}g$	.	.			.				.				.
8	$q\bar{q}q\bar{q}q\bar{q}$	.	.	.		.					.	.		
9	$gggg$	.		.	.			.	.			.	.	.
10	$q\bar{q}ggg$	.	.		.				.			.	.	.
11	$q\bar{q}q\bar{q}gg$	.	.	.		.				.				.
12	$q\bar{q}q\bar{q}q\bar{q}g$	.	.	.	.	.				.	.			
13	$q\bar{q}q\bar{q}q\bar{q}q\bar{q}$	.	.	.	.	.	.		.	.	.	.		

Eigenvalues and Eigensolutions give Hadron Spectrum and Light-Front wavefunctions

DLCQ: Frame-independent, No fermion doubling; Minkowski Space

DLCQ: Periodic BC in  $x^-$ . Discrete  $k^+$ ; frame-independent truncation



Spectra for  $N = 3$ , baryon number  $B = 0, 1$  and  $2$  as a function of  $g/m$ ;  $K$  fixed.

### Light Cone Quantized QCD in (1+1)-Dimensions.

[Kent Hornbostel](#), [Stanley J. Brodsky](#), (SLAC) , [Hans Christian Pauli](#), (Heidelberg, Max Planck Inst.) . SLAC-PUB-4678, Phys.Rev.D41:3814,1990.



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# Quantum chromodynamics and other field theories on the light cone

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# *Goal: an analytic first approximation to QCD*

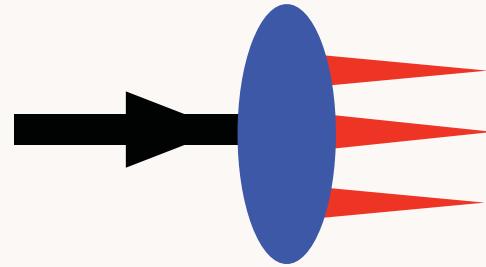
- **As Simple as Schrödinger Theory in Atomic Physics**
- **Relativistic, Frame-Independent, Color-Confining**
- **QCD Coupling at all scales**
- **Hadron Spectroscopy**
- **Light-Front Wavefunctions**
- **Form Factors, Hadronic Observables, Constituent Counting Rules**
- **Insight into QCD Condensates**
- **Systematically improvable**  
**de Teramond, Deur, Shrock, Roberts, Tandy**

# Light-Front Holography and Non-Perturbative QCD

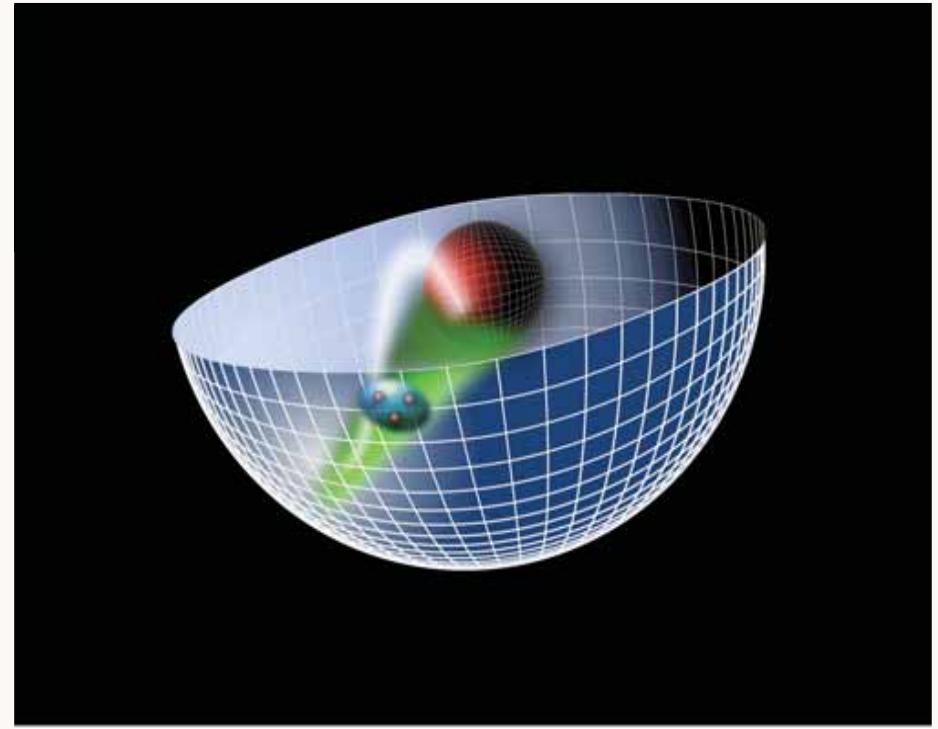
*Goal:*

**Use AdS/QCD duality to construct  
a first approximation to QCD**

Hadron Spectrum  
Light-Front Wavefunctions,  
Running coupling in IR



$$\Psi_n(x_i, \vec{k}_{\perp i}, \lambda_i)$$



in collaboration with  
Guy de Teramond and Alexandre Deur

***Central problem for strongly-coupled gauge theories***

# Light-Front Wavefunctions

Dirac's Front Form: Fixed  $\tau = t + z/c$

$$\Psi(x, k_{\perp})$$

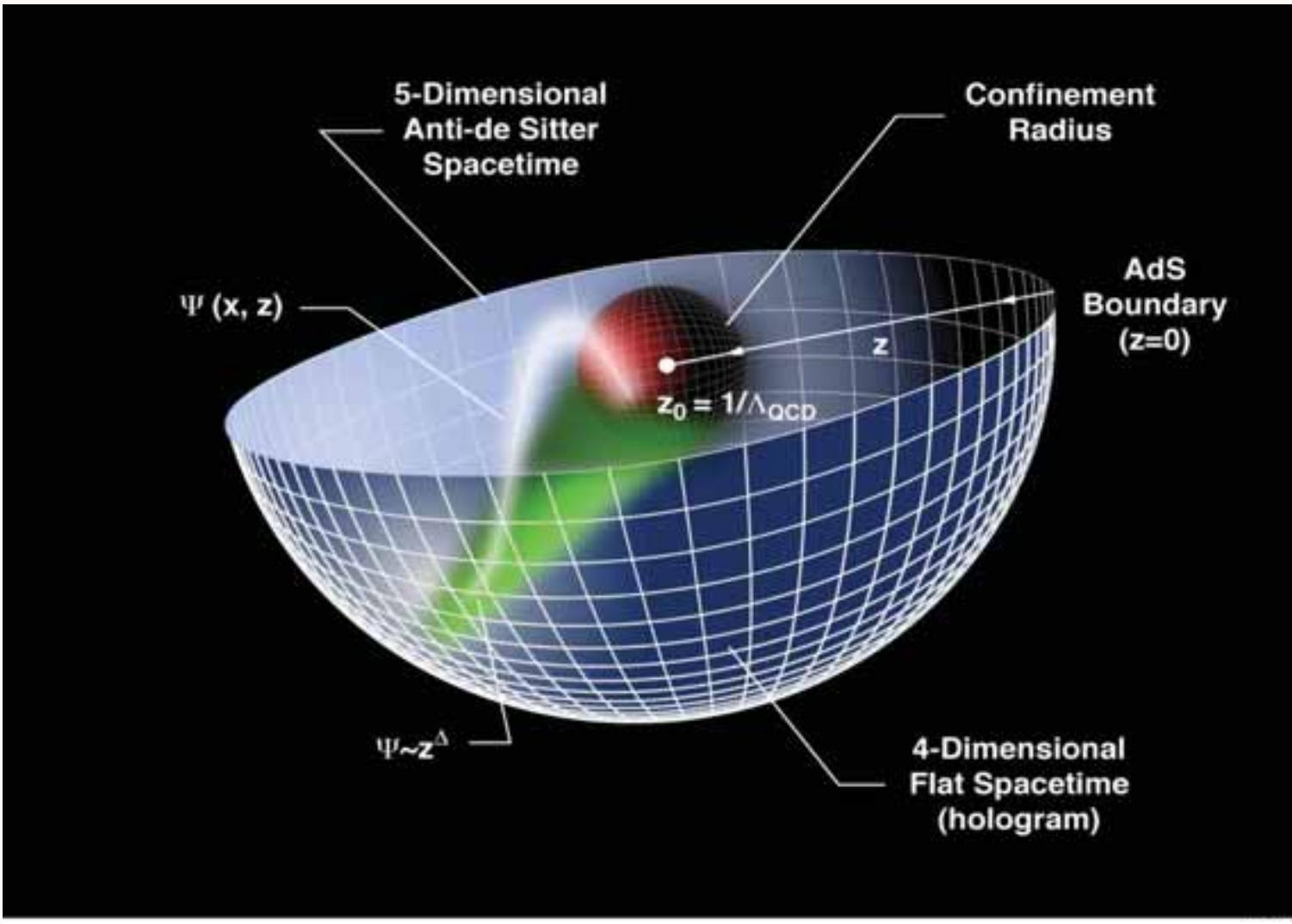
$$x_i = \frac{k_i^+}{P^+}$$

Invariant under boosts. Independent of  $P^\mu$

$$H_{LF}^{QCD} |\Psi\rangle = M^2 |\Psi\rangle$$

*Remarkable new insights from AdS/CFT, the duality between conformal field theory and Anti-de Sitter Space*

# *Applications of AdS/CFT to QCD*



*Changes in physical length scale mapped to evolution in the 5th dimension  $z$*

**in collaboration with Guy de Teramond**

Conformal Theories are invariant under the Poincare and conformal transformations with

$$M^{\mu\nu}, P^\mu, D, K^\mu,$$

the generators of  $SO(4,2)$

**SO(4,2) has a mathematical representation on AdS<sub>5</sub>**

# *AdS/CFT: Anti-de Sitter Space / Conformal Field Theory*

Maldacena:

*Map  $AdS_5 \times S_5$  to conformal  $N=4$  SUSY*

- **QCD is not conformal;** however, it has manifestations of a scale-invariant theory:  
Bjorken scaling, dimensional counting for hard exclusive processes
- **Conformal window:**  $\alpha_s(Q^2) \simeq \text{const}$  at small  $Q^2$
- **Use mathematical mapping of the conformal group  $SO(4,2)$  to  $AdS_5$  space**

