# MATHEMATICAL AND COMPUTATIONAL SCIENCE 

Courses offered by Mathematical and Computational Science program are listed under the subject code MCS on the Stanford Bulletin's ExploreCourses (http://explorecourses.stanford.edu) website.

This interdisciplinary undergraduate degree program in MCS is administrated by the departments of Mathematics, Computer Science, and Statistics. It provides a core of mathematics basic to all the mathematical sciences and an introduction to concepts and techniques of computation, optimal decision making, probabilistic modeling, and statistical inference.

Using the faculty and courses of the departments listed above, this major prepares students for graduate study or employment in the mathematical and computational sciences or in those areas of applied mathematics which center around the use of computers and are concerned with the problems of the social and management sciences. A biology option is offered for students interested in applications of mathematics, statistics, and computer science to the biological sciences (bioinformatics, computational biology, statistical genetics, neurosciences); and in a similar spirit, an engineering and statistics option.

## Undergraduate Mission Statement for Mathematical and Computational Science

The mission of the Mathematical and Computational Science Program is to provide students with a core of mathematics basic to all the mathematical sciences and an introduction to concepts and techniques of computation, optimal decision making, probabilistic modeling and statistical inference. The program is interdisciplinary in its focus, and students are required to complete course work in mathematics, computer science, statistics, and management science and engineering. A computational biology track is available for students interested in biomedical applications. The program prepares students for careers in academic, financial and government settings as well as for study in graduate or professional schools.

## Learning Outcomes

The program expects undergraduate majors to be able to demonstrate the following learning outcomes. These learning outcomes are used in evaluating students and the department's undergraduate program. Students are expected to be able to demonstrate:

1. understanding of principles and tools of statistics.
2. command of optimization and its applications and the ability to analyze and interpret problems from various disciplines.
3. an understanding of computer applications emphasizing modern software engineering principles.
4. an understanding of multivariate calculus, linear algebra, and algebraic and geometric proofs.

## Bachelor of Science in Mathematical and Computational Science

The requirement for the bachelor's degree, beyond the University's basic requirements, is an approved course program of 78-84 units, distributed as follows:

| Mathematics (MATH) | 28 |
| :--- | ---: |
| MATH $41 \quad$ Calculus ${ }^{1} \quad 5$ |  |


| MATH 42 | Calculus ${ }^{1}$ | 5 |
| :---: | :---: | :---: |
| Select one of the following: |  | 5 |
| MATH 51 | Linear Algebra and Differential Calculus of Variables |  |
| MATH 51H | Honors Multivariable Mathematics |  |
| Select one of the following: |  | 5 |
| MATH 52 | Integral Calculus of Several Variables |  |
| MATH 52H | Honors Multivariable Mathematics |  |
| Select one of the following: |  | 5 |
| MATH 53 | Ordinary Differential Equations with Linear |  |
| MATH 53H | Honors Multivariable Mathematics |  |
| Select one of the following: |  | 3 |
| MATH 104 | Applied Matrix Theory |  |
| MATH 113 | Linear Algebra and Matrix Theory |  |
| Computer Science (CS) |  | 22-24 |
| CS 103 | Mathematical Foundations of Computing | 5 |
| CS 106A | Programming Methodology ${ }^{1}$ | 5 |
| and |  |  |
| CS 106B | Programming Abstractions | 5 |
| or |  |  |
| CS 106X | Programming Abstractions (Accelerated) | 5 |
| Select two of the following: |  | 7-9 |
| CME 108 | Introduction to Scientific Computing |  |
| CS 107 | Computer Organization and Systems |  |
| CS 154 | Introduction to Automata and Complexity |  |
| CS 161 | Design and Analysis of Algorithms |  |
| CS 181W | Computers, Ethics, and Public Policy |  |
| Management Science and Engineering (MS\&E) |  | 7-11 |
| MSE 211 | Linear and Nonlinear Optimization |  |
| MSE 221 | Stochastic Modeling |  |
| Or select three of the following: |  |  |
| MSE 111 | Introduction to Optimization |  |
| MSE 121 | Introduction to Stochastic Modeling |  |
| MSE 211 | Linear and Nonlinear Optimization |  |
| MSE 221 | Stochastic Modeling |  |
| MSE 251 | Stochastic Control |  |
| Statistics (STATS) |  | 11-12 |
| STATS 116 | Theory of Probability | 5 |
| STATS 200 | Introduction to Statistical Inference | 3 |
| Select one of the following: |  | 3 |
| STATS 191 | Introduction to Applied Statistics |  |
| STATS 203 | Introduction to Regression Models and An Variance |  |
| 1 Students who scored a 5 on both the Calculus $A B$ and $B C$ advanced placement exams (total of 10 units) can be waived out of MATH 41 and MATH 42; A score of 4 or 5 in Computer Science A will receive credit for CS106A (5 units). See also the Registrar's Advanced Placement (https://studentaffairs.stanford.edu/registrar/ students/ap) web site (AP (https://studentaffairs.stanford.edu/ registrar/students/baccalaureate-credit) or IB (https:// studentaffairs.stanford.edu/registrar/students/baccalaureate-credit) exams). |  |  |

## Writing in the Major Requirement

The University requires students to complete at least one approved writing-intensive course in each of their majors. See the Hume Center for Writing and Speaking (https://undergrad.stanford.edu/tutoring-support/ hume-center/writing/writing-major) web site for a full description of the

WIM (https://undergrad.stanford.edu/tutoring-support/hume-center/ writing/writing-major/overview-wim-requirement) requirement.

| Choose one from the M\&CS designated WIM courses to fulfill the | 3-4 |
| :--- | :--- |
| Writing in the Major requirement: |  |


| MATH 109 | Applied Group Theory |
| :--- | :--- |
| MATH 110 | Applied Number Theory and Field Theory |
| MATH 120 | Groups and Rings |
| MATH 171 | Fundamental Concepts of Analysis |
| CS 181W | Computers, Ethics, and Public Policy |
| STATS 155 | Statistical Methods in Computational Genetics |

## Mathematical and Computational Science Electives

Choose three courses in Mathematical and Computational Science 100level or above, at least 3 units each from two different departments. At least one must be from following list:

| Choose three courses from the following: | Units <br> en |
| :--- | :--- |
|  |  |
| ECON 102C | Advanced Topics in Econometrics |
| ECON 107 | Causal Inference and Program Evaluation |
| ECON 140 | Introduction to Financial Economics |
| ECON 160 | Game Theory and Economic Applications |
| ECON 179 | Experimental Economics |
| EE 261 | The Fourier Transform and Its Applications |
| EE 263 | Introduction to Linear Dynamical Systems |
| EE 278 | Introduction to Statistical Signal Processing |
| EE 282 | Computer Systems Architecture |
| EE 364A | Convex Optimization I |
| EE 364B | Convex Optimization II |
| MSE 220 | Probabilistic Analysis |
| MSE 223 | Simulation |
| MSE 251 | Stochastic Control |
| MCS 100 | Mathematics of Sports |
| MATH 104 | Applied Matrix Theory |
| MATH 106 | Functions of a Complex Variable |
| MATH 108 | Introduction to Combinatorics and Its Applications |
| MATH 113 | Linear Algebra and Matrix Theory |
| MATH 115 | Functions of a Real Variable |
| MATH 116 | Complex Analysis |
| MATH 131P | Partial Differential Equations I |
| MATH 171 | Fundamental Concepts of Analysis |
| MATH 172 | Lebesgue Integration and Fourier Analysis |
| MATH 174 | Calculus of Variations |
| PHIL 151 | Metalogic (Winte) |
| STATS 202 | Data Mining and Analysis |
| STATS 206 | Applied Multivariate Analysis |
| STATS 207 | Introduction to Time Series Analysis |
| STATS 208 | Introduction to the Bootstrap |
| STATS 215 | Statistical Models in Biology |
| STATS 216 | Introduction to Statistical Learning |
| STATS 217 | Introduction to Stochastic Processes |
| STATS 218 | Introduction to Stochastic Processes |
| STATS 219 | Stochastic Processes |
| STATS 240 | Statistical Methods in Finance |
| STATS 270 | Bayesian Statistics I |

For Computer Science (CS), electives can include courses not taken as units under the CS list above and the following:

| CME 206 | Introduction to Numerical Methods for Engineering |
| :--- | :--- |
| CME 211 | Software Development for Scientists and <br> Engineers |
| CME 302 | Numerical Linear Algebra |
| CS 108 | Object-Oriented Systems Design |
| CS 110 | Principles of Computer Systems |
| CS 140 | Operating Systems and Systems Programming |
| CS 143 | Compilers |
| CS 157 | Logic and Automated Reasoning |
| CS 161 | Design and Analysis of Algorithms |
| CS 194 | Software Project |
| CS 221 | Artificial Intelligence: Principles and Techniques |
| CS 223A | Introduction to Robotics |
| CS 225A | Experimental Robotics |
| CS 228 | Probabilistic Graphical Models: Principles and <br> Techniques <br> CS 229$\quad$Machine Learning <br> CS 243$\quad$ Program Analysis and Optimizations |
| CS 246 | Mining Massive Data Sets |
| CS 248 | Interactive Computer Graphics |

The following courses are not offered this year but may be used by students who completed them in fulfillment of this requirement:CS 164

With the adviser's approval, courses other than those offered by the sponsoring departments may be used to fulfill part of the elective requirement. These may be in fields such as biology, economics, electrical engineering, industrial engineering, and medicine, etc., that might be relevant to a mathematical sciences major, depending on a student's interests.

- At least three quarters before graduation, majors must file with their advisers a plan for completing degree requirements.
- All courses used to fulfill major requirements must be taken for a letter grade with the exception of courses offered satisfactory/no credit only.
- The student must have a grade point average (GPA) of 2.0 or better in all course work used to fulfill the major requirement.
- Electives that are not offered this year, but may be offered in subsequent years, are eligible for credit toward the major.


## Mathematical and Computational Science Biology Track (Option)

Students in the Biology track take the introductory courses for the Mathematics and Computational Science major with the following allowable substitutions as electives.

|  |  | Units |
| :--- | :--- | :--- |
| STATS/BIO 141 | Biostatistics $^{1}$ | $3-5$ |
| Take three courses from the Biology Core: | 10 |  |
| BIO 41 | Genetics, Biochemistry, and Molecular Biology |  |
| BIO 42 | Cell Biology and Animal Physiology |  |
| BIO 43 | Plant Biology, Evolution, and Ecology |  |
| Or take two courses from the core and one of the following: | $3-4$ |  |
| BIO 136 | Evolutionary Paleobiology |  |
| BIO 143 | Evolution |  |
| BIO 144 | Conservation Biology: A Latin American |  |
| BIO 183 | Perspective | Theoretical Population Genetics |


| B10 230 | Molecular and Cellular Immunology |
| :---: | :---: |
| Honors students select the following three courses: |  |
| STATS 155 | Statistical Methods in Computational Genetics |
| BIO 113 | Fundamentals of Molecular Evolution |
| BIO 146 | Population Studies |
| The following courses are not offered this year but may be used by students who completed them in fulfillment of this requirement: BIO102, 160A \& 160B |  |
| Can replace STATS 191 Introduction to Applied Statistics or STATS 203 Introduction to Regression Models and Analysis of Variance |  |
| Mathemati <br> Track (Opt | and Computational Science Enginee |

Students in the Engineering track take the introductory courses for the Mathematics and Computational Sciences major with the following allowable substitutions.

With consent of an MCS advisor, MATH 51-52-53 series may be substituted for CME 100-102-104. Depending on the exact material taught in relevant years, an additional math course might be necessary **

| CME 100 | Vector Calculus for Engineers |
| :--- | :--- |
| CME 102 | Ordinary Differential Equations for Engineers |
| CME 104/ | Linear Algebra and Partial Differential Equations |
| ENGR 155B | for Engineers |

STATS 116 may be replaced by: 3-5

STATS $110 \quad$| Statistical Methods in Engineering and the |
| :--- |
| Physical Sciences |

STATS 191/STATS 203 may be replaced by: 3-4

STATS 202 Data Mining and Analysis
Engineering Track Electives:
Select one of the following: 3-4

| MATH 106 | Functions of a Complex Variable |
| :--- | :--- |
| MATH 108 | Introduction to Combinatorics and Its Applications |
| MATH 116 | Complex Analysis |
| MATH 118 | Mathematics of Computation |
| MATH 132 | Partial Differential Equations II |
| MATH 174 | Calculus of Variations |
| PHIL 151 | Metalogic |
| Select two of the following: | $3-5$ |

ENGR 15 Dynamics
ENGR 20 Introduction to Chemical Engineering
ENGR 25B Biotechnology
ENGR 30 Engineering Thermodynamics
ENGR 40 Introductory Electronics
ENGR 50 Introduction to Materials Science, Nanotechnology Emphasis
ENGR 105 Feedback Control Design
** Only M\&CS majors pursuing the engineering track may petition their adviser to substitute the required Math series for CME courses listed above.

## Mathematical and Computational Science Statistics 1-4 Track (Option)

Students in the Statistics track take the introductory courses for the Mathematics and Computational Sciences major with the following additional courses - (87 units total)

## Required:

|  |  | Units |
| :---: | :---: | :---: |
| STATS 217 | Introduction to Stochastic Processes | 3 |
| Advanced CS, such as: |  |  |
| CS 246 | Mining Massive Data Sets | 3-4 |
| Advanced MS\&E, such as: |  |  |
| MSE 220 | Probabilistic Analysis | 3-4 |
| or |  |  |
| MSE 223 | Simulation |  |
| Statistics Track Electives: |  |  |
| Select three of | following: | 9 |
| STATS 202 | Data Mining and Analysis |  |
| STATS 206 | Applied Multivariate Analysis |  |
| STATS 207 | Introduction to Time Series Analysis |  |
| STATS 208 | Introduction to the Bootstrap |  |
| STATS 216 | Introduction to Statistical Learning |  |
| STATS 219 | Stochastic Processes |  |
| STATS 270 | Bayesian Statistics I |  |

## Honors Program

The honors program is designed to encourage a more intensive study of mathematical sciences than the B.S. program. In addition to meeting all requirements for the B.S., the student must:

1. Maintain an average letter grade equivalent to at least a 3.5 in all academic work.
2. Complete at least 15 units in mathematical sciences in addition to the requirements for the major listed above. Include in these 15 units at least one of the following:
a. An approved upper-level or graduate course
b. Participation in a small group seminar
c. At least 3 units of directed reading
3. Prepare a statement describing major area of concentration for honors work.
4. Describe how each course selected added to the student's knowledge and understanding in area chosen for concentration.
5. Students interested in honors should consult with their adviser by last quarter of their junior year to prepare their program of study. Honors work may be concentrated in fields such as biological sciences, environment, physics, etc.
6. Suggested electives for students pursuing Honors: CME 206, CS 229, CS 248, EE 364, MATH 171, MATH 172, STATS 202, STATS 216, STATS 217.

## Minor in Mathematical and Computational Science

The minor in Mathematical and Computational Science is intended to provide an experience of the four constituent areas: Computer Science, Mathematics, Management Science and Engineering, and Statistics. Five basic courses are required:

Select two of the followning: 10
CS 106A Programming Methodology
and

| CS 106B | Programming Abstractions |  |
| :---: | :---: | :---: |
| or |  |  |
| CS 106X | Programming Abstractions (Accelerated) |  |
| Select one of the following: |  | 3-5 |
| MATH 51 | Linear Algebra and Differential Calculus of Several Variables |  |
| or |  |  |
| MATH 104 | Applied Matrix Theory |  |
| Select one of the | following: | 3-4 |
| MSE 211 | Linear and Nonlinear Optimization |  |
| or |  |  |
| MSE 221 | Stochastic Modeling |  |
| Select two of the | following: | 8 |
| STATS 116 | Theory of Probability |  |
| and either |  |  |
| STATS 191 | Introduction to Applied Statistics |  |
| or |  |  |
| STATS 200 | Introduction to Statistical Inference |  |

In addition to the above, the minor requires three courses from the following, two of which must be in different departments:

Lester Mackey (Statistics), Parviz Moin (Engineering), George Papanicolaou (Mathematics), Eric Roberts (Computer Science), David Rogosa (Education), Tim Roughgarden (Computer Science), Chiara Sabatti (Statistics), Amin Saberi (Management Science and Engineering), David Siegmund (Statistics), Jonathan Taylor (Statistics), Brian White (Mathematics).

|  |  |
| :--- | :--- |
|  | Units |
| Select three of the following: |  |
| CME 108 | Introduction to Scientific Computing |
| CS 103 | Mathematical Foundations of Computing |
| CS 107 | Computer Organization and Systems |
| CS 154 | Introduction to Automata and Complexity Theory |
| CS 161 | Design and Analysis of Algorithms |
| EE 261 | The Fourier Transform and Its Applications |
| ECON 160 | Game Theory and Economic Applications |
| MSE 251 | Stochastic Control |
| MATH 104 | Applied Matrix Theory |
| MATH 106 | Functions of a Complex Variable |
| MATH 108 | Introduction to Combinatorics and Its Applications |
| MATH 109 | Applied Group Theory |
| MATH 110 | Applied Number Theory and Field Theory |
| MATH 115 | Functions of a Real Variable |
| MATH 131P | Partial Differential Equations I |
| MATH 171 | Fundamental Concepts of Analysis |
| MATH 174 | Calculus of Variations |
| PHIL 151 | Metalogic |
| STATS 191 | Introduction to Applied Statistics |
| STATS 200 | Introduction to Statistical Inference |
| STATS 202 | Data Mining and Analysis |
| STATS 203 | Introduction to Regression Models and Analysis of |
| STATS 217 | Introduction to Stochastic Processes |

Other upper-division courses appropriate to the program major may be substituted with consent of the program director. Undergraduate majors in the constituent programs may not count courses in their own departments.

Co-Directors: Bradley Efron, Susan Holmes
Steering Committee: Takeshi Amemiya (Economics, emeritus), Emmanuel Candes (Mathematics, Statistics), Gunnar Carlsson (Mathematics), Richard Cottle (Management Science and Engineering, emeritus), Bradley Efron (Statistics), Margot Gerritsen (ICME), Peter Glynn (Management Science and Engineering), Susan Holmes (Statistics),

